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Should Consensus Suppress the Individual ?

Frank Dodd (Tony) Smith, Jr. - 2017 - viXra 1705.0271

Consider two cases, each with

Consensus = the Physics Establishment including: Fermilab, CDF, and D0 Collaborations (pages 8-16); the Cornell arXiv (pages 13; 23-24); CERN CDS (pages 14; 24) LHC, ATLAS, and CMS Collaborations (pages 17-22); the Princeton Institute for Advanced Study (page 22); and the Simons Center for Geometry and Physics (page 22)

and

Individual = I, a Georgia lawyer with a 1963 AB in math from Princeton and some physics study at Georgia Tech with David Finkelstein as adviser, but, having at age 50 failed the Fall 1991 Georgia Tech Comprehensive Exam (a 3-day closed book exam), I have no physics degree

First Case (pages 4-22): Our Universe: Is it Stable ? Consensus = NO (only metastable) Individual = YES

Second Case (pages 23-29): Dark Energy and Dark Matter Consensus = Unknown Individual = Known Segal Conformal Structure

This paper is a brief description of interactions between Consensus and Individual in each of those two cases. Since I, the author, have been directly involved, you should read this paper bearing in mind possible bias in my point of view that might also be present in this paper. Bearing that in mind, you should decide for yourself the answer to the question posed in the title of this paper.

The following two pages descibe how I use in this paper histogram interpretation terminology:

observation - evidence - indication

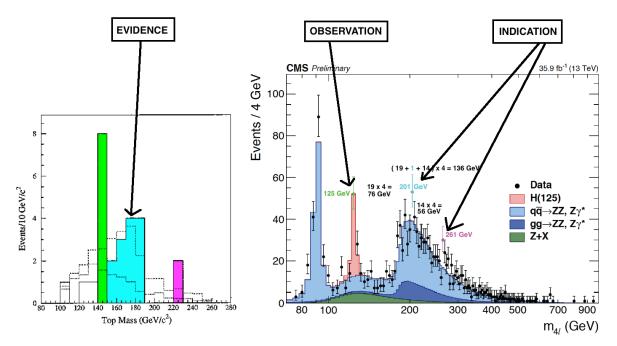
As I use in this paper, this is what I mean by each of these three terms:

Observation - means a state is conclusively observed in that there is no reasonable doubt as to the histogram bin peak corresponding to the state. Example: 125 GeV Higgs peak in 2016 CMS Higgs -> ZZ* -> 4I channel.

Evidence - means that the histogram bins very likely correspond to the state, in that the correspondence exists by preponderance of the evidence. Example: 174 GeV Tquark peak in 1994 semileptonic histogram in FERMILAB-PUB-94/097-E by CDF.

Indication - means that the histogram bins, when **subjectively** considered as to their height and that of adjacent bins, and expected background, seem to me to indicate a possible correspondence between the histogram bins and the state.

Example: 201 and 261 GeV peaks in 2016 CMS Higgs -> ZZ* -> 4I channel possibly corresponding to Higgs Mass States at 200 GeV and 260 GeV.



Note that, particularly in earlier experiments with low numbers of events and with respect to some NJL model calculations, the Mass numbers in GeV are more "in the area of", meaning roughly +/- 10% or so, than "exact".

Particularly with respect to Indication, I rely on my **subjective** seat-of-the-pants intuition more than on objective statistical criteria. Such **subjective** criteria may be harder to formulate than simpler objective statistical criteria, but when evaluating the usefulness of specific physics models (such as Nambu-Jona-Lasinio) **subjective** intuition may be the most effective technique. As to how to formulate it with respect to well-known math,

my guess is that it would be most accurately formulated in terms of Bayesian Statistics. Wikipedia says "... The Bayesian design of experiments includes a concept called 'influence of prior beliefs'.

This approach uses sequential analysis techniques to include the outcome of earlier experiments in the design of the next experiment. ...".

With respect to this paper and experiments discussed herein: Nambu-Jona-Lasinio model theory leads to belief in three Higgs-Tquark Mass states:

Higgs = 260 GeV and Tquark = 220 GeV Higgs = 200 GeV and Tquark = 174 GeV Higgs = 125 GeV and Tquark = 130 GeV

1994 CDF saw Indications of Tquark Mass states in the area of 130 GeV and 220 GeV 1997 D0 saw Indications of Tquark Mass states in the area of 130 GeV and 220 GeV Both experiments strengthen belief in the states

> Higgs = 260 GeV and Tquark = 220 GeV Higgs = 125 GeV and Tquark = 130 GeV

2011-2012 LHC Higgs -> ZZ* -> 4I ATLAS saw Indications of Higgs Mass states in the area of 200 GeV and 260 GeV and Observation of Higgs Mass state at 125 GeV 2011-2012 LHC Higgs -> ZZ* -> 4I CMS saw Indications of Higgs Mass states in the area of 200 GeV and 260 GeV and Observation of Higgs Mass state at 125 GeV Both experiments strengthened belief in all 3 Nambu-Jona-Lasinio states.

2015 LHC Higgs -> ZZ* -> 4I ATLAS saw Indications of Higgs Mass states in the area of 200 GeV and 260 GeV and Observation of Higgs Mass state at 125 GeV 2015 LHC Higgs -> ZZ* -> 4I CMS saw Indications of Higgs Mass states in the area of 200 GeV and 260 GeV and Observation of Higgs Mass state at 125 GeV Both experiments strengthened belief in all 3 Nambu-Jona-Lasinio states

2016 LHC Higgs -> ZZ* -> 4I ATLAS saw, for the first 14.8 fb-1 of the total 36.1 fb-1, Indications of Higgs Mass states in the area of 200 GeV and 260 GeV and Observation of Higgs Mass state at 125 GeV 2016 LHC Higgs -> ZZ* -> 4I CMS saw Indications of Higgs Mass states in the area of 200 GeV and 260 GeV and Observation of Higgs Mass state at 125 GeV

Based on consistently increasing belief in 3 Nambu-Jona-Lasinio states over 20 years of Fermilab and LHC experiments, I am hopeful that if the 2017 LHC run gets the total 13 TeV data up to 60 - 80 fb-1 then the data will raise my level of confidence in the 3 states from Indication to Evidence.

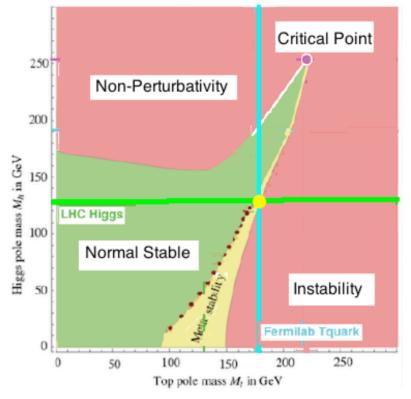
Our Universe: Is it Stable ? Consensus = NO (only metastable) Individual = YES

The Consensus view is simple and clear:

The Higgs and the Tquark are both Standard Model point particles, each with only one Mass State:

Higgs = 125 GeV Observed by LHC in 2012 Tquark = 174 GeV for which Fermilab saw Evidence in 1994

If you use the Standard Model to plot their phase space on a diagram of Higgs mass v. Tquark mass, Consensus gets



so Consensus says that Our Universe is NOT Stable but is rather at the boundary of Metastability and Instability.

The Individual view is more complicated, but more Optimistic.

In it, the Higgs is a Tquark Condensate and

the Higgs and Tquark form a 3-Mass-State System according to Nambu-Jona-Lasinio type structures described in the papers hep-ph/9603293 and hep-ph/0311165 by Yamawaki, Hashimoto, and Tanabashi producing 3 Higgs-Tquark Mass States:

> at the Non-Perturbativity Bounday; and in the Normal Stable Zone. Critical Point 250 Non-Perturbativity 200 Higgs pole mass M_h in GeV 00 00 051 Normal Stable Instability 0 250 200 0 50 100 150 Top pole mass Mt in GeV

at the Critical Point;

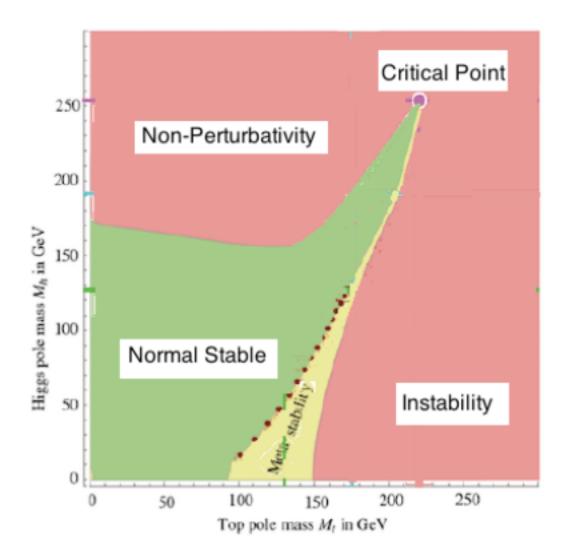
Only at the Critical Point (where the Higgs Mass is at the Higgs VEV) is the zone of Vacuum Instability or Metastability encountered.

Therefore, the Individual view is YES - Our Universe is Stable.

How and Why did the Consensus reject the Optimistic View of the Individual ?

Here are some details:

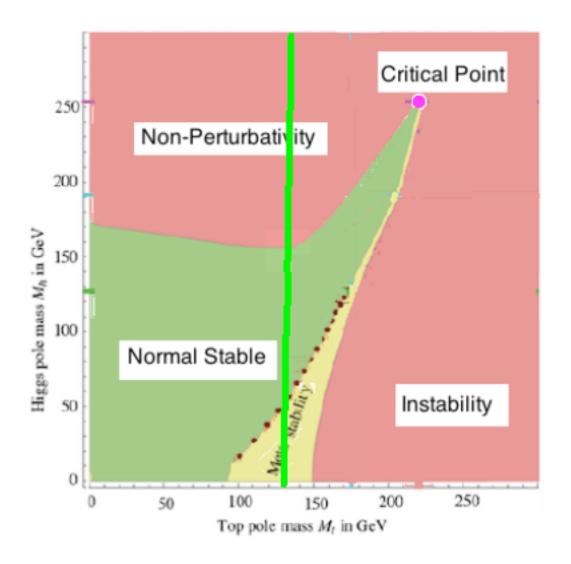
You can plot characteristics of a Nambu-Jona-Lasinio type Higgs-Tquark system on a Higgs Mass - Tquark Mass diagram like this:



From First Principles it is clear that there should be a Higgs-Tquark Mass State at the Critical Point:

Critical Point State: Higgs Mass about 260 GeV (around the Higgs VEV) -- Tquark Mass about 220 GeV

From its geometry, my physics model - see viXra 1602.0319 - predicted in the 1980s a Tquark Mass State about 130 GeV, indicated by the Green Line:



The 130 GeV calculation can be seen in terms of

Particles as Schwinger Sources, finite small regions defined by Julian Schwinger, whose geometry determines Green's Functions from Bergman Kernels of Complex Domains having symmetry of the gauge groups of Particle charges. Armand Wyler developed this technique in the context of electromagnetic force strength (fine structure constant) and particle masses (proton / electron mass ratio). Hua Luogeng calculated the relative volumes of Schwinger Source structures needed to apply Wyler's techniques to the Weak, Color, and Gravity forces. On 22 May 1992 the paper

"ANALYSIS OF TOP-ANTITOP PRODUCTION AND DILEPTON DECAY EVENTS AND THE TOP QUARK MASS"

by R. H. Dalitz and Gary R. Goldstein was received by Physics Letters B (Phys. Lett. B 287 (1992) 225-230).

It stated that: "A simple idealized procedure is proposed for the analysis of individual top-antitop quark pair production

and dilepton decay events, in terms of the top quark mass.

This procedure is illustrated by its application to the CDF candidate event.

If this event really represents top-antitop production and decay,

then the top quark mass would be 131 +22 -11 GeV.".

When I saw that paper I was very happy

because it supported my theoretical prediction of a 130 GeV Tquark Mass State

However, for political reasons - NOT based on physics reasoning -

the Fermilab Consensus hated the Dalitz-Goldstein paper and its result so

instead of what I had hoped for,

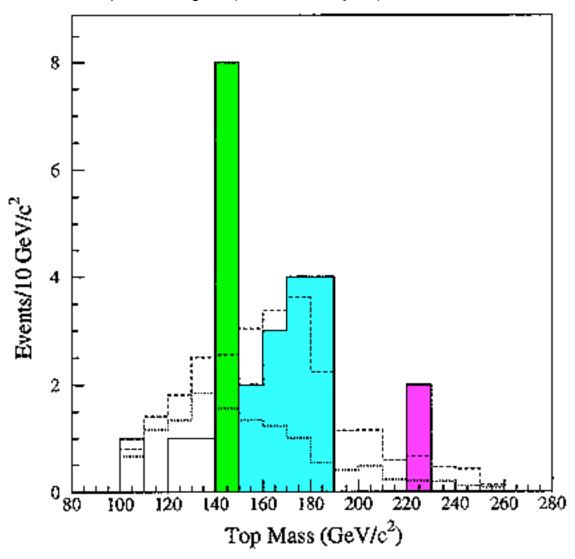
intelligent discussion of my model and its successful prediction,

the paper's authors (and I who was supporting their work)

were on the receiving end of hateful vitriol from the Fermiab Consensus.

Example of hateful vitriol - Goldstein was at Tufts, and the Fermilab Consensus told Tufts that if Goldstein continued to publicize his Tquark mass calculation work then all faculty and students at Tufts would be banned from working at Fermilab.

On 26 April 1994 Fermilab released FERMILAB-PUB-94/097-E by The CDF Collaboration "Evidence for Top Quark Production inpp Collisions at 4s = 1.8 TeV" with this semileptonic histogram (colors added by me)



Fermilab ignored the magenta small peak corresponding to the Critical Point State, without comment,

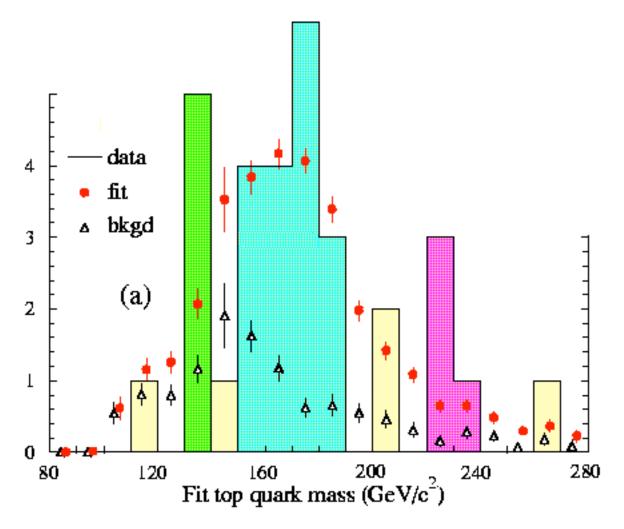
and also ignored the green large peak corresponding to my prediction and the Dalitz-Goldstein paper, saying

"... We assume the mass combinations in the 140 to 150 GeV/c^2 bin represent a statistical fluctuation since their width is narrower than expected for a top signal. ...".

I think that the Fermilab Consensus ignored the large green peak because it is roughly coincident with 130 GeV of Dalitz, Goldstein, and me that the Consensus hates.

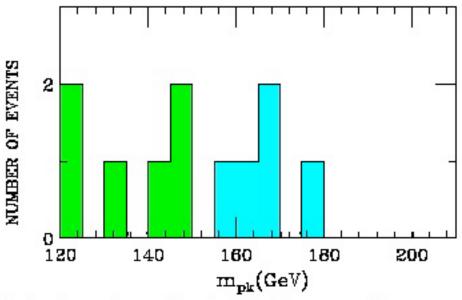
Fermilab, from that time on, insisted that the one and only Tquark Mass State was the broad cyan peak around 174 GeV

and continued to do so even when Fermilab's other detector, D0, in 1997 (hep-ex/9703008) also saw semileptonic histogram peaks around the Critical Point Mass State (magenta) and the predicted Dalitz-Goldstein Mass State (green)



Fermilab continued to insist that the one and only Tquark Mass State was the broad cyan peak around 174 GeV despite the fact that their published data could be analyzed to be consistent with all three Nambu-Jona-Lasinio Mass States. If you would like to see a lot of details about such alternative analyses, see my web pages www.valdostamuseum.com/hamsmith/ and www.tony5m17h.net

Here, on the following 2 pages, are a few of those details:

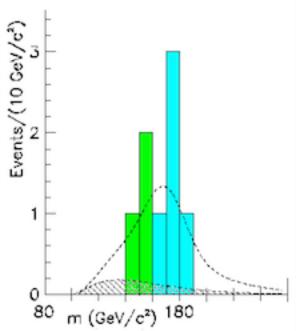


In February 1998 a dilepton histogram of 11 events from CDF (hep-ex/9802017)

The distribution of m_{pk} values determined from 11 CDF dilepton events available empirically.

shows both the low (green) state and the middle (cyan) T-quark state but

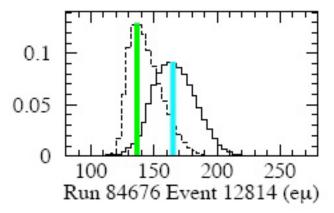
in October 1998 CDF revised their analysis by using only 8 Dilepton CDF events (hep-ex/9810029)



CDF kept the 8 highest-mass dilepton events, and threw away the 3 lowest-mass dilepton events that were indicated to be in the 120-135 GeV range, and shifted the

mass scale upward by about 10 GeV, indicating to me that Fermilab was attempting to discredit the low-mass T-quark state by use of cuts etc on its T-quark data.

In his 1997 Ph.D. thesis Erich Ward Varnes (Varnes-fermilab-thesis-1997-28 at page 159) said: "... distributions for the dilepton candidates. For events with more than two jets, the dashed curves show the results of considering only the two highest ET jets in the reconstruction ...

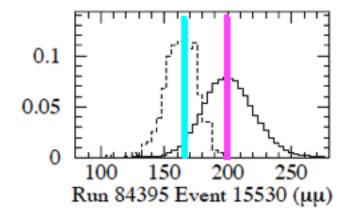


..." (colored bars added by me)

The event for all 3 jets (solid curve) seems to me to correspond to decay of a middle (cyan) T-quark state with one of the 3 jets corresponding to

decay from the Triviality boundary to the Normal Stable Region (green) T-quark state, whose immediately subsequent decay corresponds to the 2-jet (dashed curve) event at the low (green) energy level.

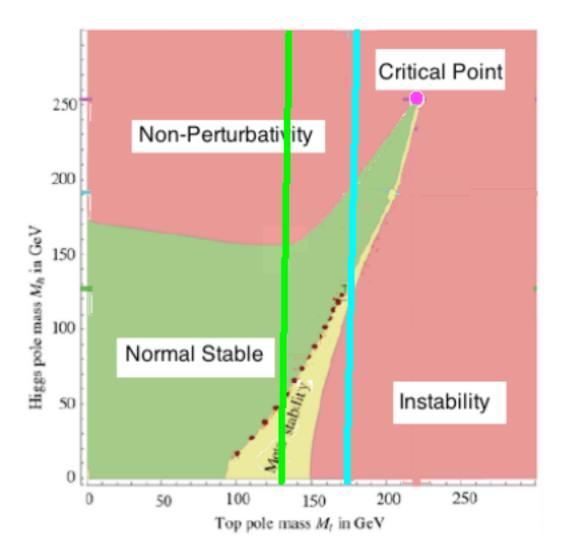
In the Varnes thesis there is one dilepton event with 3 jets (solid curve)



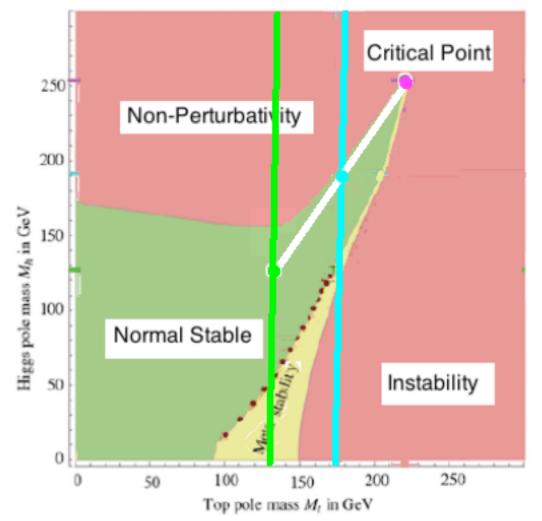
that seems to me to correspond to decay of a high (magenta) T-quark state with one of the 3 jets corresponding to

decay from the Critical Point down to the Triviality Boundary (cyan) T-quark state, whose immediately subsequent decay corresponds to the 2-jet (dashed curve) event.

No matter whatever the reality of the green low mass or magenta high mass peaks, it is clear that Fermilab was observing the broad cyan middle mass Nambu-Jona-Lasinio Tquark Mass Peak so as of the mid-1990s our diagram should be



Now, start at the Critical Point and run down (white line) the Boundary of Normal Stable - Non-Perturbativity until you hit the cyan Fermilab Middle Mass Statee and then continue down a straight line (white line) to the green Tquark Ground State

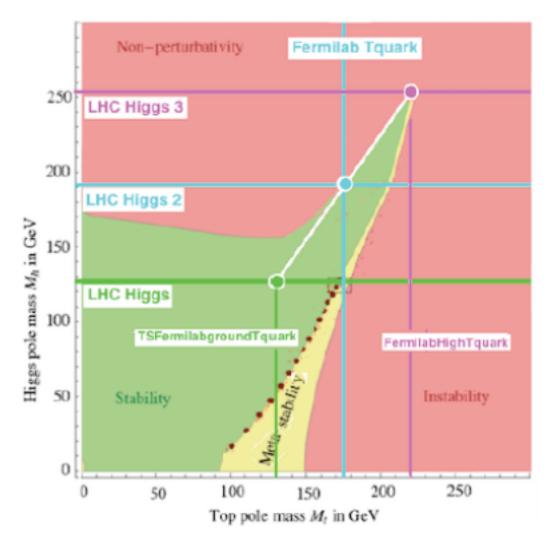


At this point, mid-1990s, assuming a Nambu-Jona-Lasinio-type Higgs-Tquark System, Fermilab had seen the Tquark Masses of the three Higgs-Tquark Mass States but the Higgs Masses were only NJL predictions not yet seen by LHC.

Critical Point High Mass States: Higgs about 260 GeV and Tquark about 220 GeV Experiments in this region should tell us about the Critical Intersection of Normal Stability, Non-Perturbativity of Compositeness and 8-dim Kaluza-Klein M4 x CP2 Structure, and Vacuum Instability.

Non-Perturbativity Boundary Middle Mass States: Higgs about 200 GeV and Tquark about 174 GeV Experiments in this region should tell us a lot about Non-Perturbativity of Compositeness and 8-dim Kaluza-Klein M4 x CP2 Structure.

Normal Stable Low Mass Ground States: Higgs about 125 GeV and Tquark about 130 GeV.



It was only in the time from mid-1990s to early 2000s that I began to understand the Nambu-Jona-Lasinio-type 3-Mass-State Higgs-Tquark System, based on reading the papers hep-ph/9603293 and hep-ph/0311165 by Yamawaki, Hashimoto, and Tanabashi,

but

just when I was beginning to really understand the NJL-type Higgs-Tquark System I was blacklisted by the Cornell arXiv (2002)

I had tried to fight the blacklisting by suing Cornell (Case No.:4:02-CV-280 fin my home Northern District of Georgia) which suit was dismissed 24 March 2003 only on Jurisdictional grounds (not a dismissal of the merits of my case) the Court saying that I should sue Cornell in its home state of New York. My efforts to hire a good New York law firm were unsuccessful because, as I was told, no matter whether I paid a good fee, I would be only an Individual one-time client, and Cornell was a multi-billion dollar enterprise involving a large number of people (some of my cousins are alumnae) with whom a good relationship was of continuing usefulness for New York lawyers. Therefore I gave up the law suit approach. Further,

the CERN CDS EXT service which had allowed me to put up papers terminated outside access (and therefore terminated my access) pursuant to an 8 October 2004 meeting of the CERN Scientific Information Policy Board (SIPB) so

my ability to communicate my ideas to the physics community was severely curtailed, being restricted to my personal web sites, and the alternative archive viXra,

and making talks at meetings,

including contributing a talk at the 2005 APS April Meeting in Tampa.

The chairman of the session at which I presented my Nambu-Jona-Lasinio-type 3-Mass-State Higgs-Tquark System was Joseph Lykken of Fermilab. At the meeting he seemed interested, and said he would discuss it with the people at Fermilab and let me know if I could maybe go there and make a talk etc.

I did not hear from him immediately,

so I sent him an email and he replied (20 April 2005) saying:

"... Thanks, I will let you know if I get any postive response from the CDF and D0 experiments. Regards, -Joe ...".

There was no further contact with him after that,

which

showed me that even if a smart individual like Joe Lykken at a place like Fermilab were to be interested in my ideas, the Consensus Powers would make certain that I and my ideas would not be allowed.

Therefore about all I could do was to wait for the LHC to start taking data that might indicate Higgs Mass States predicted by my NJL model.

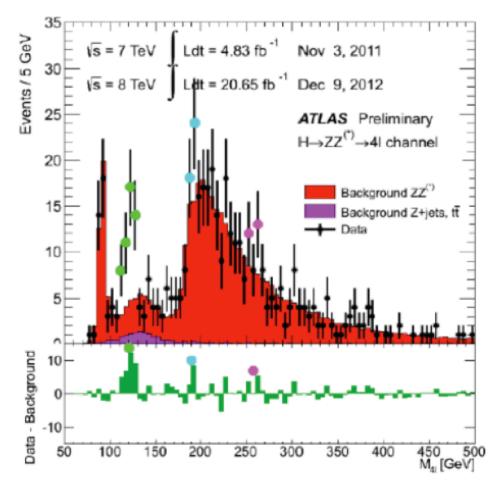
The cleanest and most reliable channel in the LHC experiment is Higgs -> ZZ* -> 4I which would show a Higgs Mass State as a clean peak but it has fewer events than other channels so

the most likely early discovery of a Higgs State would be in the digamma channel which would show a Higgs Mass State as a shallow bump on a broad background curve that might be hard to distinguish from a statistical fluctuation.

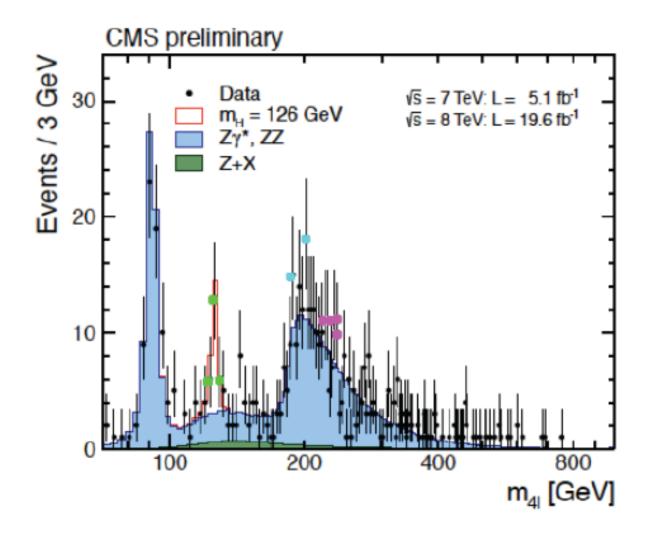
In 2008 the LHC started up to run at 14 TeV, but defective electrical connections caused an explosion that terminated operation.

In 2010-2011, after repairs and rethinking, the LHC began to run at 7 TeV with ATLAS and CMS indicating possible Higgs Mass State around 115-130 GeV.

In 2012, running at 8 TeV, ATLAS and CMS Observed in the digamma channel the 125 GeV Low Mass HIggs Ground State. As to the other two Higgs Mass States, ATLAS saw Indications of Higgs Mass States around 200 and 260 GeV, as well as at 125 GeV, in the Higgs -> ZZ* -> 4I channel



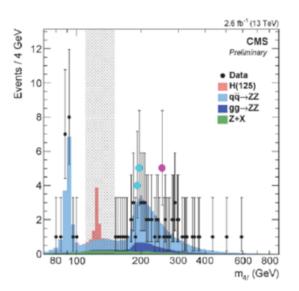
CMS also saw indications of the same two Higgs Mass States with cross sections around 25% of Standard Model expectations:



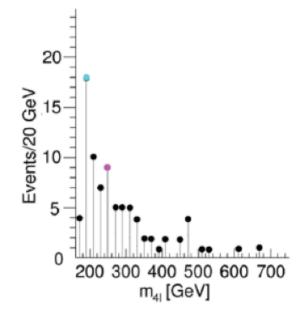
The LHC shut down in 2013-2014 for repair and reconstruction needed for operation at 13 TeV.

In 2015 the LHC had a 13 TeV run producing 2.6 fb-1 for CMS and 3.2 fb-1 for ATLAS both of which saw iindications of Higgs Mass States around 200 and 260 GeV

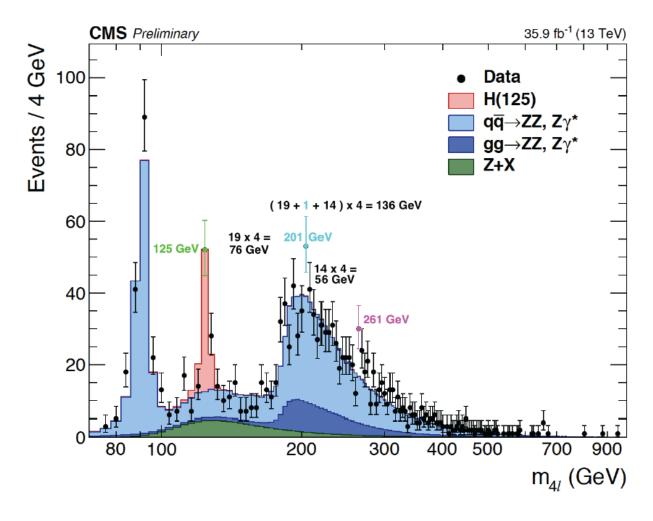
CMS saw



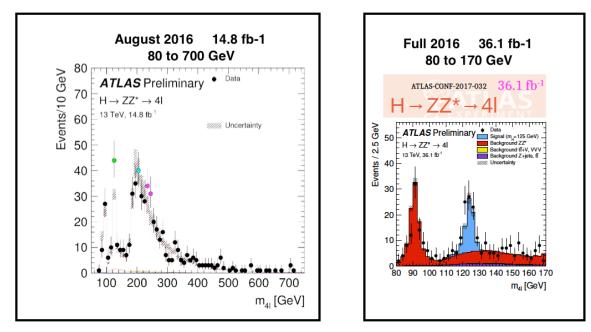
ATLAS saw



In 2016 the LHC had a 13 TeV run producing 35.9 fb-1 for CMS and 36.1 fb-1 for ATLAS CMS saw for the Higgs -> ZZ^* -> 4I channel:



ATLAS saw for the Higgs $-> ZZ^* -> 4I$ channel:



In August 2016,

based on the first 14.8 fb-1 of 2016 data in the Higgs -> ZZ* -> 4I channel, ATLAS saw Indications of Higgs Mass states in the area of 200 GeV and 260 GeV and Observation of Higgs Mass state at 125 GeV.

For the Full 2016 36.1 fb-1 of data in the Higgs -> ZZ* -> 4I channel, ATLAS did not report results at Moriond 2017,

and at Shanghai LHCP2017 only reported results for the 80 to 170 GeV range, thus ignoring the possible Higgs Mass states in the area of 200 GeV and 260 GeV while emphasing Observation of the Higgs Mass state at 125 GeV.

If in future data analysis and reporting,

the LHC follows the trend of ATLAS, ignoring any Higgs at 200 and 260 GeV, and concentrating only on the Observed 125 GeV Higgs Mass state that is favored by the Consensus,

then the Individual's Nambu-Jona-Lasinio 3-State HIggs-Tquark System will have been Effectively Suppressed

and the Simple Consensus View of a single Higgs state at 125 GeV will have prevailed,

just as the Fermilab Consensus, by ignoring any Tquark data at 130 and 220 GeV, has seen its Simple Consensus View of a single Tquark state at 174 GeV become Accepted Dogma.

In 2016-2017 I wanted to present my Nambu-Jona-Lasinio 3-Mass-State ideas for a Higgs-Tquark system in the context of watching LHC results as the amount of data increased, being 30-40 fb-1 for 2016 and expected to be a similar amount for 2017 because I hope that the Higgs -> ZZ* -> 4I channel results with 60-80 fb-1 may be enough to show clearly evidence or observation of the 200 GeV Higgs Mass State on the Non-Perturbativity Boundary and

the 260 GeV Higgs Mass State at the Critical Point (Higgs VEV)

so I applied to visit

the 2017 Rencontres de Moriond (results of the LHC 2016 run) and the Princeton Institute for Advanced Study and

the Simons Center for Geometry and Physics.

The Moriond organizer was very courteous, but declined my offer to talk about my ideas.

The Princeton IAS rejected my application, stating that I was unqualified because I have no Ph.D., despite the facts that: Freeman Dyson was a Professor at IAS (1953-1994, then becoming emeritus) Freeman Dyson has no Ph.D., but has a 1945 Trinity College Cambridge B.A. in mathematics. I have a 1963 Princeton A.B. in mathematics.

The Simons Center rejected my application, not stating any particular reason.

A personal reason that I would have liked to visit the Simons Center

is that it is near the Setauket Presbyterian Church, of which

my 8-Great Grandfather Nathaniel Brewster was the First Minister (1665-1690).

Nathaniel Brewster (AB Harvard 1642) was one of the nine graduates of Harvard's first class.

His father, my 9-Great Grandfather Francis Brewster II (MA Pembroke Cambridge 1624), died at sea in 1647 aboard the New Haven Phantom Ship.

If the Influential Physics Establishment Institutions

such as CERN-LHC-Moriond, Princeton IAS, and Simons Geometry and Physics **continue to exclude Individuals with ideas** such as Nambu-Jona-Lasinio Systems then

Physics will enter a Dark Age with only incremental advancements

and

No Major Advancement in Fundamental Understanding.

Dark Energy and Dark Matter Consensus = Unknown Individual = Known Segal Conformal Structure

Again, the Consensus view is simple and clear:

Nobody understands Dark Energy and Dark Matter.

Also again, the Individual view is more complicated, but more Optimistic.

In 2003 the Wilkinson Microwave Anisotropy Probe (WMAP) released its first results (astro-ph/0302207) showing a Dark Energy : Dark Matter : Ordinary Matter ratio **DE : DM : OM = 0.73 : 0.22 : 0.044**

Irving Ezra Segal based his ideas about Gravity and the Cosmological Constant on the Conformal group Spin(2,4) = SU(2,2) whose 15 generators act as gauge bosons which combine to produce Einstein-Hilbert Gravity plus Cosmological Constant -- see section 14.6 of Rabindra Mohapatra's book "Unification and Supersymmetry".

The 15 Conformal Generators are:

6 Lorentz plus 4 Special Conformal = 10 for the Expanding Universe of Dark Energy 4 Translations for 4-dim spacetime of Primordial Black Holes and Dark Matter 1 Dilatation for the Higgs scalar giving Mass to Ordinary Matter

At first glance, that gives the ratio DE : DM : OM = 10/15 : 4/15 : 1/15 = 0.67 : 0.27 : 0.06

but DE, DM, and OM vary differently with the time-varying radius of Our Universe. When you take into account the differing variations with age of Our Universe, you get for the ratio at our present time:

DE : DM : OM = 0.753 : 0.202 : 0.045 in very good agreement with the WMAP results.

I then wrote a paper that, even though I had been blacklisted by the Cornell arXiv in 2002, I hoped would be good enough and important enough that Cornell would lift its blacklist. However, when I submitted my WMAP ratio calculation paper to the Cornell arXiv, I found that my blacklisting would not be lifted, and it was rejected by Cornell in February 2004.

I then submitted the paper to the CERN CDS document server which allowed me to post it as EXT-2004-013.

My success was short-lived, because pursuant to an 8 October 2004 meeting of the CERN Scientific Information Policy Board (SIPB) the CERN CDS External Service was terminated. My personal opinion is that my name was involved in the October 2004 discussions leading to the killing of the CERN CDS preprint server. My only sources are rumors, because nobody officially involved will talk to me directly. The rumor sources are people connected with CERN who would talk to me or to friends of mine but were (and probably still are) afraid of their jobs if they were to be identified.

If the Consensus continues to Suppress the distribution of Individual ideas such as Conformal Gravity, Dark Energy, and Dark Matter then

it is very unlikely that Understanding of Gravity, Dark Energy, and Dark Matter will advance beyond the Consensus View, which is that

Dark Energy and Dark Matter are Mysteries that Nobody Understands.

The following 5 pages are my WMAP ratio calculation paper EXT-2004-013 that was put on CERN CDS before termination of External service in October 2004.

Cosmology, Gravity, and the WMAP ratio 0.73 : 0.23 : 0.04

Frank D. (Tony) Smith, Jr., Cartersville, Georgia USA

[Note - shortly after arXiv removed this paper, in response to some comments mde by others, I added the material set off by [].]

Abstract

WMAP results indicate that our universe is now made up of 73% dark energy (DE), 23% dark matter (DM), and 4% ordinary matter (OM), the DE possibly being in the form of a cosmological constant (itself a misnomer, as a "cosmological constant" can be variable). A model of gravity based on the conformal group Spin(2,4) = SU(2,2), motivated by work of I. E. Segal, can be used to estimate the present-day DE : DM : OM ratio. If DM obeys the ordinary matter equation of state, then the model gives the ratio 0.753 : 0.202 : 0.045, which is quite close to the WMAP observation of 0.73 : 0.23 : 0.04.

<u>WMAP</u> results indicate that our universe is now made up of 73% dark energy (DE), 23% dark matter (DM), and 4% ordinary matter (OM), the DE possibly being in the form of a cosmological constant (itself a misnomer, as a "cosmological constant" can be variable).

In the <u>D4-D5-E6-E7-E8 VoDou Physics model</u>, <u>Gravity and the Cosmological Constant come from the</u> <u>MacDowell-Mansouri Mechanism</u> and the 15-dimensional Spin(2,4) = SU(2,2) <u>Conformal</u> Group, which is the group used by <u>Irving Ezra Segal</u> in his work on gravity and cosmology.

The 15 generators of the Conformal Group SU(2,2) = Spin(2,4) correspond to:

- 3 Rotations;
- 3 Boosts;
- 4 Translations;
- 4 Special Conformal transformations; and
- 1 Dilatation.

The main purpose of this paper is to use the structure of the Conformal group to estimate the present-day ratio

file:///iCube/Users/tsmith/Documents/Graviphoton%202004/coscongraviton.html (1 of 5) [14/2/2004 11:52:13 AM]

DE : DM : OM

which, according to WMAP results, is

.73:.23:.04

The basis of the estimation is the following correspondence:

- DE (dark energy, cosmological constant) the 10 Rotations, Boosts, and Special Conformal generators
- DM (dark matter) the 4 Translations
- OM (ordinary matter) the 1 Dilatation

[Here is some motivation for the above <u>correspondence</u>:

- DE is the NORMAL state of stuff in our universe (it is now, according to WMAP, about 73% of it). It looks more like deSitter spacetime than Minkowski spacetime. In Segal's model and as Aldrovandi and Peireira show in some mathematical detail in their paper at <u>gr-qc/9809061</u> the DE spacetime structure comes from "... the group Q, formed by a semi-direct product between Lorentz and special conformal transformation groups ...". Those are the 10 Rotations, Boosts and Special Conformal generators that correspond to DE.
- DM is a lesser part (it is now, according to WMAP, about 23% of it) of our universe, and differs from the dominant DE by being based on the 4 Translations that are the basis for Einstein's description of spacetime curvature, which in turn describes effective mass (such as the mass of such DM candidates as primordial black holes). Those 4 Translations therefore correspond to DM.
- OM (the stuff of which we and Earth are made) is sort of weird and exceptional (it is now, according to WMAP, only about 4% of it). For us to call it ordinary is quite provincial, because it is only ordinary in the context of our physical bodies and the planet on which we live. What characterizes all OM is that its mass comes from the Higgs mechanism. The Dilatation gives the spin 0 Higgs field, and therefore all the mass of OM, so the 1 Dilatation therefore corresponds to OM.

In terms of I. E. Segal's book Mathematical Cosmology and Extragalactic Astronomy (Academic Press 1976), you might say that DE and DM are respectively related to Unispace and Minkowski space, and that OM is something like a little frothy foam on/in the DE/DM system.]

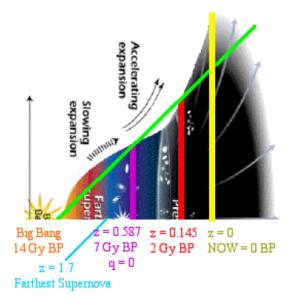
As a first-order calculation, the correspondence gives the ratio

DE : DM : OM = 10/15 : 4/15 : 1/15 = .67 : .27 : .06

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Segal Conformal Physics and GraviPhotons

However, the various components of DE, DM, and OM vary differently with time (or, equivalently, with the radius of our expanding universe), so the ratio 0.67 : 0.27 : 0.06 is valid only for a particular time, or scale factor, of our Universe, so it is necessary to ask at what stage of the expansion of the universe should the first-order ratio 0.67 : 0.27 : 0.06 be valid. In order to answer that question, we should try to see what are the Special Times in the History of our Universe ?



There seem to be four Special Times in the history of our Universe:

- the **Big Bang Beginning of Inflation** (about 13.7 Gy BP);
- the End of Inflation = Beginning of Decelerating Expansion (beginning of green line also about 13.7 Gy BP);
- the End of Deceleration (q=0) = Inflection Point = Beginning of Accelerating Expansion (purple vertical line at about z = 0.587 and about 7 Gy BP). According to a hubble site web page credited to Ann Feild, the above diagram "... reveals changes in the rate of expansion since the universe's birth 15 billion years ago. ... The curve changes noticeably about 7.5 billion years ago, when objects in the universe began flying apart as a faster rate. ...". According to a CERN Courier web page: "... Saul Perlmutter, who is head of the Supernova Cosmology Project ... and his team have studied altogether some 80 high red-shift type Ia supernovae. Their results imply that the universe was decelerating for the first half of its existence, and then began accelerating approximately 7 billion years ago. ...". According to astro-ph/0106051 by Michael S. Turner and Adam G. Riess: "... current supernova data ... favor deceleration at z > 0.5 ... SN 1997ff at z = 1.7 provides direct evidence for an early phase of slowing expansion if the dark energy is a cosmological constant ...".
- the Last Intersection of the Accelerating Expansion of our Universe with Linear Expansion

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(green line) from End of Inflation (first interesection) through Inflection Point (second intersection, at purple vertical line at about z = 0.587 and about 7 Gy BP) to the Third Intersection (at red vertical line at z = 0.145 and about 2 Gy BP), which is also around the times of <u>the</u> beginning of the Proterozoic Era and Eukaryotic Life, Fe2O3 Hematite ferric iron Red Bed formations, a Snowball Earth, and the start of the Oklo fission reactor.

After the Last Intersection at the end of the Early Part of the Accelerating Expansion of our Universe, expansion of our Universe continues to accelerate with the Late Part of its Accelerating Expansion.

Those four Special Times define four Special Epochs:

- The Inflation Epoch, beginning with the Big Bang and ending with the End of Inflation. The Inflation Epoch is described by Zizzi Quantum Inflation, ending with Self-Decoherence of our Universe.
- The **Decelerating Expansion Epoch**, beginning with the End of Inflation. During the Decelerating Expansion Epoch, the Radiation Era is succeeded by the Matter Era, and the Matter Components (Dark and Ordinary) remain more prominent than they would be under the "standard norm" conditions of Linear Expansion.
- The Early Accelerating Expansion Epoch, beginning with the End of Deceleration and ending with the Last Intersection of Accelerating Expansion with Linear Expansion. During Accelerating Expansion, the prominence of Matter Components (Dark and Ordinary) declines, reaching the "standard norm" condition of Linear Expansion at the end of the Early Accelerating Expansion Epoch at the Last Intersection with the Line of Linear Expansion.
- The Late Accelerating Expansion Epoch, beginning with the Last Intersection and continuing into the far future. During the Late Accelerating Expansion Epoch, DE dark energy is more prominent than it would be under the "standard norm" conditions of Linear Expansion.

In making my estimation of the ratio DE : DM : OM, the time of the first approximation ratio 0.67 : 0.27 : 0.06 is taken to be the time of the Last Intersection, which is about 2 billion years ago.

To see how the ratio DE : DM : OM evolved during the 2 billion years from the Last Intersection to the present time, you must know the value of w in equation of state

density =proportional= 1 / R^3(1+w)

for DE, DM, and OM in our universe at a time when its scale factor is R.

- For DE (dark energy cosmological constant), w = -1
- For DM(dark matter) that obeys the ordinary matter equation of state, w = 0
- For OM, w = 0

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Segal Conformal Physics and GraviPhotons

About 2 billion years ago, the redshift z = 0.145, or 1+z = 1.145, or $(1+z)^{\wedge}3 = 1.5$,

so that from then to now:

- DM density would decline by the $1 / R^3$ factor as Ordinary Matter, from .27 to .27 / 1.5 = .18.
- OM density would decline by the $1/R^3$ factor as Ordinary Matter, from .06 to .06 / 1.5 = .04
- DE density would remain constant at .67.

Therefore, the ratio as of now would be

DE : DM : OM = .67 : .18 : .04 = .753 : 202 : 0.45

or

75.3% : 20.2% : 4.5%

which is quite close to the WMAP observation of

73% : 23% : 4%.

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From E8 Root Vector Geometry to the LHC

Frank Dodd (Tony) Smith, Jr. - 2017 - viXra 1701.0496

Abstract

This paper is intended to be a only rough semi-popular overview of how the 240 Root Vectors of E8 can be used to construct a useful Lagrangian describing Gravity and Dark Energy plus the Standard Model. For details and references, see viXra/1602.0319.

The 240 Root Vectors of E8 represent the physical forces, particles, and spacetime that make up the construction of a realistic Lagrangian describing the Octonionic Inflation Era followed by a Quaternionic M4 x CP2 Kaluza-Klein Era in which the HIggs emerges by the Mayer mechanism and 2nd and 3rd Generation Fermions appear. By generalizations of the Nambu-Jona-Lasinio models, the Higgs is seen to be a Truth Quark-AntiQuark Condensate giving 3 Mass States of the Higgs and 3 Mass States of the Truth Quark. My analysis of Fermilab and LHC observation data indicates that Fermilab has observed the 3 Truth Quark Mass States and LHC has observed the 3 Higgs Mass States. The Lagrangian, which is fundamentally classical, is constructed from E8 only and E8 lives in $Cl(16) = Cl(8) \times Cl(8)$ which corresponds to two copies of an E8 Lattice.

A seperate paper discusses using a third copy of an E8 Lattice in connection with construction of a realistic Algebraic Quantum Field Theory related to the Leech Lattice.

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Higgs - Truth Quark-AntiQuark System give 3 Mass States of each ... page 16

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Consensus 1-state Higgs and Tquark give Metastable Universe but E8 3-state Higgs and Tquark gives Stable Universe at Low Energy and 8-dim Kaluza-Klein Compositeness at Medium Energy and Full Electroweak Symmetry at High Energy ... page 19 The **240 root vectors of E8** are of equal length in 8 dimensions as they form the 240-vertex Witting-Gossett polytope so you can in 8 dimensions visualize how they group together If you look at the 240 vertices as points on an 8-dim sphere then you can pick one point as the North Pole

and

see where the other points fall at their angle of latitude:

1 is at North Pole

56 nearest neighbors of the North Pole are at North Temperate Latitude

126 2nd nearest neighbors of the North Pole are at the Equator

56 3rd nearest neighbors of the North Pole are at South Temperate Latitude

1 4th nearest neighbor of the North Pole is Anitpodal at the South Pole

Therefore you see that the 240 break down into 1 + 56 + 126 + 56 + 1 but what you need to see next is which root vector corresponds to which physics thing.

Geometry of the E8 Lie Group gives you some ideas:

56 + 56 = 112 Temperate North and South is the D8 = Spin(16) subgroup of E8 and they correspond to Gravity + Dark Energy and the Standard Model gauge groups and to 8-dimensional Spacetime position and momentum.

Each 56 breaks down into 24 + 32.

North Temperate 24 = D4 Lie Algebra = Spin(2,6) which contains Conformal Spin(2,4) which gives Gravity plus Conformal Dark Energy as well as Ghosts of Standard Model Gauge Bosons

South Temperate 24 = D4 Lie Algebra = Spin(8) which contains SU(4) which gives SU(3) of the Color Force which is the Global Group of Kaluza-Klein Internal Symmetry Space CP2 and CP2 = SU(3) / SU(2) x U(1) contains groups of Weak and Electromagnetic Forces as well as Ghosts of Gravity and Dark Energy

Symmetric space D8 / D4(gravity) x D4(standard model) is 112-28-28 = 64-dim and it corresponds to 64 = 8-dim position x 8-dim momentum of 8-dim Spacetime which

8-dim Spacetime reduces to 4+4 dim M4 x CP2 Kaluza-Klein spacetime

Symmetric space E8 / D8 is 128-dim Rosenfeld OctoOctonionic Projective Plane which is

1 + 126 + 1 of the North Pole, Equator, and South Pole

The 128 are the 8 Spacetime components of Fermions: 8 Particles and 8 AntiParticles for 8x8 = 64 Particle components + 8x8 = 64 AntiParticle components.

1 at North Pole = time component of Neutrino

1 at South Pole = time component of AntiNeutrino

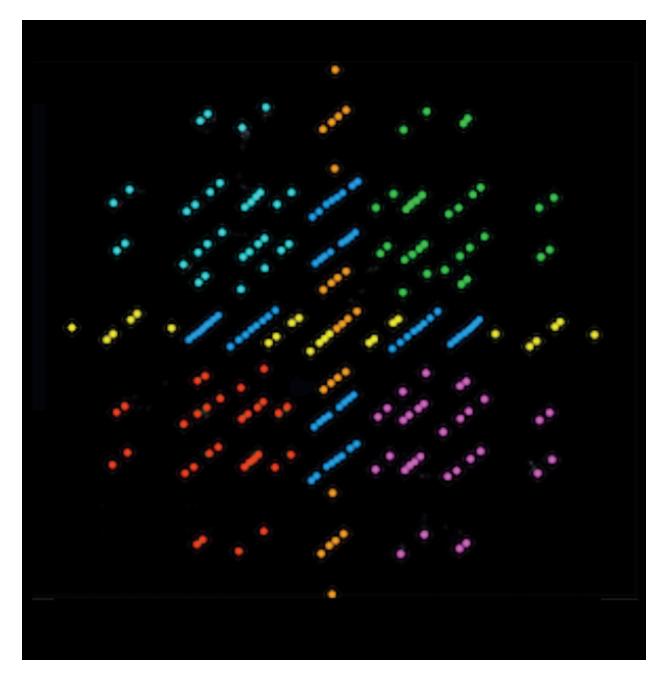
126 at Equator = other components of Leptons and Quarks = root vectors of E7

Symmetric space E7 / D6xSU(2) = 64-dim Rosenfeld QuaterOctonionic Projective Plane corresponds to 8 components of (electron + rgb up quarks) = 8x4 = 32

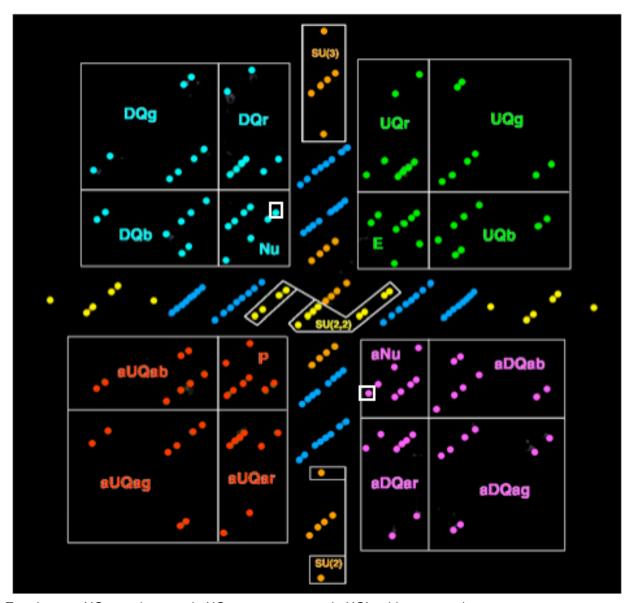
plus 8 components of (positron + rgb up antiquarks) = 8x4 = 32 D6 x SU(2) has 60+2 = 62 root vectors so if you add 1+1 North and South Poles you get 64 corresponding to 8 components of (neutrino + rgb down quarks) = 8x4 = 32 plus 8 components of (antineutrino + rgb down antiquarks) = 8x4 = 32

2-dim projection of 240 E8 Root Vectors gives useful visualization of which root vector corresponds to which physics thing

In 2-dim Projection the Root Vectors no longer have the same distance from origin



but in this particular 2-dim projection the physical interpretations of each Root Vector becomes clear:



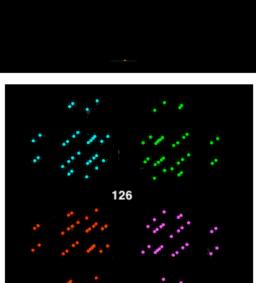
E = electron, UQr = red up quark, UQg = green up quark, UQb = blue up quark Nu = neutrino, DQr = red down quark, DQg = green down quark, DQb = blue down quark P = positron, aUQar = anti-red up antiquark, aUQag = anti-green up antiquark, aUQab = anti-blue up antiquark aNu = antineutrino, aDQar = anti-red down antiquark white boxes enclose time components of neutrino and antineutrino aDQag = anti-green down antiquark, aDQab = anti-blue down antiquark Each Lepton and Quark has 8 components with respect to 4+4 dim Kaluza-Klein 6 orange SU(3) and 2 orange SU(2) represent Standard Model root vectors 24-6-2 = 16 orange represent U(2,2) Conformal Gravity Ghosts 12 yellow SU(2,2) represent Conformal Gravity SU(2,2) root vectors 24-12 = 12 yellow represent Standard Model Ghosts 32+32 = 64 blue represent 4+4 dim Kaluza-Klein spacetime position and momentum

Here is how the 2-dim physical interpretations correspond to the 8-dim Sphere Latitude decomposition: 1 is at North Pole



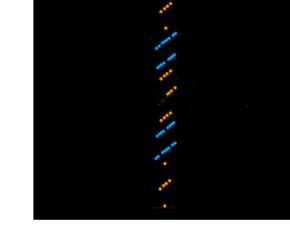
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126 2nd nearest neighbors of the North Pole are at the Equator

56 3rd nearest neighbors of the North Pole are at South Temperate Latitude



1 4th nearest neighbor of the North Pole is Anitpodal at the South Pole



Recipe for constructing Lagrangian from E8 Root Vectors

My favorite Fundamental Structure of Physics is the Lagrangian. In his Dirac Lecture, Steven Weinberg says "... Lagrangian density ... you can think of it as the density of energy. Energy is the guantity that ... tells us how the system evolves. ...".

The Lagrangian Density contains Boson terms and Fermion terms. To get the full Lagrangian, you integrate those terms over Spacetime.

The Code or Recipe just says:

put

the Gravity + Dark Energy Gauge Bosons and Standard Model Ghosts and

the Standard Model Gauge Bosons and Gravity-Dark Energy Ghosts into the Lagrangian Density Boson terms in accord with the standard way of constructing physics boson terms

and

put

the Fermion Particles and AntiParticles

into the Lagrangian Density Fermion terms in accord with the standard way of constructing physics fermion terms

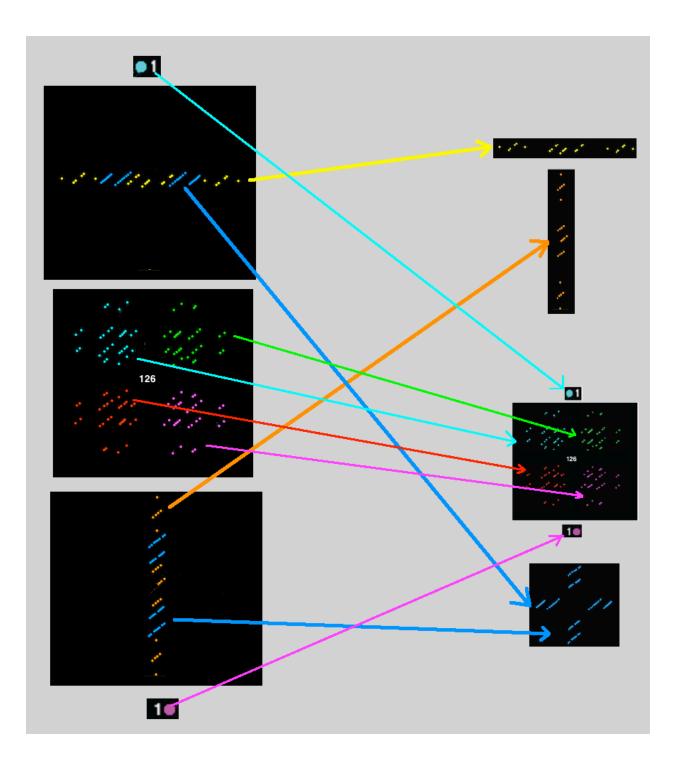
and

put the Spacetime Root Vectors into the Spacetime Base Manifold over which the Lagrangian Density is integrated.

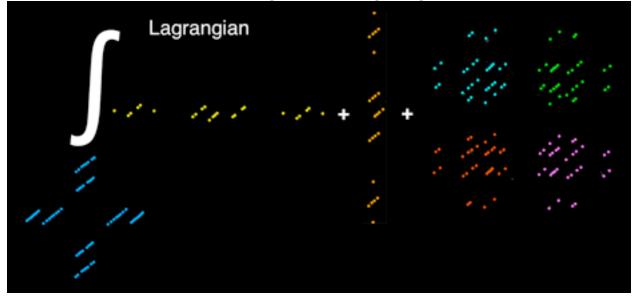
In terms of the preceding pictures of physics of E8 Root Vectors the Code or Recipe gives a Lagrangian that is a realistic physics model.

Of course, to completely carry out the Code or Recipe you need to write out the Lagrangian terms in the math language of conventional physics and that is described in some of the long papers I have written (see my web site and my viXra papers).

Here I am just trying to show the basic underlying structure of E8 Geometry so I am not writing down the extensive details in this paper.



The fundamental Lagrangian formed by this structure is an Octonionic structure over 8-dim Spacetime and is effective during the Initial Big Bang and Inflation.

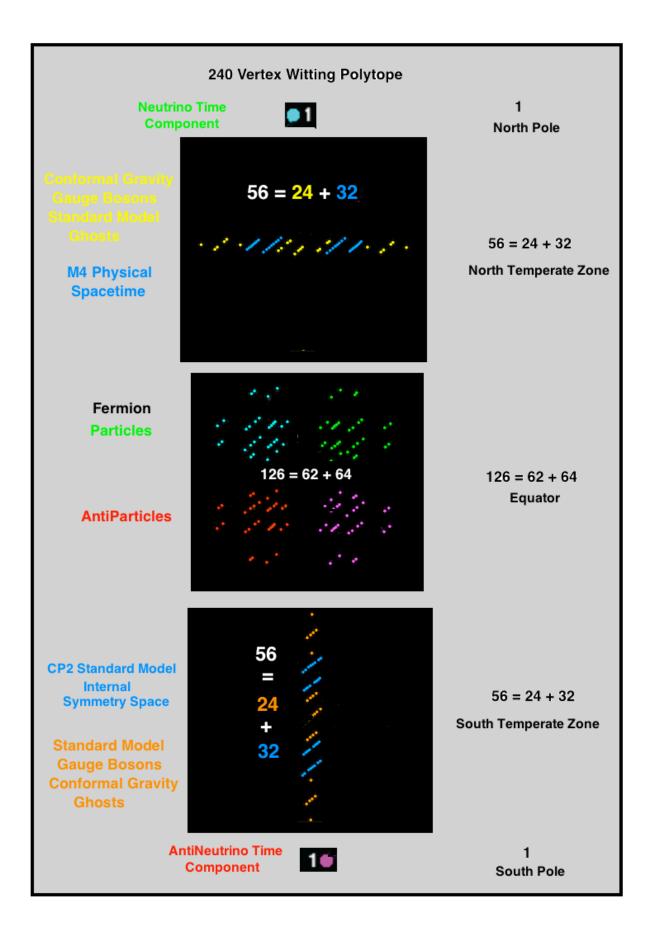


Since Octonionic Quantum Field Theory is NOT Unitary, Particle / AntiParticle Creation occurs during Inflation.

Inflation Ends when a preferred Quaternionic Subspacetime freezes out, converting 8 dim Spacetime into 4+4 dim M4 x CP2 Spacetime where M4 = Physical Minkowski Spacetime and CP2 = SU(3) / U(2) Internal Symmetry Space and the Octonionic Integral becomes two Quaternionic Integrals



Here is how the Witting 240-Polytope splits into two 600-Cells:

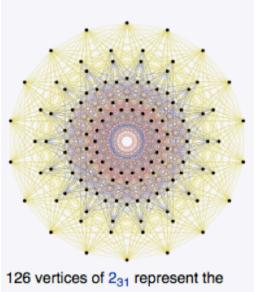


In more detail, start with the North Pole.

Then the North Pole has 56 nearest neighbors that live on a North Temperate Zone which is a fixed Latitude Angle from the North Pole and is a 6-dim sphere Latitude subset of the 7-dim sphere. The 56 are of two kinds: 32 describing half of 8-dim Spacetime for 4-dim Minkowski Physical Spacetime and 24 describing Gauge Bosons and Ghosts for Gravity and the Standard Model. The 32 Spacetime-type vertices live on the Equator of the 6-dim sphere and are distributed on that 5-dim sphere as one half of the 64 vertices of a hypercube in 6-dim space. 12 of the 24 live on a North Temperate Latitude of the 6-dim sphere

The other 12 of the 24 live on a South Temperate Latitude of the 6-dim sphere.

Then there are 126 next-nearest neighbors to the North Pole. They live on the Equator of the 7-dim sphere and are distributed on that 6-dim sphere as the Root Vectors of the E7 Lie Algebra



root vectors of E7

They correspond to 126 of the 128 components of 8+8 Fermion Particles+AntiParticles.

Then are the 56 nearest neighbors of the South Pole that of a South Temperate Zone which is a fixed Latitude Angle from the South Pole and is a 6-dim sphere Latitude subset of the 7-dim sphere. The 56 are of two kinds: 32 describing half of 8-dim Spacetime for 4-dim CP2 Standard Model Internal Symmetry Space and 24 describing Gauge Bosons and Ghosts for the Standard Model and Gravity. The 32 Spacetime-type vertices live on the Equator of the 6-dim sphere and are distributed on that 5-dim sphere as the other half of the 64 vertices of a hypercube in 6-dim space. 12 of the 24 live on a North Temperate Latitude of the 6-dim sphere The other 12 of the 24 live on a South Temperate Latitude of the 6-dim sphere.

Then there is finally the South Pole. The 240-Polytope decomposes into two 120-vertex 600-Cells

The 240-Polytope splits into two 120-vertex 600-Cells:

Sadoc and Mosseri in their book "Geometrical Frustration" (Cambridge 1999, 2006), say: "...

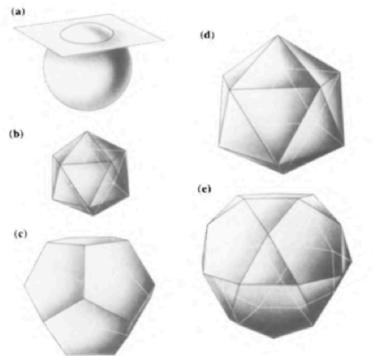


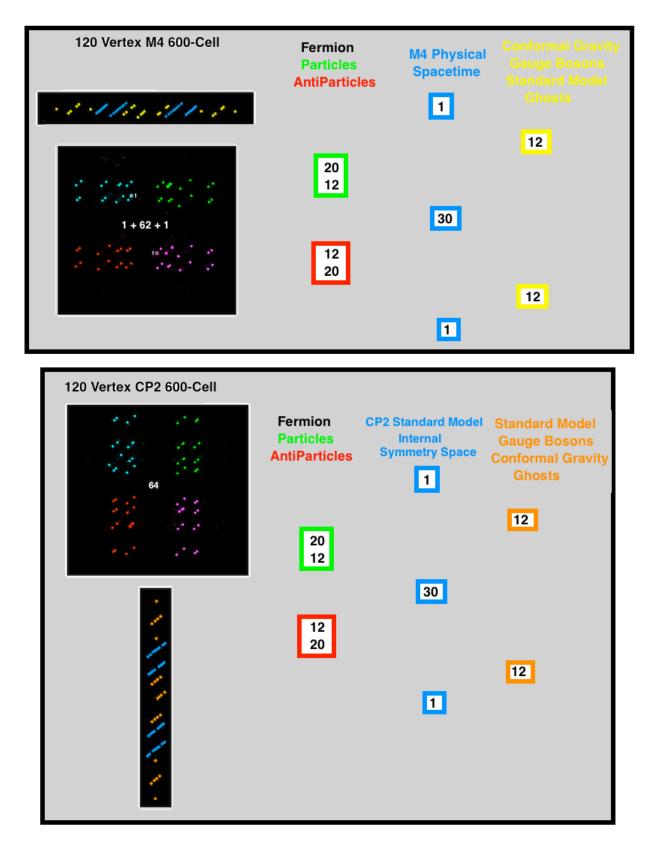
Fig. A5.1. The $\{3, 3, 5\}$ polytope. Different flat sections in S^3 (with one site on top) give the following successive shells; (a) an icosahedral shell formed by the first 12 neighbours, (b) a dodecahedral shell, (c) a second and larger icosahedral shell, (d) an icosidodecahedral shell on the equatorial sphere. Then other shells are symmetrically disposed in the second 'south' hemi-hypersphere, relative to the equatorial sphere (e).

Section	X_0	$(x_1, x_2, x_3)^{\dagger}$	Vertex number	Shape
0	2	(0, 0, 0)	1	point
1	τ	$(1, 0, \tau^{-1})$	12	icosahedron
2	1	(1, 1, 1)	20	dodecahedron
		$(\tau, \tau^{-1}, 0)$		
3	τ^{-1}	$(\tau, 0, 1)$	12	icosahedron
4	0	(2, 0, 0)	30	icosidodecahedron
		$(\tau, 1, \tau^{-1})$		
5	$-\tau^{-1}$	$(\tau, 0, 1)$	12	icosahedron
6	$^{-1}$	(1, 1, 1)	20	dodecahedron
		$(\tau, \tau^{-1}, 0)$		
7	$-\tau$	$(1, 0, \tau^{-1})$	12	icosahedron
8	$^{-2}$	(0, 0, 0)	1	point

Table A5.1. Sections of the {3, 3, 5} polytope (with an edge length equal to $2\tau^{-1}$) beginning with a vertex

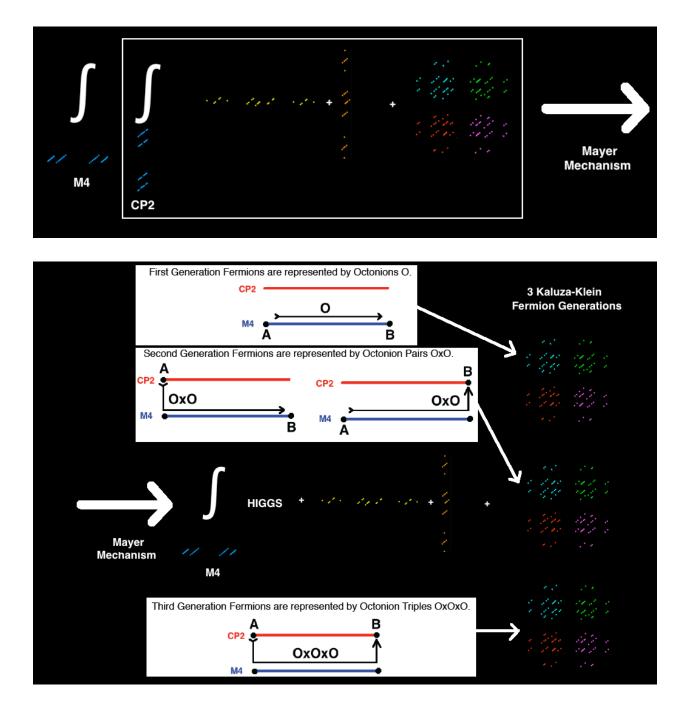
...

[†]Cyclic permutation with all possible changes of signs. $\tau = (1 + \sqrt{5})/2$.

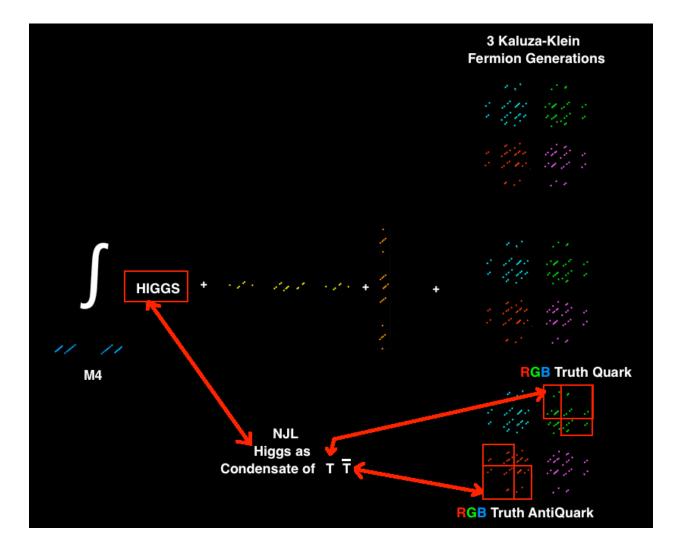


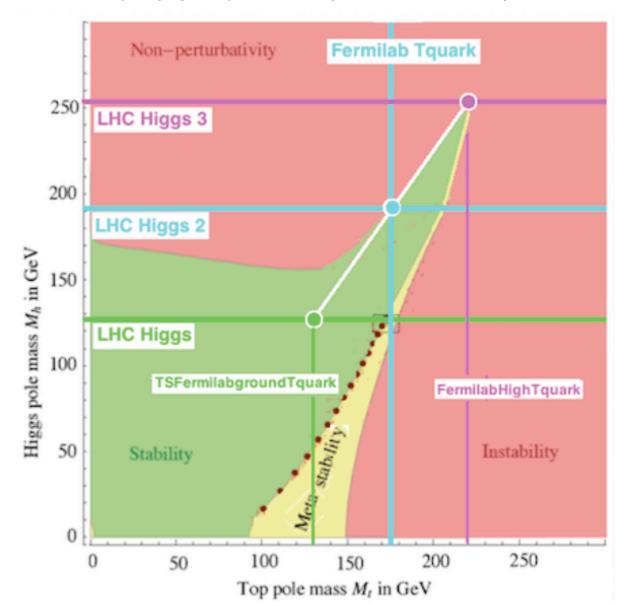
One 600-Cell represents M4 and the other 600-Cell represents CP2:

Splitting Octonionic Spacetime into Quaternionic M4 x CP2 Kaluza-Klein over CP2 produces Higgs by the Mayer Mechanism and Second and Third Generation Fermions

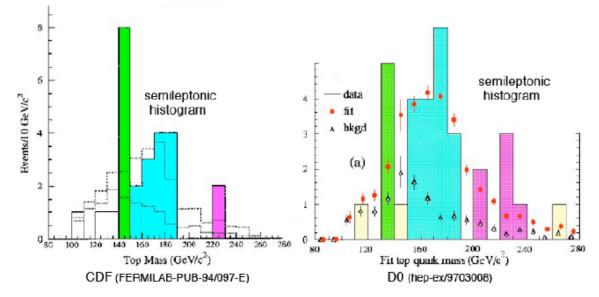


By generalizations of the Nambu-Jona-Lasinio mechanism Higgs is a Fermion Particle-AntiParticle Condensate which, since the Truth Quark is by far the most massive Fermion, effectively means that Higgs is a Truth Quark - Truth AntiQuark Condensate.



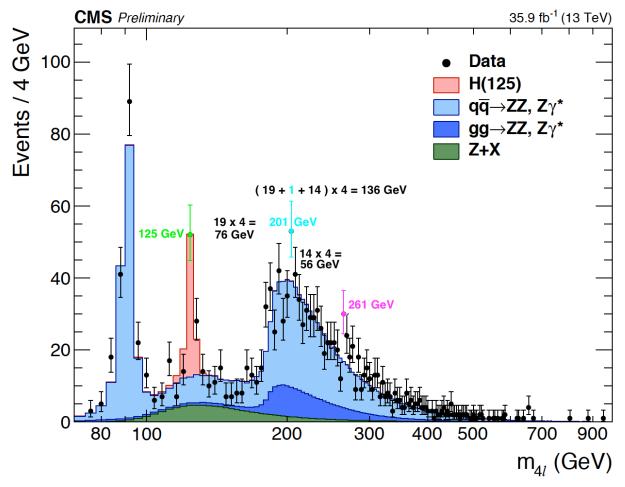


Higgs - Truth Quark System has 3 mass states for Higgs and for Truth Quark that have (in my opinion) been seen by Fermilab and LHC experiments



Semileptonic histograms of CDF and D0 show 3 Truth Quark Mass States





The histogram, from CMS-PAS-HIG-16-041 discussed at Moriond March 2017, has bins of 4 GeV width, so that CMS analysis shows two higher Higgs mass states:

middle-mass Higgs state (cyan) with mass 201 GeV high-mass Higgs state (magenta) with mass 261 GeV

The CMS observation of 261 GeV for the high-mass Higgs state is somewhat higher than the theoretical value given by Koichi Yamawaki in hep-ph/9603293 where he says: "... the four-fermion theory in the presence of gauge interactions (... gauged Nambu-Jona-Lasinio (NJL) ... model) can become renormalizable and nontrivial ... The Higgs boson was predicted as a tbar-t bound state ... Its mass was ... calculated by BHL ... [Bardeen-Hill-Lindner] ... through the full RG equation ... the result being ... MH = mt x 1.1 at 10^19 GeV ...[which gives]... MH = 239 +/- 3 GeV ..."

The CMS observation of 201 GeV for the middle-mass Higgs state is also somewhat higher than the theoretical value given by Hashimoto, Tanabashi, and Yamawaki in hep-ph/0311165 where they say:

"... We perform the most attractive channel (MAC) analysis in the top mode standard model with TeV-scale extra dimensions for ...[Kaluza-Klein type]... dimension... D=8 ... $m_t = 172-175$ GeV and $m_H=176-188$ GeV ...".

In both cases

the CMS observed mass is about 20 GeV higher than the theoretical mass which is close enough to show that the theory is fundamentally realistic but indicates that further experimental data and study of data analysis and consideration of refinements of the theoretical models would be useful.

Consensus 1-state Higgs and Tquark give Metastable Universe but E8 3-state Higgs and Tquark gives Stable Universe at Low Energy and 8-dim Kaluza-Klein Compositeness at Medium Energy and Full Electroweak Symmetry at High Energy

The Consensus View of experimental results of the LHC and Fermilab is that there is only one Higgs state and it is the 125 GeV state and everything else seen by the LHC is statistical fluctuation and

that there is only one Tquark state and it is the 174 GeV state and everything else seen by Fermilab or the LHC is statistical fluctuation.

Based on the history of Fermilab analyses since the 1990s

and on the fact at Moriond 2017 for the channel H -> ZZ* -> 4I

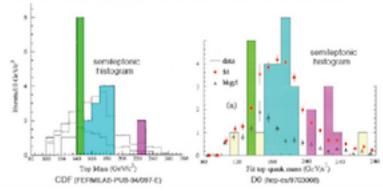
Oda's slide 14 about ATLAS analysis covered only Higgs masses 80 to 170 GeV and

Mei's slide 2 about CMS analysis covered only Higgs masses 70 to 170 GeV it seems likely

that all Higgs mass analysis of 2017 data will be only for the region 70 to 170 GeV so that

the two higher-mass Higgs states of E8 physics will forever be ignored.

A similar thing happened with analyses of Tquark mass states at Fermilab in the 1990s. Semileptonic histograms of CDF and D0 show 3 Truth Quark Mass States



Then the Fermilab Consensus decided: that there is only one Tquark mass state; that it is the 174 GeV central (cyan) peak; and that the green and magenta peaks predicted by E8 physics are only statistical fluctuations.

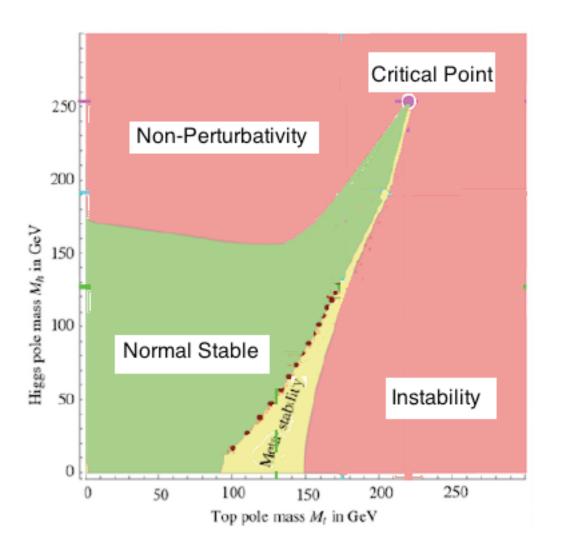
Therefore later Fermilab analyses experiments ignored the green and magenta peaks.

What does this mean for physics ?

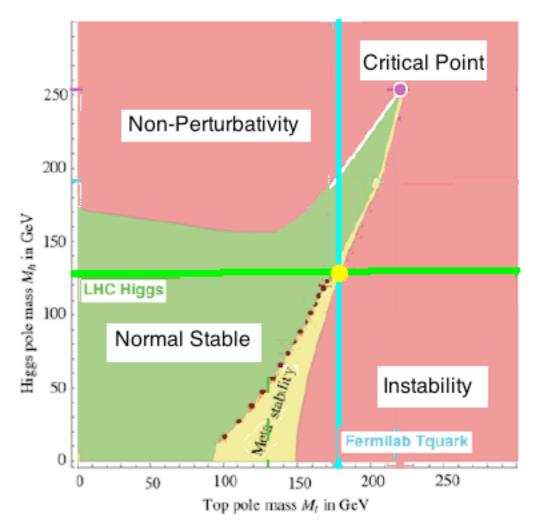
It means that every physics student has been since the 1990s and will be from now on taught that the Standard Model has only one Higgs mass state (125 GeV) and one Tquark mass state (174 GeV).

WHAT IS WRONG WITH THAT ? WHAT REAL DIFFERENCE WOULD IT MAKE TO FOLLOW THE CONSENSUS ?

If you use the Standard Model to plot Higgs mass against Tquark mass you get this phase diagram:



Where is the Consensus View on the Phase Diagram ?



The Consensus View of one Higgs at 125 GeV and one Tquark at 174 GeV gives a METASTABLE UNIVERSE that might destroy itself at any moment:

How about the E8 physics model with 3-state Higgs and 3-state Tquark ?

In the E8 physics 3-state model there are 3 intersections:

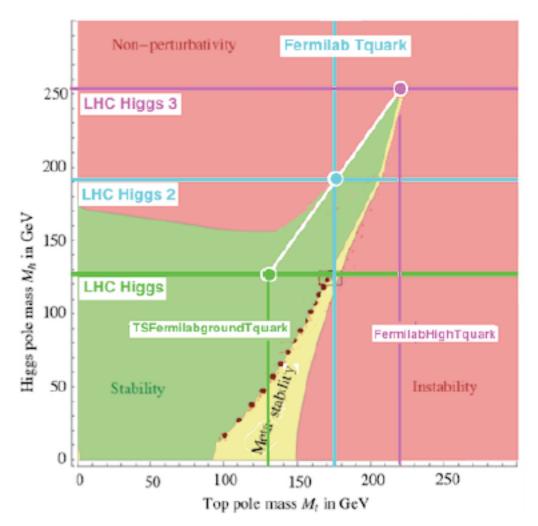
low mass H with low mass Tq medium mass H with medium mass Tq high mass H with high mass Tq

Those 3 intersections are, respectively:

in the Normal Stable region - with STABLE Universe

on the boundary line of non-perturbativity - at which Higgs compositeness and 8-dim Kaluza-Klein spacetime structure become manifest (see hep-ph/0311165 by Hashimoto, Tanabashi, and Yamawaki)

at the critical point - beyond which Electroweak Symmetry is NOT broken and W and Z bosons stay massless



E8 Root Vector Geometry - AQFT - 26D String Theory -- Schwinger Sources - Quantum Consciousness

Frank Dodd (Tony) Smith, Jr. - 2017 - viXra 1701.0495

Abstract

This paper is intended to be a only rough semi-popular overview of how the 240 Root Vectors of E8 can be used to construct a useful Lagrangian and Algebraic Quantum Field Theory (AQFT) in which the Bohm Quantum Potential emerges from a 26D String Theory with Strings = World-Lines = Path Integral Paths and the Massless Spin 2 State interpreted as the Bohm Quantum Potential. For details and references, see viXra/1602.0319.

The 240 Root Vectors of E8 represent the physical forces, particles, and spacetime that make up the construction of a realistic Lagrangian describing the Octonionic Inflation Era. The Octonionic Lagrangian can be embedded into a Cl(1,25) Clifford Algebra which with 8-Periodicity gives an AQFT. The Massless Spin 2 State of 26D String Theory gives the Bohm Quantum Potential. The Quantum Code of the AQFT is the Tensor Product Quantum Reed-Muller code. A Single Cell of the 26D String Theory model has the symmetry of the Monster Group. Quantum Processes produce Schwinger Sources with size about 10^(-24) cm. Microtubule Structure related to E8 and Clifford Algebra enable Penrose-Hameroff Quantum Consciousness. E8 and Cl(8) may have been encoded in the Great Pyramid. A seperate paper discusses using the Quaternionic M4 x CP2 Kaluza-Klein version of the Lagrangian to produce the Higgs and 2nd and 3rd Generation Fermions and a Higgs - Truth Quark System with 3 Mass States for Higgs and Truth Quark.

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Recipe for constructing Lagrangian from E8 Root Vectors ... page 7 Octonionic Inflation and Clifford Algebra 8-Periodicity AQFT ... page 9 Cl(1,25) E8 AQFT with Paths=World-Lines=Strings gives 26D String Theory ... page 11 Massless Spin 2 State of 26D String Theory = Bohm Quantum Potential ... page 15 AQFT Quantum Code = Tensor Product Quantum Reed-Muller code ... page 16 Monster Symmetry of a Single Cell of the 26D String Theory model ... page 17 Schwinger Sources ... page 19 Penrose-Hameroff Quantum Consciousness ... page 24 Condensate Structure of Higgs and Spacetime ... page 29 Great Pyramid, Clifford Algebra Cl(8), and E8 ... page 31 The **240 root vectors of E8** are of equal length in 8 dimensions as they form the 240-vertex Witting-Gossett polytope so you can in 8 dimensions visualize how they group together If you look at the 240 vertices as points on an 8-dim sphere then you can pick one point as the North Pole

and

see where the other points fall at their angle of latitude:

1 is at North Pole

56 nearest neighbors of the North Pole are at North Temperate Latitude

126 2nd nearest neighbors of the North Pole are at the Equator

56 3rd nearest neighbors of the North Pole are at South Temperate Latitude

1 4th nearest neighbor of the North Pole is Anitpodal at the South Pole

Therefore you see that the 240 break down into 1 + 56 + 126 + 56 + 1 but what you need to see next is which root vector corresponds to which physics thing.

Geometry of the E8 Lie Group gives you some ideas:

56 + 56 = 112 Temperate North and South is the D8 = Spin(16) subgroup of E8 and they correspond to Gravity + Dark Energy and the Standard Model gauge groups and to 8-dimensional Spacetime position and momentum.

Each 56 breaks down into 24 + 32.

North Temperate 24 = D4 Lie Algebra = Spin(2,6) which contains Conformal Spin(2,4) which gives Gravity plus Conformal Dark Energy as well as Ghosts of Standard Model Gauge Bosons

South Temperate 24 = D4 Lie Algebra = Spin(8) which contains SU(4) which gives SU(3) of the Color Force which is the Global Group of Kaluza-Klein Internal Symmetry Space CP2 and CP2 = SU(3) / SU(2) x U(1) contains groups of Weak and Electromagnetic Forces as well as Ghosts of Gravity and Dark Energy

Symmetric space D8 / D4(gravity) x D4(standard model) is 112-28-28 = 64-dim and it corresponds to 64 = 8-dim position x 8-dim momentum of 8-dim Spacetime which

8-dim Spacetime reduces to 4+4 dim M4 x CP2 Kaluza-Klein spacetime

Symmetric space E8 / D8 is 128-dim Rosenfeld OctoOctonionic Projective Plane which is

1 + 126 + 1 of the North Pole, Equator, and South Pole

The 128 are the 8 Spacetime components of Fermions: 8 Particles and 8 AntiParticles for 8x8 = 64 Particle components + 8x8 = 64 AntiParticle components.

1 at North Pole = time component of Neutrino

1 at South Pole = time component of AntiNeutrino

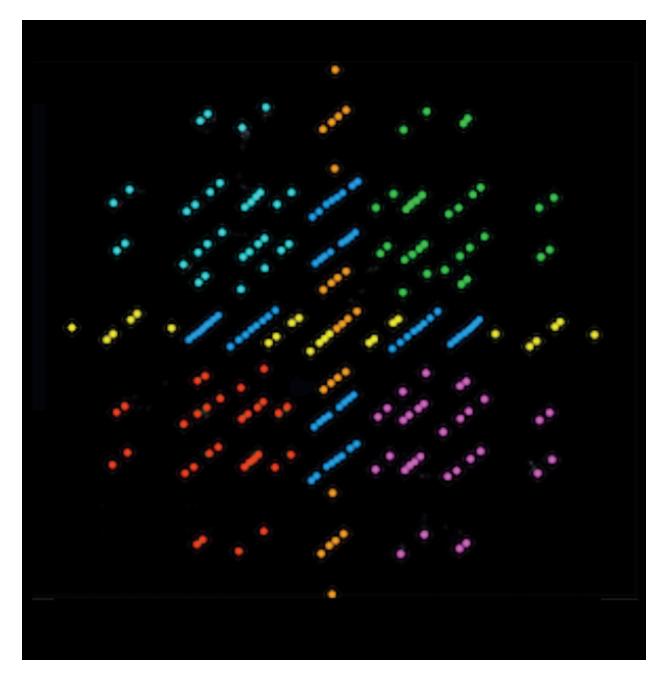
126 at Equator = other components of Leptons and Quarks = root vectors of E7

Symmetric space E7 / D6xSU(2) = 64-dim Rosenfeld QuaterOctonionic Projective Plane corresponds to 8 components of (electron + rgb up quarks) = 8x4 = 32

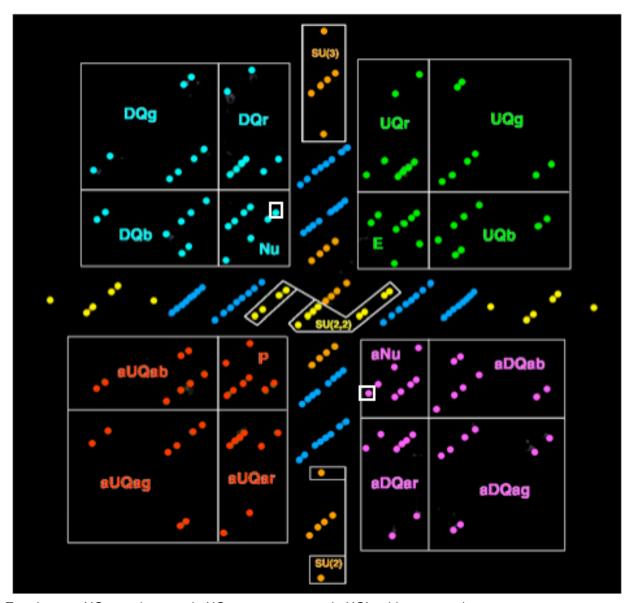
plus 8 components of (positron + rgb up antiquarks) = 8x4 = 32 D6 x SU(2) has 60+2 = 62 root vectors so if you add 1+1 North and South Poles you get 64 corresponding to 8 components of (neutrino + rgb down quarks) = 8x4 = 32 plus 8 components of (antineutrino + rgb down antiquarks) = 8x4 = 32

2-dim projection of 240 E8 Root Vectors gives useful visualization of which root vector corresponds to which physics thing

In 2-dim Projection the Root Vectors no longer have the same distance from origin



but in this particular 2-dim projection the physical interpretations of each Root Vector becomes clear:



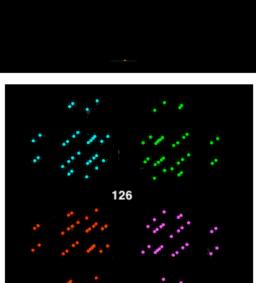
E = electron, UQr = red up quark, UQg = green up quark, UQb = blue up quark Nu = neutrino, DQr = red down quark, DQg = green down quark, DQb = blue down quark P = positron, aUQar = anti-red up antiquark, aUQag = anti-green up antiquark, aUQab = anti-blue up antiquark aNu = antineutrino, aDQar = anti-red down antiquark white boxes enclose time components of neutrino and antineutrino aDQag = anti-green down antiquark, aDQab = anti-blue down antiquark Each Lepton and Quark has 8 components with respect to 4+4 dim Kaluza-Klein 6 orange SU(3) and 2 orange SU(2) represent Standard Model root vectors 24-6-2 = 16 orange represent U(2,2) Conformal Gravity Ghosts 12 yellow SU(2,2) represent Standard Model Ghosts 32+32 = 64 blue represent 4+4 dim Kaluza-Klein spacetime position and momentum

Here is how the 2-dim physical interpretations correspond to the 8-dim Sphere Latitude decomposition: 1 is at North Pole



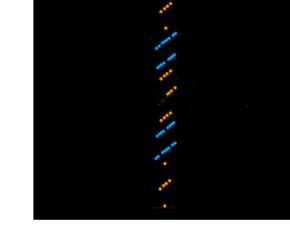
1.11111111





126 2nd nearest neighbors of the North Pole are at the Equator

56 3rd nearest neighbors of the North Pole are at South Temperate Latitude



1 4th nearest neighbor of the North Pole is Anitpodal at the South Pole



Recipe for constructing Lagrangian from E8 Root Vectors

My favorite Fundamental Structure of Physics is the Lagrangian. In his Dirac Lecture, Steven Weinberg says "... Lagrangian density ... you can think of it as the density of energy. Energy is the guantity that ... tells us how the system evolves. ...".

The Lagrangian Density contains Boson terms and Fermion terms. To get the full Lagrangian, you integrate those terms over Spacetime.

The Code or Recipe just says:

put

the Gravity + Dark Energy Gauge Bosons and Standard Model Ghosts and

the Standard Model Gauge Bosons and Gravity-Dark Energy Ghosts into the Lagrangian Density Boson terms in accord with the standard way of constructing physics boson terms

and

put

the Fermion Particles and AntiParticles

into the Lagrangian Density Fermion terms in accord with the standard way of constructing physics fermion terms

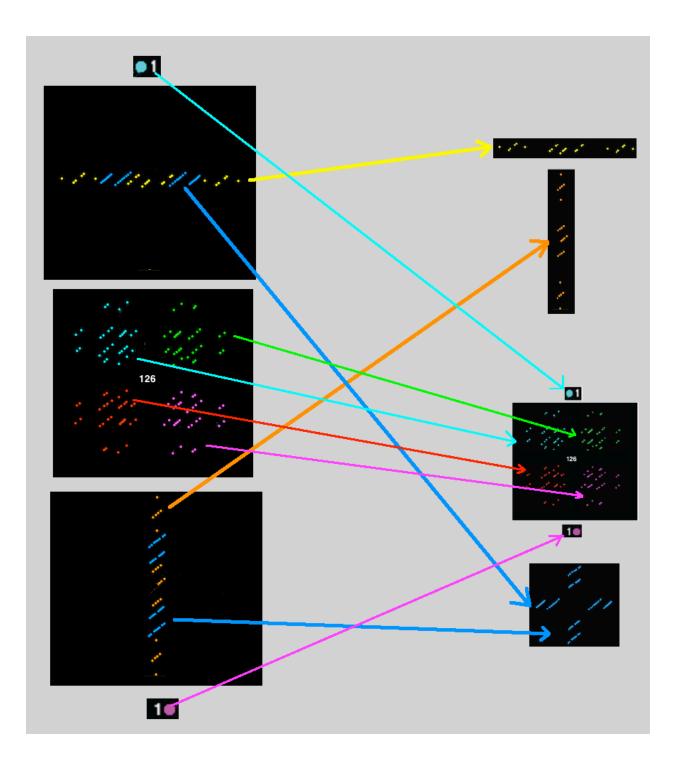
and

put the Spacetime Root Vectors into the Spacetime Base Manifold over which the Lagrangian Density is integrated.

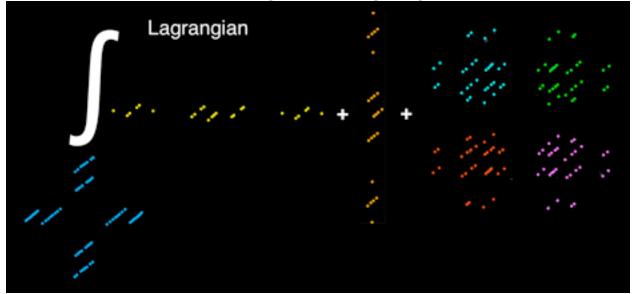
In terms of the preceding pictures of physics of E8 Root Vectors the Code or Recipe gives a Lagrangian that is a realistic physics model.

Of course, to completely carry out the Code or Recipe you need to write out the Lagrangian terms in the math language of conventional physics and that is described in some of the long papers I have written (see my web site and my viXra papers).

Here I am just trying to show the basic underlying structure of E8 Geometry so I am not writing down the extensive details in this paper.



The fundamental Lagrangian formed by this structure is an Octonionic structure over 8-dim Spacetime and is effective during the Initial Big Bang and Inflation.



Inflation Ends when a preferred Quaternionic Subspacetime freezes out, converting 8 dim Spacetime into 4+4 dim M4 x CP2 Spacetime where

M4 = Physical Minkowski Spacetime and CP2 = SU(3) / U(2) Internal Symmetry Space and the Octonionic Integral becomes two Quaternionic Integrals but

the Octonionic Lagrangian can be used as a basis for constructing an AQFT (Algebraic Quantum Field Theory)

by embedding each local E8 local classical Lagrangian into a copy of Cl(0,16) The E8 Physics Creation Sequence begins with Spinor/Clifford Algebra Doubling

Cl(0,0) -> Cl(0,2) -> Cl(0,4) -> Cl(0,6) -> Cl(0,8) ->

that goes to Cl(0,8) which has Vector - Half-Spinor Triality and is the Basic Building Block of 8-Periodicity of Real Clifford Algebras whereby the Creation Sequence continues by Tensor Product

-> CI(0,8)xCI(0,8) = CI(0,16) -> CI(0,16)xCI(0,8) = CI(0,24) ->

CI(0,16) contains the Maximal Exceptional E8 Lie Algebra

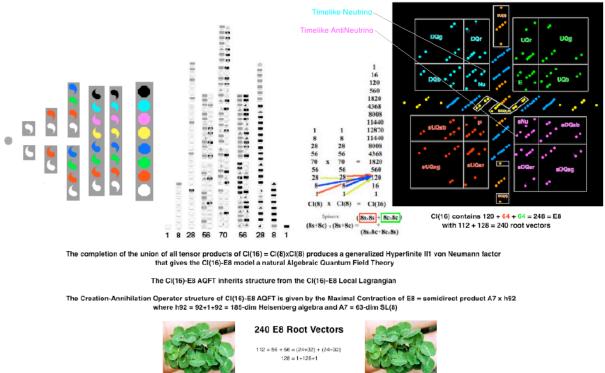
CI(0,24) contains the Vector Space of the 24-dim Leech Lattice \land 24 that is 3 copies of E8 Lattices (2 being Integral Domains and 1 not Algebraically closed)

The Creation Sequence continues by constructing the Conformal Structure of $2x^2$ matrices with entries in Cl(0,24) = M(2,Cl(0,24))

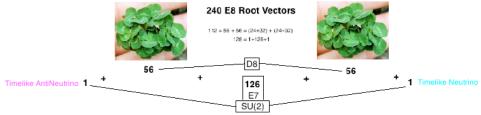
Since all the matrix entries are CI(0,24) = tensor product of 3 copies of CI(0,8)8-Periodicity allows formation of the tensor products of copies of CI(1,25)

-> Completion of Union of All Tensor Products of Cl(1,25) = hyperfinite AQFT

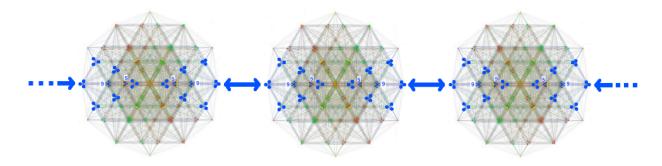
(This hyperfinite algebra structure corresponds to the Universal Action Reservoir of Garrett Lisi in arXiv physics/0605068) Cl(0,0) -> Cl(0,2) -> Cl(0,4) -> Cl(0,6) -> Cl(0,8) -> Cl(0,8)xCl(0,8) = Cl(0,16) --> Cl(0,16)xCl(0,8) = Cl(0,24) -> M(2,Cl(0,24)) = Cl(1,25) -> -> Completion of Union of All Tensor Products of Cl(1,25) = hyperfinite AQFT



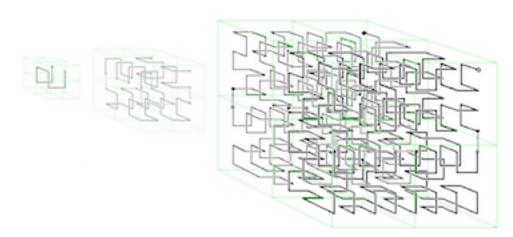
Cl(1,25) = Cl(1,9)xCl(0,8)xCl(0,8) and Cl(1,9) = Cl(1,5) x Cl(0,4) = Cl(2,4) x Cl(0,4)



One Cl(1,25) containing one Cl(0,16) containing one E8 gives a Lagrangian description of one local spacetime neighborhood. To get a realistic global spacetime structure, take the tensor product Cl(1,25) x ... x Cl(1,25) with all E8 local 8-dim Octonionic spacetimes consistently aligned as described by 64-dim D8 / D4xD4 (blue dots) (this visualization uses a hexagonal type of projection of the 240 E8 root vectors to 2-dim)



which then fill up spacetime according to Gray Code Hilbert's curves:



The Union of all Cl(1,25) tensor products is the Union of all subdivided 8-HyperCubes and

their Completion is a huge superposition of 8-HyperCube Continuous Volumes which Completion belongs to the Third Grothendieck Universe.

The Cl(1,25) E8 AQFT inherits structure from the Cl(1,25) E8 Local Lagrangian

Gauge Gravity + Standard Model + Fermion Particle-AntiParticle

8-dim SpaceTime .

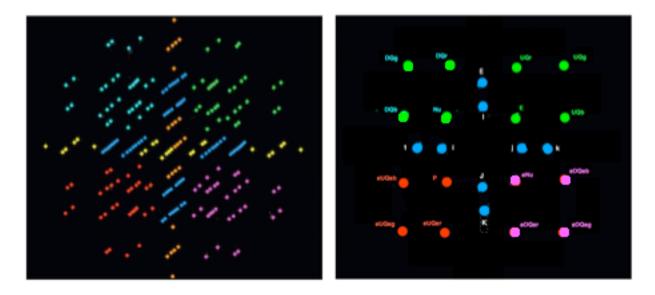
whereby World-Lines of Particles are represented by Strings moving in a space whose dimensionality includes 8v = 8-dim SpaceTime Dimensions + + 8s+=8 Fermion Particle Types + 8s-=8 Fermion AntiParticle Types combined in the traceless part J(3,O)o of the 3x3 Octonion Hermitian Jordan Algebra a 8s+8v

8s+* b 8s-

8v* 8s-* -a-b

which has total dimension 8v + 8s + 8s - 2 = 26 and is the space of a 26D String Theory with Strings seen as World-Lines.

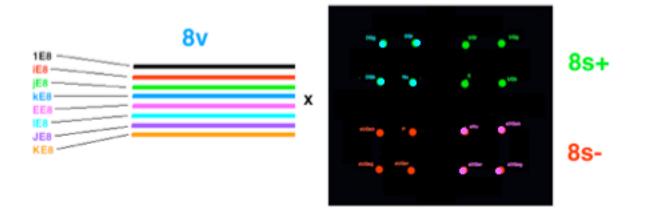
24 = 8v + 8s + 8s- of the 26 dimensions of 26D String Theory correspond to 24x8 = 192 of the 240 E8 Root Vectors by representing the 8v + 8s + 8s- as superpositions of their respective 8 components



8v SpaceTime is represented by D8 branes. A D8 brane has Planck-Scale Lattice Structure superpositions of 8 types of E8 Lattice denoted by 1E8, iE8, jE8, kE8, EE8, IE8, JE8, KE8



A single Snapshot of SpaceTime is represented by a D8 brane at each point of which is placed Fermion Particles or AntiParticles represented by 8+8 = 16 orbifolded dimensions of the 26 dimensions of 26D String Theory.



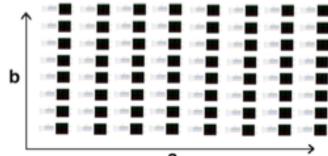
It is necessary to patch together SpaceTime Snapshots to form a Global Structure describing a Many-Worlds Global Algebraic Quantum Field Theory (AQFT) whose structure is described by Deutsch

in "The Fabric of Reality" (Penguin 1997 pp. 276-283):

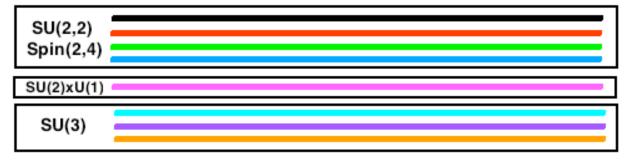
"... there is no fundamental demarcation between snapshots of other times and snapshots of other universes ... Other times are just special cases of other universes ... Suppose ... we toss a coin ... Each point in the diagram represents one snapshot ... in the multiverse there are far too many snapshots for clock readings alone to locate a snapshot relative to the others. To do that, we need to consider the intricate detail of which snapshots determine which others. ...

in some regions of the multiverse, and in some places in space, the snapshots of some physical objects do fall, for a period, into chains, each of whose members determines all the others to a good approximation ...".

The Many-Worlds Snapshots are structured as a 26-dim Lorentz Leech Lattice of 26D String Theory parameterized by the a and b of J(3,O)o as indicated in this 64-element subset of Snapshots



The 240 - 192 = 48 = 24+24 Root Vector Vertices of E8 that do not represent the 8-dim D8 brane or the 8+8 = 16 dim of Orbifolds for Fermions do represent the Gauge Bosons (and their Ghosts) of E8 Physics: Gauge Bosons from 1E8, iE8, jE8, and kE8 parts of a D8 give U(2,2) Conformal Gravity Gauge Bosons from EE8 part of a D8 give U(2) Electroweak Force Gauge Bosons from IE8, JE8, and KE8 parts of a D8 give SU(3) Color Force



Each Deutsch chain of determination represents a World-Line of Particles / AntiParticles corresponding to a String of 26D String Theory

such as the red line in this 64-element subset of Snapshots



26D String Theory is the Theory of Interactions of Strings = World-Lines = Paths (World-Lines = Path Integral Paths of Garrett Lisi in arXiv physics/0605068)

Interactions of World-Lines can describe Quantum Theory according to Andrew Gray (arXiv quant-ph/9712037): "... probabilites are ... assigned to entire fine-grained histories ... base[d] ... on the Feynman path integral formulation ... The formulation is fully relativistic and applicable to multi-particle systems. It ... makes the same experimental predictions as quantum field theory ...". Green, Schwartz, and Witten say in their book "Superstring Theory" vol. 1 (Cambridge 1986) "... For the ... closed ... bosonic string [26D String Theory] The first excited level ... consists of ... the ground state ... tachyon ... and ... a scalar ... 'dilaton' ... and ... SO(24) ... little group of a ...[26-dim]... massless particle ... and ... a ... massless ... spin two state ...".

Closed string tachyons localized at orbifolds of fermions produce virtual clouds of particles / antiparticles that dress fermions.

Dilatons are Goldstone bosons of spontaneously broken scale invariance that (analagous to Higgs) go from mediating a long-range scalar gravity-type force to the nonlocality of the Bohm-Sarfatti Quantum Potential.

The SO(24) little group is related to the Monster automorphism group that is the symmetry of each cell of Planck-scale local lattice structure.

The massless spin 2 state = Bohmion = Carrier of the Bohm Force of the Bohm Quantum Potential.

The Creation-Annihilation Operator structure of the Bohm Quantum Potential of 26D String Theory and AQFT Quantum Code Information System

is given by the Maximal Contraction of E8 = semidirect product A7 x h92 where h92 = 92+1+92 = 185-dim Heisenberg algebra and A7 = 63-dim SL(8)

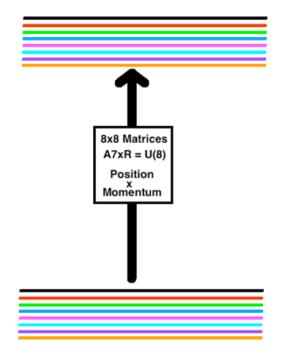
The Maximal E8 Contraction A7 x h92 can be written as a 5-Graded Lie Algebra 28 + 64 + (SL(8,R) + 1) + 64 + 28

Central Even Grade 0 = SL(8,R) + 1

The 1 is a scalar and SL(8,R) = Spin(8) + Traceless Symmetric 8x8 Matrices, so SL(8,R) represents a local 8-dim SpaceTime in Polar Coordinates.

Odd Grades -1 and +1 = 64 + 64Each = 64 = 8x8 = Creation/Annihilation Operators for 8 components of 8 Fundamental Fermions.

Even Grades -2 and +2 = 28 + 28 Each = Creation/Annihilation Operators for 28 Gauge Bosons of Gravity + Standard Model. The 8x8 matrices linking one D8 to the next D8 of a World-Line String give A7xR = U(8) representing Position x Momentum



Cerf and Adami in quantum-ph/9512022 describe virtual qubit-anti-qubit pairs (they call them ebit-anti-ebitpairs) that are related to negative conditional entropies for quantum entangled systems and are similar to fermion particle-antiparticle pairs. Therefore quantum information processes can be described by particle-antiparticle diagrams much like particle physics diagrams and the **Algebraic Quantum Field Theory of the Cl(1,25) E8 Physics Model should have a Quantum Code Information System** that is based on structure of a unit cell in 26D String Theory represented by Real Clifford Algebra Cl(0,8) x Cl(0,8) x Cl(0,8) = Cl(0,24)

> Since Quantum Reed-Muller code [[256 , 0 , 24]] corresponds to Real Clifford Algebra Cl(0,8)

Tensor Product Quantum Reed-Muller code [[256 , 0 , 24]] x [[256 , 0 , 24]] x [[256 , 0 , 24]] corresponds to AQFT (Algebraic Quantum Field Theory) hyperfinite von Neumann factor algebra that is Completion of the Union of All Tensor Products of Cl(1,25) A Single Cell of E8 26-dimensional Bosonic String Theory, in which Strings are physically interpreted as World-Lines, can be described by taking the quotient of its 24-dimensional O+, O-, Ov subspace modulo the 24-dimensional Leech lattice. Its automorphism group is the largest finite sporadic group, the Monster Group, whose order is 8080, 17424, 79451, 28758, 86459, 90496, 17107, 57005, 75436, 80000, 00000 =

2^46 .3^20 .5^9 .7^6 .11^2 .13^3 .17.19.23.29.31.41.47.59.71 or about 8 x 10^53.

What happens to a Fundamental Fermion Particle whose World-Line string intersects a Single Cell ?

The Fundamental Fermion Particle does not remain a single Planck-scale entity. Tachyons create clouds of particles/antiparticles as described by Bert Schroer in hep-th/9908021: "... any compactly localized operator applied to the vacuum generates clouds of pairs of particle/antiparticles ... More specifically it leads to the impossibility of having a local generation of pure one-particle vectors unless the system is interaction-free ...".

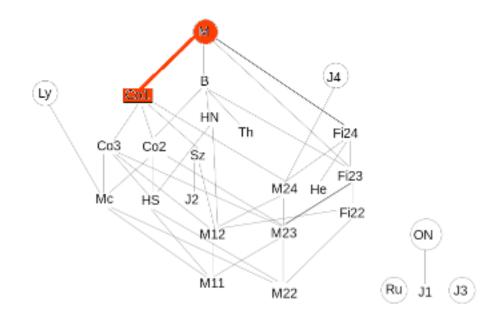
What is the structural form of the Fundamental Fermion Cloud ?

In "Kerr-Newman [Black Hole] solution as a Dirac particle", hep-th/0210103, H. I. Arcos and J. G. Pereira say: "... For $m^2 < a^2 + q^2$, with m, a, and q respectively the source mass, angular momentum per unit mass, and electric charge, the Kerr-Newman (KN) solution of Einstein's equation reduces to a naked singularity of circular shape, enclosing a disk across which the metric components fail to be smooth ... due to its topological structure, the extended KN spacetime does admit states with half-integral angular momentum. ... The state vector ... evolution is ... governed by the Dirac equation. ... for symmetry reasons, the electric dipole moment of the KN solution vanishes identically, a result that is within the limits of experimental data ... a and m are thought of as parameters of the KN solution, which only asymptotically correspond respectively to angular momentum per unit mass and mass. Near the singularity, a represents the radius of the singular ring ... With ... renormalization ... for the usual scattering energies, the resulting radius is below the experimental limit for the extendedness of the electron ...".

What is the size of the Fundamental Fermion Kerr-Newman Cloud ?

The FFKN Cloud is one Planck-scale Fundamental Fermion Valence Particle plus an effectively neutral cloud of particle/antiparticle pairs. The symmetry of the cloud is governed by the 24-dimensional Leech lattice by which the Single Cell was formed.

Here (adapted from Wikipedia) is a chart of the Monster M and its relation to other Sporadic Finite Groups and some basic facts and commentary:



The largest such subgroups of M are B, Fi24, and Co1.

B, the Baby Monster, is sort of like a downsized version of M, as B contains Co2 and Fi23 while M contains Co1 and Fi24.

Fi24 (more conventionally denoted Fi24') is of order $1255205709190661721292800 = 1.2 \times 10^{24}$ It is the centralizer of an element of order 3 in the monster group M and is a triple cover of a 3-transposition group. It may be that Fi24' symmetry has its origin in the Triality of E8 26-dim String Theory.

The order of Co1 is 2^21.3^9.5^4.7^2.11.13.23 or about 4 x 10^18.

Aut(Leech Lattice) = double cover of Co1.

The order of the double cover 2.Co1 is $2^22.3^9.5^4.7^2.11.13.23$ or about 0.8 x 10^19. Taking into account the non-sporadic part of the Leech Lattice symmetry according to the ATLAS at brauer.maths.qmul.ac.uk/Atlas/v3/spor/M/ the maximal subgroup of M involving Co1 is $2^(1+24)$.Co1 of order 139511839126336328171520000 = 1.4×10^{26}

As 2.Co1 is the Automorphism group of the Leech Lattice modulo to which the Single Cell was formed, and as

the E8 26-dim String Theory Leech Lattice is a superposition of 8 Leech Lattices, 8 x 2^(1+24).Co1 describes the structure of the FFKN Cloud. Therefore,

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the volume of the FFKN Cloud should be on the order of 10^27 x Planck scale, and
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the FFKN Cloud should contain on the order of 10^27 particle/antiparticle pairs and its size should be somewhat larger than, but roughly similar to, $10^{(27/3)} \times 1.6 \times 10^{(-33)} \text{ cm} = \text{roughly } 10^{(-24)} \text{ cm}.$

FFKN Clouds are Schwinger Sources.

Schwinger Sources, Hua Geometry, and Wyler Calculations

Fock "Fundamental of Quantum Mechanics" (1931) showed that sources require Linear Operators "... represented by a definite integral [of a]... kernel ... function ...".

Hua "Harmonic Analysis of Functions of Several Complex Variables in the Classical Domains" (1958) showed Kernel Functions for Complex Classical Domains.

Schwinger (1951 - see Schweber, PNAS 102, 7783-7788) "... introduced a description in terms of Green's functions, what Feynman had called propagators ... The Green's functions are vacuum expectation values of time-ordered Heisenberg operators, and the field theory can be defined non-perturbatively in terms of these functions ...[which]... gave deep structural insights into QFTs; in particular ... the structure of the Green's functions when their variables are analytically continued to complex values ...".

Wolf (J. Math. Mech 14 (1965) 1033-1047) showed that the Classical Domains (complete simply connected Riemannian symmetric spaces) representing 4-dim Spacetime with Quaternionic Structure are:

S1 x S1 x S1 x S1 x S1 = 4 copies of U(1) S2 x S2 = 2 copies of SU(2) CP2 = SU(3) / SU(2)xU(1)S4 = Spin(5) / Spin(4) = Euclidean version of Spin(2,3) / Spin(1,3)

Armand Wyler (1971 - C. R. Acad. Sc. Paris, t. 271, 186-188) showed how to use Green's Functions = Kernel Functions of Classical Domain structures characterizing Sources = Leptons, Quarks, and Gauge Bosons, to calculate Particle Masses and Force Strengths

Schwinger (1969 - see physics/0610054) said: "... operator field theory ... replace[s] the particle with ... properties ... distributed througout ... small volumes of three-dimensional space ... particles ... must be created ... even though we vary a number of experimental parameters ... The properties of the particle ... remain the same ... We introduce a quantitative description of the particle source in terms of a source function ... we do not have to claim that we can make the source arbitrarily small ... the experimeter... must detect the particles ...[by]... collision that annihilates the particle ... the source ... can be ... an abstraction of an annihilation collision, with the source acting negatively, as a sink ... The basic things are ... the source functions ... describing the intermediate propagation of the particle ...".

Schwinger Sources can be described by continuous manifold structures of Bounded Complex Domains and their Shilov Boundaries but

the Cl(16)-E8 model at the Planck Scale has spacetime condensing out of Clifford structures forming a Leech lattice underlying 26-dim String Theory of World-Lines with 8 + 8 + 8 = 24-dim of fermion particles and antiparticles and of spacetime.

The automorphism group of a single 26-dim String Theory cell modulo the Leech lattice is the Monster Group of order about 8 x 10^53.

When a fermion particle/antiparticle appears in E8 spacetime it does not remain a single Planck-scale entity because Tachyons create a cloud of particles/antiparticles. The cloud is one Planck-scale Fundamental Fermion Valence Particle plus an effectively neutral cloud of particle/antiparticle pairs forming a Kerr-Newman black hole. That Kerr-Newman cloud constitutes the E8 Physics model Schwinger Source.

The cloud structure comes from the 24-dim Leech lattice part of the Monster Group which is $2^{(1+24)}$ times the double cover of Co1, for a total order of about 10²⁶.

Since a Leech lattice is based on copies of an E8 lattice and since there are 7 distinct E8 integral domain lattices

there are 7 (or 8 if you include a non-integral domain E8 lattice) distinct Leech lattices. The physical Leech lattice is a superposition of them,

effectively adding a factor of 8 to the order,

so the volume of the Kerr-Newman Cloud is on the order of 10^{27} x Planck scale and the Kerr-Newman Cloud should contain about 10^{27} particle/antiparticle pairs and its size should be about $10^{(27/3)}$ x 1.6 x $10^{(-33)}$ cm = roughly $10^{(-24)}$ cm.

The Cl(1,25) E8 model Lagrangian over 4-dim Minkowski SpaceTime M4 is

GG + SM + Fermion Particle-AntiParticle + Higgs 4-dim M4 .

Consider the Fermion Term.

In the conventional picture, the spinor fermion term is of the form m S S^{*} where m is the fermion mass and S and S^{*} represent the given fermion.

The Higgs coupling constants are, in the conventional picture, ad hoc parameters, so that effectively the mass term is, in the conventional picture, an ad hoc inclusion.

The Cl(1,25) E8 model constructs the Lagrangian integral such that the mass m emerges as the integral over the Schwinger Source spacetime region of its Kerr-Newman cloud of virtual particle/antiparticle pairs plus the valence fermion so that the volume of the Schwinger Source fermion defines its mass, which, being dressed with the particle/antiparticle pair cloud, gives quark mass as constituent mass.

Fermion Schwinger Sources correspond to the Lie Sphere Symmetric space Spin(10) / Spin(8)xU(1)

which has

local symmetry of the Spin(8) gauge group from which the first generation spinor fermions are formed as +half-spinor and -half-spinor spaces and Bounded Complex Domain D8 of type IV8 and Shilov Boundary Q8 = RP1 x S7

Consider the GG + SM term from Gauge Gravity and Standard Model Gauge Bosons. The process of breaking Octonionic 8-dim SpaceTime down to Quaternionic (4+4)-dim M4 x CP2 Kaluza-Klein creates differences in the way gauge bosons "see" 4-dim Physical SpaceTime. There 4 equivalence classes of 4-dimensional Riemannian Symmetric Spaces with Quaternionic structure consistent with 4-dim Physical SpaceTime:

S4 = 4-sphere = Spin(5) / Spin(4) where Spin(5) = Schwinger-Euclidean version of the Anti-DeSitter subgroup of the Conformal Group that gives MacDowell-Mansouiri Gravity

CP2 = complex projective 2-space = SU(3) / U(2) with the SU(3) of the Color Force

S2 x S2 = SU(2)/U(1) x SU(2)/U(1) with two copies of the SU(2) of the Weak Force

S1 x S1 x S1 x S1 = U(1) x U(1) x U(1) x U(1) = 4 copies of the U(1) of the EM Photon (1 copy for each of the 4 covariant components of the Photon)

The Gravity Gauge Bosons (Schwinger-Euclidean versions) live in a Spin(5) subalgebra of the Spin(6) Conformal subalgebra of D4 = Spin(8). They "see" M4 Physical spacetime as the 4-sphere S4 so that their part of the Physical Lagrangian is

Gravity Gauge Boson Term

S4 .

an integral over SpaceTime S4.

The Schwinger Sources for GRb bosons are the Complex Bounded Domains and Shilov Boundaries for Spin(5) MacDowell-Mansouri Gravity bosons.

However, due to Stabilization of Condensate SpaceTime

by virtual Planck Mass Gravitational Black Holes,

for Gravity, the effective force strength that we see in our experiments

is not just composed of the S4 volume and the Spin(5) Schwinger Source volume, but is suppressed by the square of the Planck Mass.

The unsuppressed Gravity force strength is the Geometric Part of the force strength.

The Standard Model SU(3) Color Force bosons live in a SU(3) subalgebra of the SU(4) subalgebra of D4 = Spin(8). They "see" M4 Physical spacetime as the complex projective plane CP2 so that their part of the Physical Lagrangian is

SU(3) Color Force Gauge Boson Term

CP2 .

an integral over SpaceTime CP2.

The Schwinger Sources for SU(3) bosons are the Complex Bounded Domains and Shilov Boundaries for SU(3) Color Force bosons.

The Color Force Strength is given by

the SpaceTime CP2 volume and the SU(3) Schwinger Source volume.

Note that since the Schwinger Source volume is dressed with the particle/antiparticle pair cloud, the calculated force strength is

for the characteristic energy level of the Color Force (about 245 MeV).

The Standard Model SU(2) Weak Force bosons live in a SU(2) subalgebra of the U(2) local group of CP2 = SU(3) / U(2) They "see" M4 Physical spacetime as two 2-spheres S2 x S2 so that their part of the Physical Lagrangian is

SU(2) Weak Force Gauge Boson Term

S2xS2 .

an integral over SpaceTime S2xS2.

The Schwinger Sources for SU(2) bosons are the Complex Bounded Domains and Shilov Boundaries for SU(2) Weak Force bosons.

However, due to the action of the Higgs mechanism,

for the Weak Force, the effective force strength that we see in our experiments is not just composed of the S2xS2 volume and the SU(2) Schwinger Source volume, but is suppressed by the square of the Weak Boson masses.

The unsuppressed Weak Force strength is the Geometric Part of the force strength.

The Standard Model U(1) Electromagnetic Force bosons (photons) live in a U(1) subalgebra of the U(2) local group of CP2 = SU(3) / U(2) They "see" M4 Physical spacetime as four 1-sphere circles S1xS1xS1xS1 = T4 (T4 = 4-torus) so that their part of the Physical Lagrangian is

(U(1) Electromagnetism Gauge Boson Term

T4 .

an integral over SpaceTime T4. The Schwinger Sources for U(1) photons are the Complex Bounded Domains and Shilov Boundaries for U(1) photons. The Electromagnetic Force Strength is given by the SpaceTime T4 volume and the U(1) Schwinger Source volume.

Schwinger Sources as described above are continuous manifold structures of Bounded Complex Domains and their Shilov Boundaries but

the E8 model at the Planck Scale has spacetime condensing out of Clifford structures forming a Leech lattice underlying 26-dim String Theory of World-Lines with 8 + 8 + 8 = 24-dim of fermion particles and antiparticles and of spacetime.

The automorphism group of a single 26-dim String Theory cell modulo the Leech lattice is the Monster Group of order about 8 x 10^53.

When a fermion particle/antiparticle appears in E8 spacetime it does not remain a single Planck-scale entity becauseTachyons create a cloud of particles/antiparticles.

The cloud is one Planck-scale Fundamental Fermion Valence Particle plus an effectively neutral cloud of particle/antiparticle pairs forming a Kerr-Newman black hole. That cloud constitutes the Schwinger Source.

Its structure comes from the 24-dim Leech lattice part of the Monster Group which is $2^{(1+24)}$ times the double cover of Co1, for a total order of about 10^26.

(Since a Leech lattice is based on copies of an E8 lattice and since there are 7 distinct E8 integral domain lattices there are 7 (or 8 if you include a non-integral domain E8 lattice) distinct Leech lattices. The physical Leech lattice is a superposition of them, effectively adding a factor of 8 to the order.)

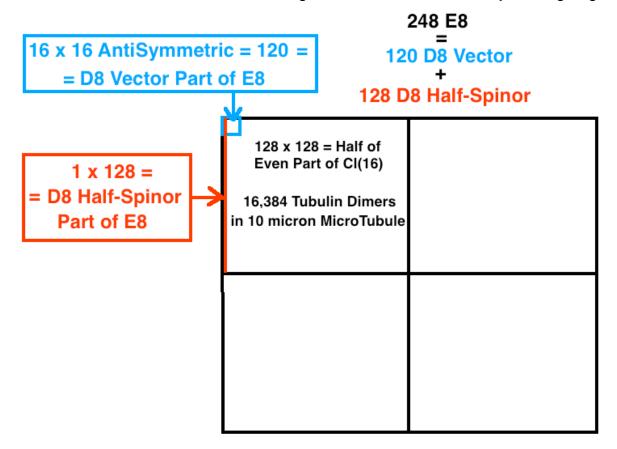
The volume of the Kerr-Newman Cloud is on the order of $10^{27} \times Planck$ scale, so the Kerr-Newman Cloud should contain about 10^{27} particle/antiparticle pairs and its size should be about $10^{(27/3)} \times 1.6 \times 10^{(-33)}$ cm = roughly $10^{(-24)}$ cm.

"... Bohm's Quantum Potential can be viewed as an internal energy of a quantum system ..." according to Dennis, de Gosson, and Hiley (arXiv 1412.5133) and Peter R. Holland says in "The Quantum Theory of Motion" (Cambridge 1993): "... the total force ... from the quantum potential ... does not ... fall off with distance ... because ... the quantum potential ... depends on the form of ...[the quantum state]... rather than ... its ... magnitude ...".

Penrose-Hameroff-type Quantum Consciousness is due to Resonant Quantum Potential Connections among Quantum State Forms. The Quantum State Form of a Conscious Brain is determined by the configuration of a subset of its 10^18 to 10^19 Tubulin Dimers with math description in terms of a large Real Clifford Algebra.

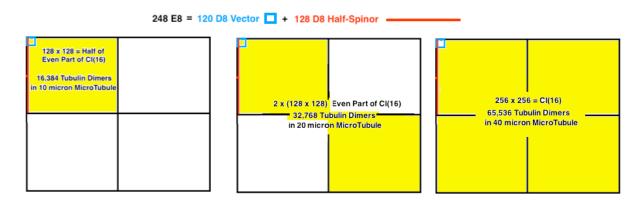
Microtubule binary math / code system corresponds

to Clifford Algebras Cl(8) and Cl(8)xCl(8) = Cl(16) containing E8 A 40 micron Microtubule contains Dimers representing the 65,536 elements of Cl(16) which contains the 248 elements of Lie Algebra E8 that defines E8 Physics Lagrangian.



E8 lives in only half of the block diagonal Even Part half of Cl(16) so that E8 of E8 Physics can be represented by the 16,384 Dimers of a 10 micron Microtubule.

Microtubules spend most of their lives between 10 microns and 40 microns, sizes that can represent E8 as half of the Even Part (half) of Cl(16) (10 microns)



or as the Even Part (half) of Cl(16) (20 microns) or as full Cl(16) (40 microns).

In a given Microtubule the 128 D8 Half-Spinor part is represented by a line of 128 Dimers in its stable GTP region and the 120 D8 Vector part by a 12 x 10 block of Dimers in its stable GTP region (image adapted from 12biophys.blogspot.com Lecture 11)

How do the Microtubules communicate with each other ?

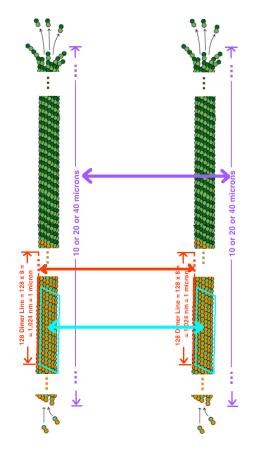
Consider the Superposition of States State 0 and State 1 involving one Tubulin Dimer with Conformation Electron mass m and State1 / State 0 position separation a .

The Superposition Separation Energy Difference is the internal energy

E_ssediff = G m^2 / a

that can be seen as either the **energy of 26D String Theory spin two gravitons or the Bohm Quantum Potential internal energy**, equivalently.

Communication between two Microtubules is by the Bohm Quantum Potential between their respective corresponding Dimers (purple arrow) with the correspondence being based on connection between respective E8 subsets, the 128 D8 Half-Spinors (red arrow) and the 120 D8 BiVectors (cyan arrow)



How is information encoded in the Microtubules ?

Each Microtubule contains E8, allowing Microtubules to be corrrelated with each other. The parts of the Microtubule beyond E8 are in Cl(16) for 40 micron Microtubules, or the Even Subalgebra of Cl(16) for 20 micron Microtubules, or half of the Even Subalgebra of Cl(16) for 10 micron Microtubules so since by 8-Periodicity of Real Clifford Algebras Cl(16) = Cl(8) x Cl(8) and since Cl(8) information is described by the Quantum Reed-Muller code [[256 , 0 , 24]] the information content of Cl(16) and its Subalgebras is described by the Tensor Product Quantum Reed-Muller code [[256 , 0 , 24]] x [[256 , 0 , 24]]

For a 40-micron Microtubule there are, outside the 248-E8 part, about 65,000 TD Qubits available to describe one Quantum Thought State among about 2^65,000 possibilities.

65,536-dimensional CI(16) not only contains the E8 of E8 Physics and the information content of Microtubules but also contains the information content of DNA chromosome condensation and the information content of mRNA triple - amino acid transformations.

In "Living Matter: Algebra of Molecules" (CRC Press 2016) Valery V. Stcherbic and Leonid P. Buchatsky say: "... DNA structure contains four nucleotides: adenine A, guanine G, cytosine C and thymine T. ...

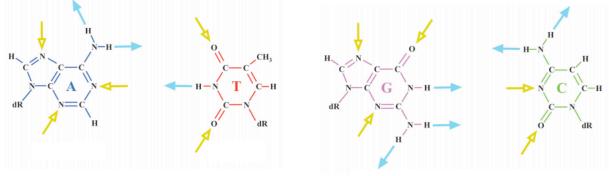


Figure 1.4 Potential vectors of hydrogen bond of DNA nucleotides. Yellow arrows—acceptors, blue arrows—donors of hydrogen.

The space of DNA nucleotide states contains T2^3 \otimes C2^4 \otimes A2^5 \otimes G2^6 = 2^18 elements of Clifford algebras. This space reduction to four nucleotides means compression of DNA information by a factor of 2^18 / 4 = 65536. Reduction of the nucleotide state space leads to DNA compactization and chromosome condensation. ...".

Information lost by condensing DNA is stored in Microtubules through Anaphase after which it has been restored to the new Duplicated DNA

The DNA information condensation factor of 65,536 is the dimension of Cl(16) which is the Real Clifford Algebra containing 248-dim E8 of E8 Physics as 120-dim bivector D8 plus 128-dim D8 half-spinor and is also the Clifford Algebra of Microtubule information in Quantum Consciousness.

What about information in the Many Microtubules of Human Consciousness ?

The information in one Microtubule is based on Cl(16) which is contained in the Cl(1,25) of 26D String Theory E8 Physics

How does this give rise to Penrose-Hameroff Quantum Consciousness ?

Consider the Superposition of States State 0 and State 1 involving one Tubulin Dimer with Conformation Electron mass m and State1 / State 0 position separation a . The Superposition Separation Energy Difference is the internal energy

E_ssediff = G m^2 / a

that can be seen as the energy of 26D String Theory spin two gravitons which physically represent the Bohm Quantum Potential internal energy.

For a given Tubulin Dimer a = 1 nanometer $= 10^{(-7)}$ cm so that $T = h / E_electron = (Compton / Schwarzschild) (a / c) = 10^{26}$ sec $= 10^{19}$ years

Now consider the case of N Tubulin Dimers in Coherent Superposition connected by the Bohm Quantum Potential Force that does not fall off with distance.

Jack Sarfatti defines coherence length L by $L^3 = N a^3$ so that the Superposition Energy E_N of N superposed Conformation Electrons is

 $E_N = G M^2 / L = N^{(5/3)} E_{ssediff}$

The decoherence time for the system of N Tubulin Electrons is

T_N = h / E_N = h / N^(5/3) E_ssediff = N^(-5/3) 10^26 sec

so we have the following rough approximate Decoherence Times T_N

```
Number of Involved
                                      Time
  Tubulin Dimers
                                      ΤΝ
10^{(11+9)} = 10^{20} 10^{(-33 + 26)} = 10^{(-7)} sec
                                                           10^11 neurons
                                                                х
                                                           10^9 TD / neuron
                                                                _
                                                           10^20 Tubuin Dimers
                                                               in Human Brain
10^16
                     10^{(-27 + 26)} = 10^{(-1)} \sec - 10 Hz
                           Human Alpha EEG is 8 to 13 Hz
                     Fundamental Schumann Resonance is 7.8 Hz
     Time of Traverse by a String World-Line Quantum Bohmion of a Quantum
     Consciousness Hamiltonian Circuit of 10^16 TD separated from nearest
     neighbors by 10 nm is 10^{16} \times 10 nm / c = (10^{16} \times 10^{(-6)}) cm / c =
                             = 10^{10} \text{ cm} / \text{ c} = 0.3 \text{ sec}
```

Condensate Structure of Higgs and Spacetime

"... The Nambu Jona-Lasinio model ...

is a theory of Dirac particles with a local 4-fermion interaction and, as such, it belongs to the same class of effective theories as the BCS theory of superconducting metals ... the Nambu Jona-Lasinio model has very recently been applied to the standard model. In this application the Higgs meson is a ttbar top quark mass excitation ...".

(from Nambu Jona-Lasinio Models Applied to Dense Hadronic Matter, by Georges Ripka, in a Workshop on Nuclear Physics, Iguazu Falls, 28 Aug - 1 Sep 1989)

As to the Higgs in the E8 physics model (viXra 1602.0319), consider a generalized Nambu Jona-Lasinio model in which the Higgs is a Fermion-AntiFermion condensate. As the most massive fermion, the Truth Quark - AntiQuark pairs would be so dominant that the Higgs could be effectively considered as a condensate of Truth Quark - Truth AntiQuark pairs but the detailed picture would be as a condensate of Fermion - Anti-Fermion pairs where there are 24 types of Fermions, each Quark coming in color R, G, or B:

> E-Neutrino and Electron Down Quark (R, G, B) and Up Quark (R, G, B) M-Neutrino and Muon Strange Quark (R, G, B) and Charm Quark (R, G, B) T-Neutrino and Tauon Beauty Quark (R, G, B) and Truth Quark (R, G, B)

so that there are $24 \times 24 = 576$ Fermion-AntiFermion pairs for each Higgs and each Higgs can be in Bohm Quantum Resonance with 24×24 Bohm Quantum String states: dilaton; antisymmetric Planck-cell group; and symmetric Bohm Quantum Potential.

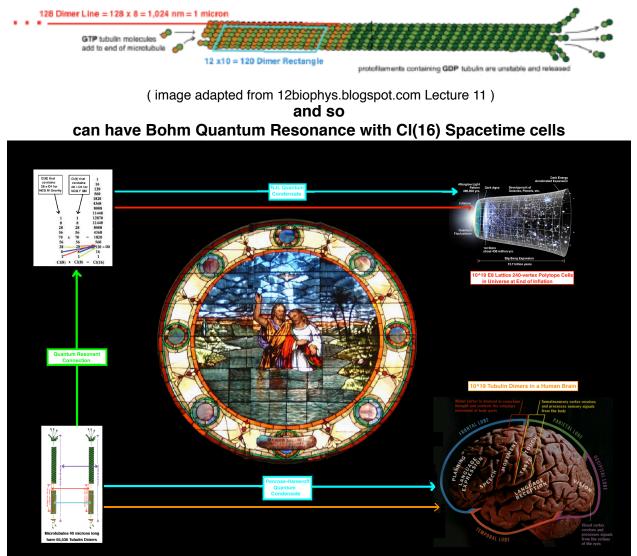
As to Spacetime in the E8 physics model (viXra 1602.0319), consider a generalized Nambu Jona-Lasinio model in which 8-dim Classical Lagrangian Spacetime is a condensate of Geoffrey Dixon's 64-dim Particle spinor T = RxCxHxO = Real x Complex x Quaternion x Octonion and its corresponding 64-dim AntiParticle spinor Tbar. The T - Tbar pairs of the condensate form the 128-dim part of E8 that lives in the Cl(16) Real Clifford Algebra as

248-dim E8 = 120-dim bivector D8 + 128-dim half-spinor D8

By Triality, the D8 / D4xD4 = 64-dim part of E8 representing Spacetime is equivalent to T and Tbar, with T representing Fermions and Tbar representing AntiFermions.

Each cell of E8 Classical Lagrangian Spacetime corresponds to 65,536-dim Cl(16) which contains 248-dim E8 = 120-dim D8 bivectors +128-dim D8 half-spinors

Human Brain Microtubules 40 microns long have 65,536 Tubulin Dimers



(image from Wikipedia and Time)

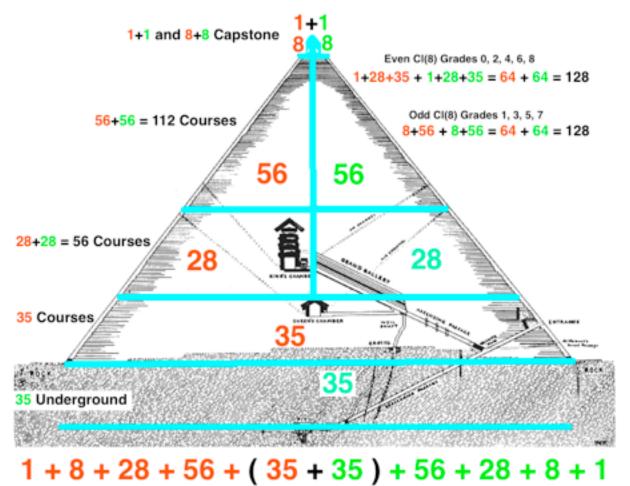
so that at any and all Times the State of Consciousness of a Human is in exact resonant correspondence with a subset of the cells of E8 Classical Lagrangian Spacetime

Therefore

E8 Classical Lagrangian Spacetime NJL Condensate is effectively the **Spirit World** in which the **Human States of Consciousness = Souls exist.**

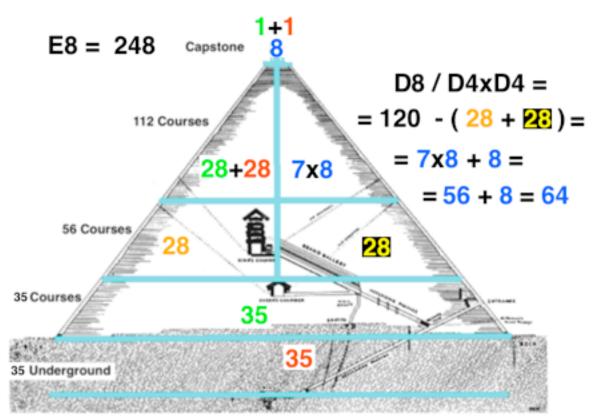
After the death of the Human Physical Body the Spirit World interactions with its Soul are no longer constrained by Physical World interactions with its Body so that the Spirit World can harmonize the individual Soul with the collective Universal Soul by the process of Gehinnom whereby the Soul is prepared for Gan Eden.

Clifford Algebras were not known to European mathematicians until Clifford in the 19th century and not known to European physicists until Dirac in the 20th century but it seems to me that their structure was known to Africans in ancient times. For example, the courses of the Great Pyramid of Giza correspond to the graded structure of Cl(8):

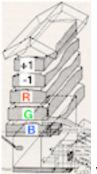


(image adapted from David Davidson image - for larger size see tony5m17h.net/GreatPyrCl8.png)

248-dim E8 (like 256-dim Cl(8)) can also be seen in terms of the Great Pyramid (the 8-dim difference is related to the Cl(8) Primitive Idempotent and the Higgs).



E8 / D8 = 248 - 120 = 128 = 64 + 64



The **28** is in the area of the Upper Chamber which has 5 slabs that represent the 5 charges (+1,-1 electric and R,G,B color) of the Standard Model.

The is in the area of the Grand Gallery which rises at a slope of about 26 degrees, or about half of the Golden Ratio slope of the Great Pyramid which is $\operatorname{arccosine}(1 / ((1 + \operatorname{sqrt}(5))/2)) = 51.8$ degrees. The Grand Gallery could represent a segment of a space-time path (World-Line) in the context of Conformal Gravity

E8 Root Vectors and Geometry of E8 Physics

Frank Dodd (Tony) Smith, Jr. - 2016 - viXra 1602.0319

Abstract - Introduction

This paper describes a research program based on the 240 E8 Root Vectors encoding the basic structure of a Unified Theory of Fundamental Physics by forming a local classical Lagrangian for the Standard Model plus Gravity and Dark Energy.

The Root Vectors know where they belong in the Lagrangian because of their place in the geometric structure of E8 and its related symmetric spaces such as: E8 / D8 = 128-dim (OxO)P2 E8 / E7 x SU(2) = 112-dim set of (QxO)P2 in (OxO)P2 D8 / D4 x D4 = 64-dim Gr(8,16)

Embedding E8 local classical Lagrangian into Cl(0,16) Clifford Algebra and taking the completion of the union of all tensor products of all the Cl(0,16)s produces a generalization of hyperfinite II1 von Neumann factor fermionic Fock space forming a global AQFT describing spacetime, the Standard Model, and Gravity with Dark Energy. The structure is related to unconventional 26D String Theory by

 $CI(0,16) \rightarrow CI(0,16)xCI(0,8) = CI(0,24) \rightarrow M(2,CI(0,24)) = CI(1,25)$ Completion of Union of All Tensor Products of CI(1,25) = 2x2 matrices of CI(0,24) is the String Theory formulation of the hyperfinite AQFT.

The Physics model described herein may be called the Cl(1,25) E8 Physics Model, since the Cl(1,25) of 26D String Theory contains Cl(0,16) which contains E8 whose root vectors describe a Lagrangian for the Standard Model and Gravity + Dark Energy.

The main body of the paper describes physical interpretations of the 240 Root Vectors with a rough qualitative description of how they are used in setting up calculations of force strengths, particle masses, Dark Energy : Dark Matter : Ordinary Matter ratios, Kobayashi-Maskawa parameters, etc.

The main body of the paper (46 pages) concludes with a summary of the results of those calculations. Details of the calculations, some related experimental results, etc, are given in a more lengthy set of appendices (336 pages).

This latest (August 2016) version includes LHC results of about 13 /fb of 2016 run, including Higgs -> ZZ -> 4I channel events relevant to the existence of two Higgs mass states predicted by E8 Physics beyond the conventional 125 GeV state.

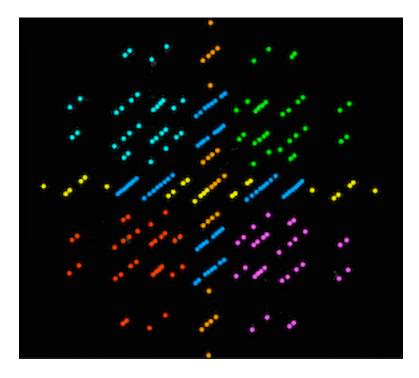
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E8 Root Vectors and Maximal SubGroups

248-dim Lie Group E8 has 240 Root Vectors arranged on a 7-sphere S7 in 8-dim space.

Since it is hard to visualize points on S7 in 8-dim space, I prefer to represent the 240 E8 Root Vectors in 2-dim / 3-dim space as



To understand the Geometry related to the 240 E8 Root Vectors, consider that

248-dim E8 = 120-dim Spin(16) D8 + 128-dim half-spinor of Spin(16) D8

and

240 E8 Root Vectors = 112 D8 Root Vectors + 128 D8 half-spinors

and

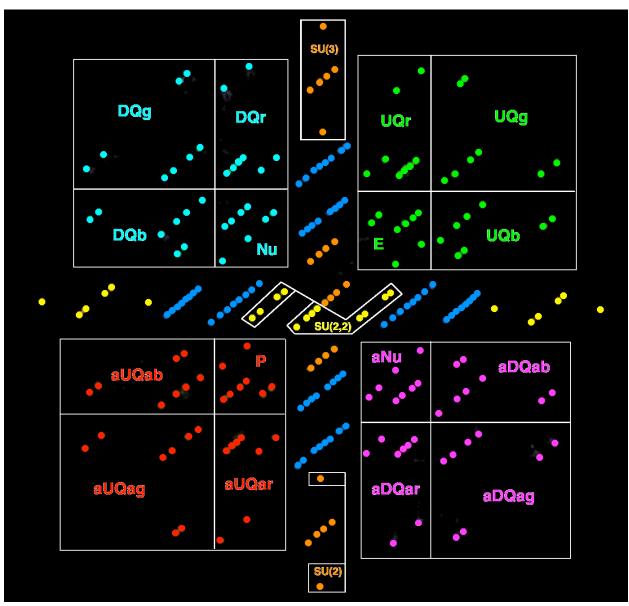
there are two ways to see a maximal symmetric subspace of E8 and E8 Root Vectors:

the symmetric space corresponding to the 128 D8 half-spinors

E8 / D8 = 128-dim Octonion-Octonionic Projective Plane (OxO)P2 and the symmetric space corresponding to the 112 D8 Root Vectors

> **E8 / E7 x SU(2) = 112-dim set of (QxO)P2 in OxO)P2** where (QxO)P2 = Quaternion-Octonion Projective Planes

Geometric Structure leads to physical interpretation of the E8 Root Vectors as:



E = electron, UQr = red up quark, UQg = green up quark, UQb = blue up quark Nu = neutrino, DQr = red down quark, DQg = green down quark, DQb = blue down quark P = positron, aUQar = anti-red up antiquark, aUQag = anti-green up antiquark, aUQab = anti-blue up antiquark aNu = antineutrino, aDQar = anti-red down antiquark, aDQag = anti-green down antiquark, aDQab = anti-blue down antiquark

Each Lepton and Quark has 8 components with respect to 4+4 dim Kaluza-Klein 6 orange SU(3) and 2 orange SU(2) represent Standard Model root vectors 24-6-2 = 16 orange represent U(2,2) Conformal Gravity Ghosts 12 yellow SU(2,2) represent Conformal Gravity SU(2,2) root vectors 24-12 = 12 yellow represent Standard Model Ghosts 32+32 = 64 blue represent 4+4 dim Kaluza-Klein spacetime position and momentum

Octonionic D8 and Spinor Fermions and Coleman-Mandula

First consider the symmetric space corresponding to the 128 D8 half-spinors

E8 / D8 = 128-dim Octonion-Octonionic Projective Plane (OxO)P2

These are the 128 (OxO)P2 half-spinor E8 Root Vectors on a S7 in 8-dim space:

Since D8 Spin(16) is the local isotropy group of E8 / D8 = (OxO)P2the 128 = 64+64 = 8x8 + 8x8 half-spinor Root Vectors have Octonionic Symmetry and can represent

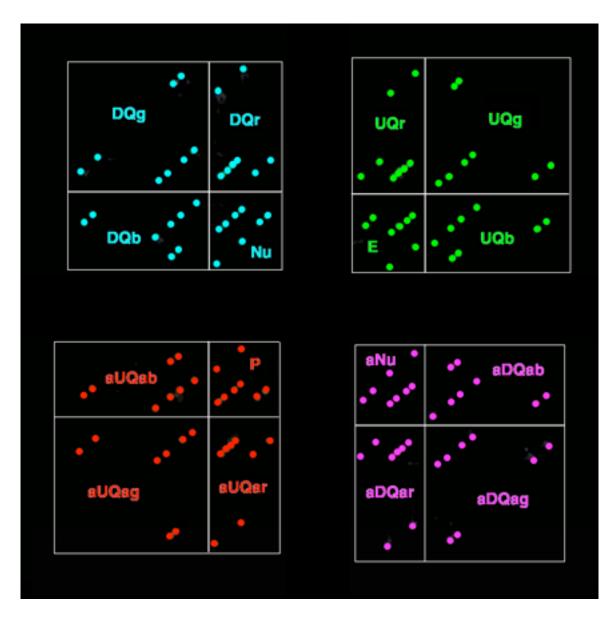
8 components of 8 Generation-1 Fermion Particles (green/cyan dots) plus

8 components of 8 Generation-1 Fermion AntiParticles (red/magenta dots)

Fermion Types are represented by Octonion Basis Elements:

- 1 Neutrino
- i Red Down Quark
- j Green Down Quark
- k Blue Down Quark
- E Electron
- I Red Up Quark
- J Green Up Quark
- K Blue Up Quark

In this view, the physical interpretation of the 128 Fermion Root Vectors is

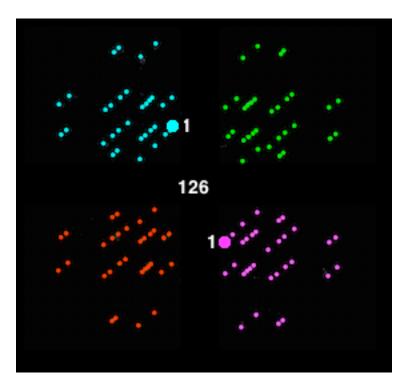


The Octonionic 8 Gen-1 Fermion Particles and 8 Gen-1 Fermion AntiParticles have Lorentz structure of spinor representations for 8-dim Spin(1,7) spacetime (since D8 = Cl(16) = Cl(8) x Cl(8) by 8-Periodicity and Cl(1,7) = Cl(0,8) = M(16,R) = 16x16 Real Matrix Algebra) and therefore satisfy the Coleman-Mandula Theorem (see Appendix - Details of Coleman-Mandula)

Creation-Annihilation Operators for the 8 components of the 8+8 Fermions are the odd-grade-+/-1 part of the E8 Maximal Contraction generalized Heisenberg Algebra h92 x A7 = 28 + 64 + ((SL(8,R)+1) + 64 + 28 (see Rutwig Campoamor-Stursberg in "Contractions of Exceptional Lie Algebras and SemiDirect Products" (Acta Physica Polonica B 41 (2010) 53-77)

Quaternionic E7 and SU(2)

E8 Root Vectors for Timelike Neutrino (the cyan dot at 1) and Timelike AntiNeutrino (the magenta dot at another 1) are an antipodal pair



so that the other 128 - 1 - 1 = 126 Root Vectors project non-trivially (i.e., off-origin) to the 7-dim Coxeter Reflection hyperplane that is perpendicular to that antipodal axis. **The cyan 1 Neutrino T-component and the magenta 1 AntiNeutrino T-component are Root Vectors of 3-dim SU(2)**

and

126 Root Vectors reflected in 7-dim hyperplane are Root Vectors of 133-dim E7

Since Neutrinos and AntiNeutrinos are fundamentally tree-level massless and therefore Left-Handed and Right-Handed respectively and since the SU(2) of the fermionic E7 x SU(2) maximal compact subgroup of E8

corresponds to the Timelike Neutrino and the Timelike AntiNeutrino and

since the SU(2) of E7 x SU(2) connects fermions to the ElectroWeak SU(2) that lives in the Standard Model Gauge Group D4 and in CP2 = SU(3) / SU(2)xU(1) the ElectroWeak SU(2) violates Parity,

coupling to Left-Handed Fermion Particles

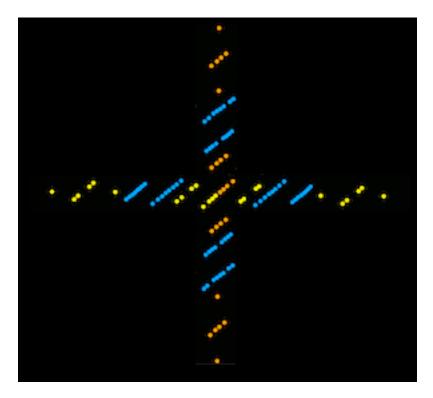
therefore

it is natural to consider the symmetric space corresponding to the 112 D8 Root Vectors **E8 / E7 x SU(2) = 112-dim set of (QxO)P2 in (OxO)P2**

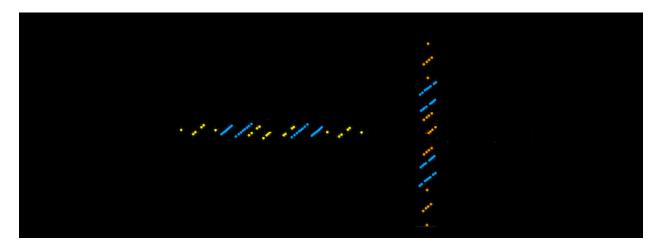
Since E7 x SU(2) is its local isotropy group

E8 Physics Structures of the 112 D8 Root Vectors have Quaternionic Symmetry

These are the 112 (QxO)P2 half-spinor E8 Root Vectors on a S7 in 8-dim space:



The 112 fall naturally into two sets of 56:



24 yellow / 32 blue horizontal 56 give D4 of Conformal Gravity / M4 of 4+4 Kaluza-Klein and 24 orange / 32 blue vertical 56 give D4 of Standard Model / CP2 of 4+4 Kaluza-Klein

Spacetime, Unimodular Gravity, and Strong CP



The 32+32 = 64 blue **Control of the** 64-dim symmetric space D8 / D4 x D4 = Gr(8,16) Grassmannian = set of RP7 in RP15

Creation-Annihilation Operators for 8-dim spacetime x 8-dim momentum space are the 64-dim grade-0 part of the E8 Maximal Contraction generalized Heisenberg Algebra $h92 \times A7 = 28 + 64 + ((SL(8,R)+1) + 64 + 28)$

Unimodular SL(8,R) Gravity effectively describes a generalized checkerboard of 8-dim SpaceTime HyperVolume Elements and, with respect to Cl(16) = Cl(8)xCl(8), is the tensor product of the two 8v vector spaces of the two Cl(8) factors of Cl(16). If those two Cl(8) factors are regarded as Fourier Duals, then **8v x 8v describes Position x Momentum in 8-dim SpaceTime**.

Bradonjic and Stachel in arXiv 1110.2159 said: "... in ... Unimodular relativity ... the metric tensor ... break[s up] ... into the conformal structure represented by a conformal metric ... with det = -1 and a four-volume element ... at each point of space-time ... [that]... may be the remnant, in the ... continuum limit, of a more fundamental discrete

quantum structure of space-time itself ...". Conformal Spin(2,4) = SU(2,2) Gravity and Unimodular SL(4,R) = Spin(3,3) Gravity

seem to be effectively equivalent. Padilla and Saltas in arXiv 1409.3573 said: "... classical unimodular gravity and classical GR are the same thing, and they can be extended into the UV such that the equivalence is maintained. ...

Classical unimodular gravity = classical GR. ...

Quantum unimodular gravity = quantum GR provided we make certain assumptions about how we extend into the UV. ...".

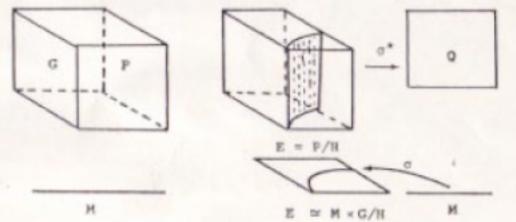
Frampton, Ng, and Van Dam in J. Math. Phys. 33 (1992) 3881-3882 said: "... Because of the existence of topologically nontrivial solutions, instantons, of the classical field equations associated with quantum chromodynamics (QCD), the quantized theory contains a dimensionless parameter \emptyset ($0 < \emptyset < 2\pi$) not explicit in the classical lagrangian. Since \emptyset multiplies an expression odd in CP, **QCD predicts** violation of ... CP ... symmetry unless the phase \emptyset takes one of the special values ... 0 (mod π) ... this fine tuning is the strong CP problem ... the quantum dynamics of ... unimodular gravity ... may lead to the relaxation of \emptyset to $\emptyset = 0$ (mod π) without the need ... for a new particle ... such as the axion ...".

Higgs and 3-state Higgs-Tquark Sysytem

Quaternionic E7xSU(2) structure breaks 8-dim Spacetime Octonionic Symmetry to Quaternionic (4+4)-dim Associative x CoAssociative Kaluza-Klein Spacetime

(see Reese Harvey "Spinors and Calibrations" (Academic 1990)) where M4 = 4-dim Minkowski Physical Spacetime is Associative and CP2 = SU(3) / SU(2) x U(1) Internal Symmetry Space is CoAssociative

Meinhard Mayer said (Hadronic Journal 4 (1981) 108-152): "... each point of ... the ... fibre bundle ... E ...



... consists of

a four- dimensional spacetime point x [in M4]

to which is attached the homogeneous space G / H [SU(3) / U(2) = CP2]

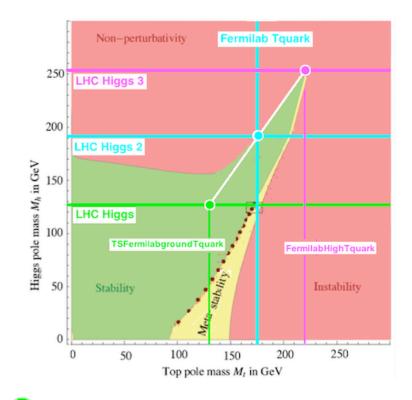
• • •

the components of the curvature lying in the homogeneous space G / H could be reinterpreted as Higgs scalars (with respect to spacetime [M4])

the Yang-Mills action reduces to a Yang-Mills action for the h-components [U(2) components] of the curvature over M [M4] and a quartic functional for the "Higgs scalars", which not only reproduces the Ginzburg-Landau potential, but also gives the correct relative sign of the constants, required for the BEHK ... Brout-Englert-Higgs-Kibble ... mechanism to work. ...".

(see Appendix - Details of Mayer - Higgs)

The Cl(1,25) E8 model identifies the Higgs with Primitive Idempotents of the Cl(8) real Clifford algebra, whereby the Higgs is not seen as a simple-minded single fundamental scalar particle, but rather the Higgs is seen as a quantum process that creates a fermionic condensate and effectively a 3-state Higgs-Tquark System.



The Green Dot - where the White Line originates in our Ordinary Phase is the low-mass state of a 130 GeV Truth Quark and a 125 GeV Higgs.

The Cyan Dot where the White Line hits the Triviality Boundary leaving the Ordinary Phase is the middle-mass state of a 174 GeV Truth Quark and Higgs around 200 GeV. It corresponds to the Higgs mass calculated by Hashimoto, Tanabashi, and Yamawaki in hep-ph/0311165 where they say: "... We perform the most attractive channel (MAC) analysis in the top mode standard model with TeV-scale extra dimensions, where the standard model gauge bosons and the third generation of quarks and leptons are put in D(=6,8,10,...) dimensions. In such a model, bulk gauge couplings rapidly grow in the ultraviolet region. In order to make the scenario viable, only the attractive force of the top condensate should exceed the critical coupling, while other channels such as the bottom and tau condensates should not. We then find that the top condensate can be the MAC for D=8 ... We predict masses of the top (m_t) and the Higgs (m_H) ... based on the renormalization group for the top Yukawa and Higgs guartic couplings with the compositeness conditions at the scale where the bulk top condenses ... for ... [Kaluza-Klein type]... dimension... D=8 ...

m_t = 172-175 GeV and m_H=176-188 GeV ...".

As to composite Higgs and the Triviality boundary, Pierre Ramond says in his book Journeys Beyond the Standard Model (Perseus Books 1999) at pages 175-176: "... The Higgs quartic coupling has a complicated scale dependence. It evolves according to d lambda / d t = ($1 / 16 pi^2$) beta_lambda where the one loop contribution is given by beta_lambda = $12 lambda^2 - ... - 4 H ...$ The value of lambda at low energies is related [to] the physical value of the Higgs mass according to the tree level formula m_H = v sqrt(2 lambda) while the vacuum value is determined by the Fermi constant ... for a fixed vacuum value v, let us assume that the Higgs mass and therefore lambda is large. In that case, beta_lambda is dominated by the lambda^2 term, which drives the coupling towards its Landau pole at higher energies. Hence the higher the Higgs mass, the higher lambda is and the close[r] the Landau pole to experimentally accessible regions.

This means that for a given (large) Higgs mass, we expect the standard model to enter a strong coupling regime at relatively low energies, losing in the process our ability to calculate. This does not necessarily mean that the theory is incomplete,

only that we can no longer handle it ... it is natural to think that this effect is caused by new strong interactions, and that the Higgs actually is a composite ...

The resulting bound on lambda is sometimes called the triviality bound.

The reason for this unfortunate name (the theory is anything but trivial)

stems from lattice studies where the coupling is assumed to be finite everywhere;

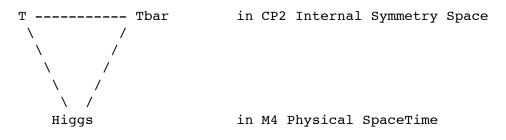
in that case the coupling is driven to zero, yielding in fact a trivial theory.

In the standard model lambda is certainly not zero. ...".

Middle Mass State Cross Section:

In the CI(1,25) E8 model, the Middle-Mass Higgs has structure that is not restricted to Effective M4 Spacetime as is the case with the Low-Mass Higgs Ground State

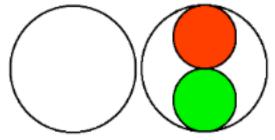
but extends to the full 4+4 = 8-dim structure of M4xCP2 Kaluza-Klein.



Therefore the Mid-Mass Higgs looks like a 3-particle system of Higgs + T + Tbar.

The T and Tbar form a Pion-like state. Since Tquark Mid-Mass State is 174 GeV the Middle-Mass T-Tbar that lives in the CP2 part of (4+4)-dim Kaluza-Klein has mass (174+174) x (135 / (312+312) = 75 GeV. The Higgs that lives in the M4 part of (4+4)-dim Kaluza-Klein has, by itself, its Low-Mass Ground State Effective Mass of 125 GeV. So, the total Mid-Mass Higgs lives in full 8-dim Kaluza-Klein with mass 75+125 = 200 GeV.

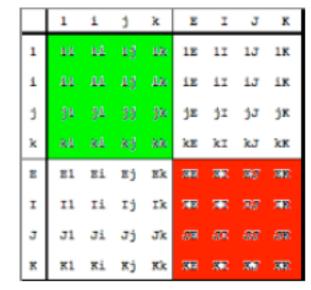
This is consistent with the Mid-Mass States of the Higgs and Tquark being on the Triviality Boundary of the Higgs - Tquark System and with the 8-dim Kaluza-Klein model in hep-ph/0311165 by Hashimoto, Tanabashi, and Yamawaki.As to the cross-section of the Middle-Mass Higgs



consider that the entire Ground State cross-section lives only in 4-dim M4 spacetime (left white circle)

while the Middle-Mass Higgs cross-section lives in full 4+4 = 8-dim Kaluza-Klein (right circle with red area only in CP2 ISS and white area partly in CP2 ISS with only green area effectively living in 4-dim M4 spacetime) so that

our 4-dim M4 Physical Spacetime experiments only see for the Middle-Mass Higgs a cross-section that is 25% of the full Ground State cross-section.



The 25% may also be visualized in terms of 8-dim coordinates {1,i,j,k,E,I,J,K}

in which {1,i,j,k} represent M4 and {E,I,J,K} represent CP2.

The Magenta Dot at the end of the White Line is the high-mass state of a 220 GeV Truth Quark and a 240 GeV Higgs. It is at the critical point of the Higgs-Tquark System with respect to Vacuum Instability and Triviality. It corresponds to the description in hep-ph/9603293 by Koichi Yamawaki of the Bardeen-Hill-Lindner model: "... the BHL formulation of the top quark condensate ... is based on the RG equation combined with the compositeness condition ... start[s] with the SM Lagrangian which includes explicit Higgs field at the Lagrangian level ...

BHL is crucially based on the perturbative picture ...[which]... breaks down at high energy near the compositeness scale \land ...[10^19 GeV]...

there must be a certain matching scale \wedge _Matching such that

the perturbative picture (BHL) is valid for $mu < \Lambda$ _Matching, while only the nonperturbative picture (MTY) becomes consistent for $mu > \Lambda$ _Matching ...

However, thanks to the presence of a quasi-infrared fixed point,

BHL prediction is numerically quite stable against ambiguity at high energy region, namely, rather independent of whether this high energy region is replaced by MTY or something else. ... Then we expect mt = mt(BHL) = ... = 1/(sqrt(2)) ybart v within 1-2%, where ybart is the quasi-infrared fixed point given by Beta(ybart) = 0 in ... the one-loop RG equation ...

The composite Higgs loop changes ybart^2 by roughly the factor Nc/(Nc +3/2) = 2/3 compared with the MTY value, i.e., 250 GeV -> 250 x sqrt(2/3) = 204 GeV, while the electroweak gauge boson loop with opposite sign pulls it back a little bit to a higher value. The BHL value is then given by mt = 218 +/- 3 GeV, at Λ = 10^19 GeV. The Higgs boson was predicted as a tbar-t bound state

with a mass MH = 2mt based on the pure NJL model calculation.

Its mass was also calculated by BHL through the full RG equation \ldots

the result being ... MH / mt = 1.1) at /.\ = 10^19 GeV ...

... the top guark condensate proposed by Miransky, Tanabashi and Yamawaki (MTY) and by Nambu independently ... entirely replaces the standard Higgs doublet by a composite one formed by a strongly coupled short range dynamics (four-fermion interaction) which triggers the top guark condensate. The Higgs boson emerges as a tbar-t bound state and hence is deeply connected with the top guark itself. ... MTY introduced explicit four-fermion interactions responsible for the top quark condensate in addition to the standard gauge couplings. Based on the explicit solution of the ladder SD equation, MTY found that even if all the dimensionless four-fermion couplings are of O(1), only the coupling larger than the critical coupling yields non-zero (large) mass ... The model was further formulated in an elegant fashion by Bardeen, Hill and Lindner (BHL) in the SM language, based on the RG equation and the compositenes condition. BHL essentially incorporates 1/Nc sub-leading effects such as those of the composite Higgs loops and ... gauge boson loops which were disregarded by the MTY formulation. We can explicitly see that BHL is in fact equivalent to MTY at 1/Nc-leading order. Such effects turned out to reduce the above MTY value 250 GeV down to 220 GeV ...".

High Mass State Cross Section:

As with the Middle-Mass Higgs,

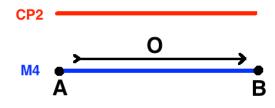
the High-Mass Higgs lives in all 4+4 = 8 Kaluza-Klein dimensions so

its cross-section is also about 25% of the Higgs Ground State cross-section.

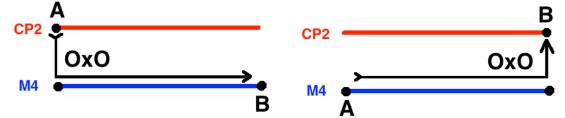
3 Generations of Fermions

In Kaluza-Klein M4 x CP2 there are 3 possibilities for a fermion represented by an Octonion O basis element to go from point A to point B:

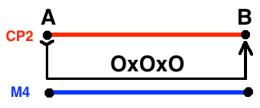
1 - A and B are both in M4: First Generation Fermion whose path can be represented by the single O basis element so that First Generation Fermions are represented by Octonions O.



2 - Either A or B, but not both, is in CP2: Second Generation Fermion whose path must be augmented by one projection from CP2 to M4, which projection can be represented by a second O basis element so that Second Generation Fermions are represented by Octonion Pairs OxO.



3 - Both A and B are in CP2: Third Generation Fermion whose path must be augmented by two projections from CP2 to M4, which projections can be represented by a second O and a third O, so that Third Generation Fermions are represented by Octonion Triples OxOxO.



D4 of Standard Model Gauge Bosons and Gravity Ghosts



The 24 orange are Root Vectors of the CP2-related D4 local isotropy group in the symmetric space D8 / D4 x D4 that acts on the CP2 Internal Symmetry Space of Kaluza-Klein M4 x CP2

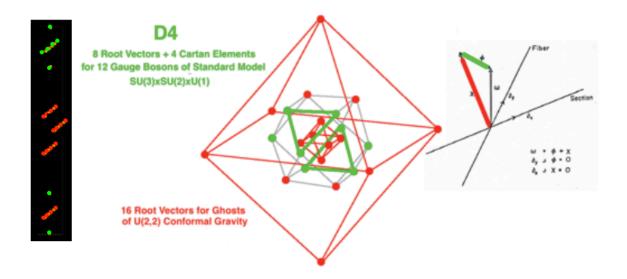
8 orange are Root Vectors for Standard Model SU(3) x SU(2) x U(1) which have 2+1+1 = 4 Cartan SubAlgebra dimensions.

Standard Model Gauge groups come from CP2 = SU(3) / SU(2) x U(1) (as described by Batakis in Class. Quantum Grav. 3 (1986) L99-L105)

Electroweak SU(2) x U(1) is gauge group as isotropy group of CP2.

SU(3) is global symmetry group of CP2 but due to Kaluza-Klein structure of compact CP2 at every M4 spacetime point, it acts as Color gauge group with respect to M4.

The 24-8 = 16 D4 of CP2 Root Vectors represent Ghosts of U(2,2) Conformal Gravity.



Jean Thierry-Mieg in J. Math. Phys. 21 (1980) 2834-2838 said: "... The ghost and the gauge field:

The single lines represent a local coordinate system

of a principal fiber bundle of base space-time.

The double lines are 1 forms.

The connection of the principle bundle w is assumed to be vertical.

Its contravariant components PHI and X are recognized, respectively,

as the Yang-Mills gauge field and the Faddeev-Popov ghost form ...".

D4 of Conformal Gravity and Standard Model Ghosts



are Root Vectors of

the M4-related D4 local isotropy group in the symmetric space D8 / D4 x D4 that acts on the M4 Internal Symmetry Space of Kaluza-Klein M4 x CP2

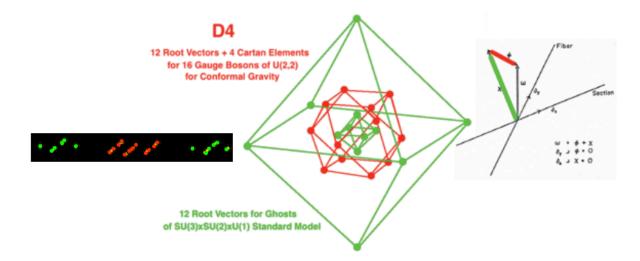
12 yellow are Root Vectors for Conformal Gravity U(2,2) which has 4 Cartan SubAlgebra dimensions.

Gravity and Dark Energy come from its Conformal Subgroup SU(2,2) = Spin(2,4) (see Appendix - Details of Conformal Gravity and ratio DE : DM :OM)

SU(2,2) = Spin(2,4) has 15 generators:

- 1 Dilation representing Higgs Ordinary Matter
- 4 Translations representing Primordial Black Hole Dark Matter
- 10 = 4 Special Conformal + 6 Lorentz representing Dark Energy (see Irving Ezra Segal, "Mathematical Cosmology and Extragalactic Astronomy" (Academic 1976))

The basic ratio Dark Energy : Dark Matter : Ordinary Matter = 10:4:1 = 0.67: 0.27: 0.06When the dynamics of our expanding universe are taken into account, the ratio is calculated to be **0.75: 0.21: 0.04** The 24-12 = 12 D4 of M4 Root Vectors represent Standard Model Ghosts



Jean Thierry-Mieg in J. Math. Phys. 21 (1980) 2834-2838 said:

"... The ghost and the gauge field:

The single lines represent a local coordinate system

of a principal fiber bundle of base space-time.

The double lines are 1 forms.

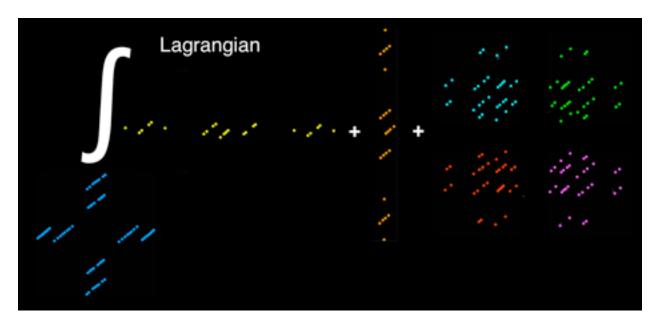
The connection of the principle bundle w is assumed to be vertical.

Its contravariant components PHI and X are recognized, respectively,

as the Yang-Mills gauge field and the Faddeev-Popov ghost form ...".

E8 Physics Lagrangian

Using the E8 Root Vector structure as described above, it is natural to construct a Lagrangian density



having terms for

E8 / D8 Fermions (with Fermion Generations 2 and 3 from Quaternionic structure) and

D4 Standard Model Gauge Bosons and Gravity Ghosts

(see Appendix - Lagrangian Terms)

and

D4 Conformal Gravity Gauge Bosons and Standard Model Ghosts (see Appendix - Details of Conformal Gravity and ratio DE : DM : OM)

that is integrated over

D8 / D4xD4 (4+4)-dim M4 x CP2 Kaluza-Klein base manifold with Higgs from the Mayer mechanism (see Appendix - Details of Mayer - Higgs)

The E8 Lagrangian is Chiral because

E8 contains Cl(16) half-spinors (64+64) for a Fermion Generation but does not contain Cl(16) Fermion AntiGeneration half-spinors (64+64). Fermion +half-spinor Particles with high enough velocity are seen as left-handed. Fermion -half-spinor AntiParticles with high enough velocity are seen as right-handed.

The E8 Lagrangian obeys Spin-Statistics because

the CP2 part of M4xCP2 Kaluza-Klein has index structure Euler number 2+1 = 3 and Atiyah-Singer index -1/8 which is not the net number of generations because **CP2 has no spin structure but you can use a generalized spin structure** (Hawking and Pope (Phys. Lett. 73B (1978) 42-44))

to get (for integral m) the generalized CP2 index $n_R - n_L = (1/2) m (m+1)$

Prior to Dimensional Reduction: m = 1, $n_R - n_L = (1/2)x1x2 = 1$ for 1 generation

After Reduction to 4+4 Kaluza-Klein: m = 2, $n_R - n_L = (1/2)x2x3 = 1$ for 3 generations (see chapter "3 Generations of Fermions")

Hawking and Pope say: "Generalized Spin Structures in Quantum Gravity ...what happens in CP2 ... is a two-surface K which cannot be shrunk to zero. ... However, one could replace the electromagnetic field by

a Yang-Mills field whose group G had a double covering G~.

The fermion field would have to occur in representations which changed sign under the non-trivial element of the kernel of the projection \dots G~ -> G while the bosons would have to occur in representations which did not change sign \dots ".

For the E8 model gauge bosons are in the 28+28=56-dim D4 + D4 subalgebra of E8. D4 = SO(8) is the Hawking-Pope G which has double covering G~ = Spin(8).

The 8 fermion particles / antiparticles are D4 half-spinors represented within E8 by anti-commutators and so do change sign while

the 28 gauge bosons are D4 adjoint represented within E8 by commutators and so do not change sign.

E8 inherits from F4 the property whereby its Spinor Part need not be written as Commutators but can also be written in terms of Fermionic AntiCommutators. (see Appendix - E8 Fermionic AntiCommutators)

However, something fundamental remains missing at this stage:

The above Lagrangian is mostly Classical.

E8 Quantum Theory

A natural way to make a Quantum Theory is to consider E8 to be Local Classical and

to embed E8 into the real Clifford Algebra Cl(0,16) and

use 8-Periodicity to form the Completion of the Union of all Tensor Products of CI(0,16) which produces a natural realistic Algebraic Quantum Field Theory (AQFT).

(see Appendix - Spinor Growth, Octonion Inflation ended by Quaternions) The structure is related to unconventional 26D String Theory by

 $CI(0,16) \rightarrow CI(0,16) \times CI(0,8) = CI(0,24) \rightarrow M(2,CI(0,24)) = CI(1,25)$ where M(2,CI(0,24)) = 2x2 matrices with entries in CI(0,24) and x = tensor product.

Cl(0,24) contains the Vector Space of the 24-dim Leech Lattice \land 24 that is composed of 3 copies of E8 Lattices (2 being Integral Domains and 1 not Algebraically closed) Since all the matrix entries are Cl(0,24) = tensor product of 3 copies of Cl(0,8) 8-Periodicity allows formation of the tensor products of copies of Cl(1,25) and therefore the **Completion of Union of All Tensor Products of Cl(1,25)** which **is the String Theory formulation of the hyperfinite AQFT**

(see Appendix - Grothendieck Universe Quantum Theory and Code and Appendix - Details of World-Line String Bohm Quantum Theory) with Real / Octonionic structure inherited from Cl(0,8) and also Quaternionic structure due to Cl(1,25) = Cl(1,9)xCl(0,8)xCl(0,8) and Cl(1,9) = Cl(1,5) x Cl(0,4) = = Cl(2,4) x Cl(0,4) where the vector space of Cl(2,4) is 6-dim Conformal Spacetime (see "Clifford Algebras and the Classical Groups" by Ian Porteous and his Chapter 2 of "Lectures on Clifford (Geometric) Algebras and Applications")

The String Theory structure can also be formulated directly in the Root Vector picture using redundancy in the E8 description of Quantum States:

Fermion components carry 8-dim Spacetime information

so E8 / D8 = 8x8 + 8x8 can be reduced to 8+8

Spacetime position and momentum are redundant

so D8 / D4 x D4 = 8x8 can be reduced to 8

Gauge Bosons and Ghosts are redundant

so D4 x D4 = 28+28 can be reduced to 28 = 16 for Gravity + 12 for Standard Model

Elimination of Redundancy gives 8+8 + 8 + 28 = 52-dim F4 with 48 Root Vectors forming a 24-cell plus its dual 52-dim F4 has 26-dim smallest non-trivial representation which has structure of J(3,O)o = traceless part of 27-dim exceptional Jordan Algebra J(3,O) and is the minimal structure containing the basic information of E8 Physics.

so

E8 Physics Quantum Theory can be formulated in terms of 26-dim J(3,O)o.

The Cl(1,25) E8 AQFT inherits structure from the Cl(1,25) E8 Local Lagrangian

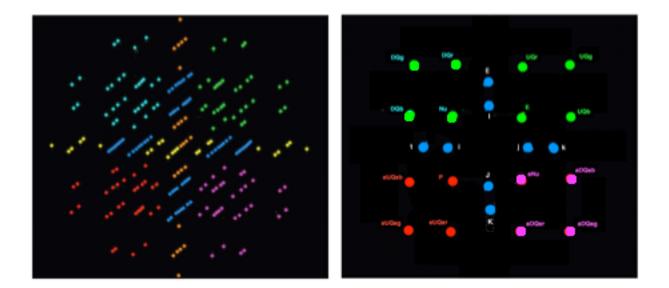
Gauge Gravity + Standard Model + Fermion Particle-AntiParticle 8-dim SpaceTime

whereby World-Lines of Particles are represented by Strings moving in a space whose dimensionality includes 8v = 8-dim SpaceTime Dimensions + + 8s+=8 Fermion Particle Types + 8s-=8 Fermion AntiParticle Types combined in the traceless part J(3,O)o of the 3x3 Octonion Hermitian Jordan Algebra

а	8s+	8v 8s-	
8s+*	b		
8v*	8s-*	-a-b	

which has total dimension 8v + 8s + 8s - 2 = 26 and is the space of a 26D String Theory with Strings seen as World-Lines.

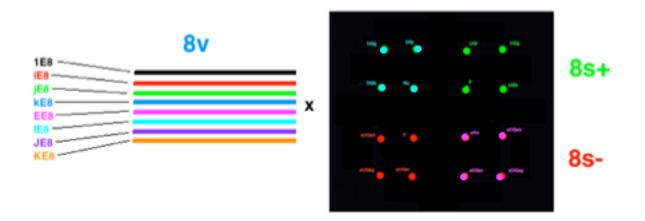
24 = 8v + 8s + 8s of the 26 dimensions of 26D String Theory correspond to 24x8 = 192 of the 240 E8 Root Vectors by representing the 8v + 8s + 8s as superpositions of their respective 8 components



8v SpaceTime is represented by D8 branes. A D8 brane has Planck-Scale Lattice Structure superpositions of 8 types of E8 Lattice denoted by 1E8, iE8, jE8, kE8, EE8, IE8, JE8, KE8



A single Snapshot of SpaceTime is represented by a D8 brane at each point of which is placed Fermion Particles or AntiParticles represented by 8+8 = 16 orbifolded dimensions of the 26 dimensions of 26D String Theory.



It is necessary to patch together SpaceTime Snapshots to form a Global Structure describing a Many-Worlds Global Algebraic Quantum Field Theory (AQFT) whose structure is described by Deutsch in "The Fabric of Reality" (Penguin 1997 pp. 276-283): "... there is no fundamental demarcation between snapshots of other times and snapshots of other universes ... Other times are just special cases of other universes ... Suppose ... we toss a coin ... Each point in the diagram represents one snapshot ... in the multiverse there are far too many snapshots for clock readings alone to locate a snapshot relative to the others. To do that, we need to consider the intricate detail of which snapshots determine which others. ...

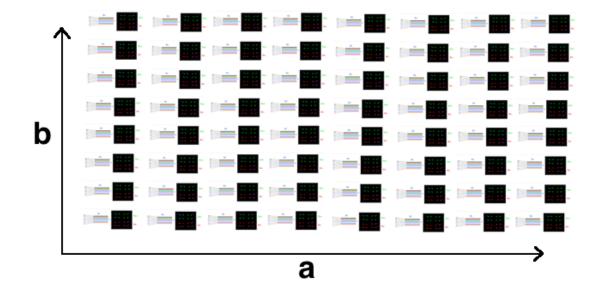
in some regions of the multiverse, and in some places in space,

the snapshots of some physical objects do fall, for a period, into chains,

each of whose members determines all the others to a good approximation ...".

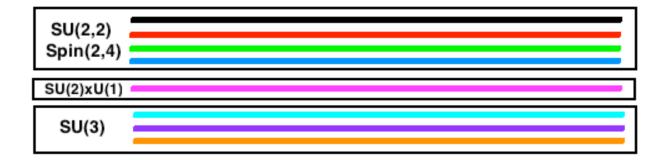
The Many-Worlds Snapshots are structured as a 26-dim Lorentz Leech Lattice

of 26D String Theory parameterized by the a and b of J(3,O)o as indicated in this 64-element subset of Snapshots



The 240 - 192 = 48 = 24+24 Root Vector Vertices of E8 that do not represent the 8-dim D8 brane or the 8+8 = 16 dim of Orbifolds for Fermions do represent the **Gauge Bosons (and their Ghosts) of E8 Physics**:

Gauge Bosons from 1E8, iE8, jE8, and kE8 parts of a D8 give U(2,2) Conformal Gravity Gauge Bosons from EE8 part of a D8 give U(2) Electroweak Force Gauge Bosons from IE8, JE8, and KE8 parts of a D8 give SU(3) Color Force



Each Deutsch chain of determination represents a World-Line of Particles / AntiParticles corresponding to a String of 26D String Theory such as the red line in this 64-element subset of Snapshots



26D String Theory is the Theory of Interactions of Strings = World-Lines.

Interactions of World-Lines can describe Quantum Theory

according to Andrew Gray (arXiv quant-ph/9712037):

"... probabilites are ... assigned to entire fine-grained histories ...

base[d] ... on the Feynman path integral formulation ...

The formulation is fully relativistic and applicable to multi-particle systems.

It ... makes the same experimental predictions as quantum field theory ...". Green, Schwartz, and Witten say in their book "Superstring Theory" vol. 1 (Cambridge 1986) "... For the ... closed ... bosonic string [**26D String Theory**] The first excited level ... consists of ... the ground state ... tachyon ... and ... a scalar ... 'dilaton' ... and ... SO(24) ... little group of a ...[26-dim]... massless particle ... and ... **a ... massless ... spin two state** ...".

Closed string tachyons localized at orbifolds of fermions produce virtual clouds of particles / antiparticles that dress fermions.

Dilatons are Goldstone bosons of spontaneously broken scale invariance that (analagous to Higgs) go from mediating a long-range scalar gravity-type force to the nonlocality of the Bohm-Sarfatti Quantum Potential.

The SO(24) little group is related to the Monster automorphism group that is the symmetry of each cell of Planck-scale local lattice structure.

The massless spin 2 state = Bohmion = Carrier of the Bohm Force of the Bohm Quantum Potential.

Roderick Sutherland (arXiv 1509.02442) gave a Lagrangian for the Bohm Potential saying: "... This paper focuses on interpretations of QM in which the underlying reality is taken to consist of particles have definite trajectories at all times ... An example ... is the Bohm model ... This paper ... provid[es]... a Lagrangian ...[for]... the unfolding events describing more than one particle while maintaining a relativistic description requires the introduction of final boundary conditions as well as initial, thereby entailing retrocausality ...

In addition ... the Lagrangian approach pursued here to describe particle trajectories also entails the natural inclusion of an accompanying field to influence the particle's motion away from classical mechanics and reproduce the correct quantum predictions. In so doing, it is ... providing a physical explanation for why quantum phenomena exist at all ... the particle is seen to be

the source of a field which alters the particle's trajectory via self-interaction ... The Dirac case ... each particle in an entangled many-particle state will be described by an individual Lagrangian density ... of the form:

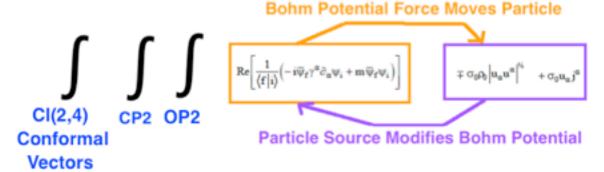
$$\mathfrak{L} = \operatorname{Re}\left[\frac{1}{\left\langle \mathbf{f} \left| i \right\rangle} \left(-i\overline{\psi}_{\mathbf{f}} \gamma^{\alpha} \partial_{\alpha} \psi_{i} + \mathbf{m} \overline{\psi}_{\mathbf{f}} \psi_{i} \right) \right] \mp \sigma_{0} \rho_{0} \left| \mathbf{u}_{\alpha} \mathbf{u}^{\alpha} \right|^{\frac{1}{2}} + \sigma_{0} \mathbf{u}_{\alpha} \mathbf{j}^{\alpha}$$

... the ... [first]... term ... [is]... the ... Lagrangian densities for the PSI field alone ...

... sigma_o is the rest density distribution of the particle through space ... j is the current density ...

... rho_o and u are the rest density and 4-velocity of the probability flow ...".

Jack Sarfatti extended the Sutherland Lagrangian to include Back-Reaction entanglement.



where a, b and VM4 form Cl(2,4) vectors and VCP2 forms CP2

and S+ and S- form OP2 so that

26D = 16D orbifolded fermions + 10D and 10D = 6D Conformal Space + 4D CP2 ISS (ISS = Internal Symmetry Space and 6D Conformal contains 4D M4 of Kaluza-Klein M4xCP2)

saying (linkedin.com Pulse 13 January 2016): "... the reason entanglement cannot be used as a direct messaging channel between subsystems of an entangled complex quantum system, is the lack of direct back-reaction of the classical particles and classical local gauge fields on their shared entangled Bohmian quantum information pilot wave ... Roderick. I. Sutherland ... using Lagrangian field theory, shows how to make the original 1952 Bohm pilot-wave theory completely relativistic,

and how to avoid the need for configuration space for many-particle entanglement. The trick is that final boundary conditions on the action

as well as initial boundary conditions influence what happens in the present.

The general theory is "post-quantum" ... and it is non-statistical ...

There is complete two-way action-reaction between quantum pilot waves and the classical particles and classical local gauge fields ...

orthodox statistical quantum theory, with no-signaling ...[is derived]... in two steps, first arbitrarily set the back-reaction (of particles and classical gauge field on their pilot waves) to zero. This is analogous to setting the curvature equal to zero in general relativity, or more precisely in setting G to zero.

Second, integrate out the final boundary information, thereby adding the statistical Born rule to the mix. ...

the mathematical condition for zero post-quantum back-reaction of particles and classical fields (aka "beables" J.S. Bell's term) is exactly de Broglie's guidance constraint. That is, in the simplest case, the classical particle velocity is proportional to the gradient of the phase of the quantum pilot wave. It is for this reason, that the independent existence of the classical beables can be ignored in most quantum calculations.

However, orthodox quantum theory assumes that the quantum system is thermodynamically closed between strong von Neumann projection measurements that obey the Born probability rule.

The new post-quantum theory in the equations of Sutherland, prior to taking the limit of orthodox quantum theory, should apply to pumped open dissipative structures. Living matter is the prime example. This is a clue that should not be ignored. ...".

Jack Sarfatti (email 31 January 2016) said: "... Sabine [Hossenfelder]'s argument ... "... two types of fundamental laws ... appear in contemporary theories.

One type is deterministic, which means that the past entirely predicts the future.

There is no free will in such a fundamental law because there is no freedom.

The other type of law we know appears in quantum mechanics and has an

indeterministic component which is random. This randomness cannot be influenced by anything, and in particular it cannot be influenced by you, whatever you think "you" are. There is no free will in such a fundamental law because there is no "will" - there is just some randomness sprinkled over the determinism.

In neither case do you have free will in any meaningful way."

... However ... [There is a Third Way]...

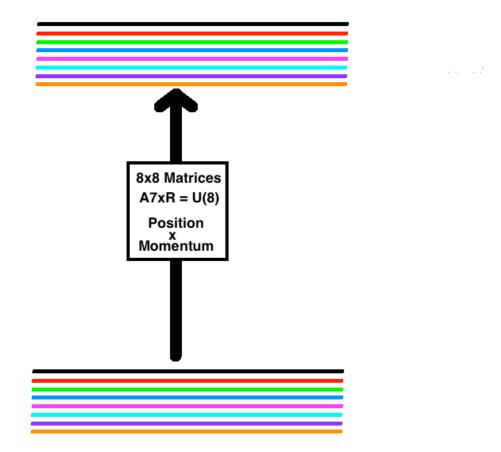
post-quantum theory with action-reaction between

quantum information pilot wave and its be-able is compatible with free will. ...".

The Creation-Annihilation Operator structure of the Bohm Quantum Potential of **26D String Theory** is given by the

 $\label{eq:main_state} \begin{array}{l} \mbox{Maximal Contraction of E8} = \mbox{semidirect product A7 x h92} \\ \mbox{where h92} = 92 + 1 + 92 = 185 - \mbox{dim Heisenberg algebra and A7} = 63 - \mbox{dim SL(8)} \\ \mbox{The Maximal E8 Contraction A7 x h92 can be written as a 5-Graded Lie Algebra} \\ & 28 + 64 + (SL(8,R) + 1) + 64 + 28 \\ & Central Even Grade 0 = SL(8,R) + 1 \\ \mbox{The 1 is a scalar and SL(8,R)} = \mbox{Spin(8)} + \mbox{Traceless Symmetric 8x8 Matrices,} \\ & so SL(8,R) \ \mbox{represents a local 8-dim SpaceTime in Polar Coordinates.} \\ & Odd \ \mbox{Grades -1 and } + 1 = 64 + 64 \\ \mbox{Each} = 64 = 8x8 = \mbox{Creation/Annihilation Operators for 8 components of 8 Fundamental Fermions.} \\ & Even \ \mbox{Grades -2 and } + 2 = 28 + 28 \\ \mbox{Each} = \mbox{Creation/Annihilation Operators for 28 Gauge Bosons of Gravity + Standard Model.} \\ \end{array}$

The 8x8 matrices linking one D8 to the next D8 of a World-Line String give A7xR = U(8) representing Position x Momentum



The Algebraic Quantum Field Theory (AQFT) structure of the Bohm Quantum Potential of 26D String Theory is given by the Cl(1,25) E8 Local Lagrangian

Gauge Gravity + Standard Model + Fermion Particle-AntiParticle 8-dim SpaceTime

and by 8-Periodicity of Real Clifford Algebras, as the Completion of the Union of all Tensor Products of the form

CI(1,25) x ...(N times tensor product)... x CI(1,25)

For $N = 2^8 = 256$ the copies of Cl(1,25) are on the 256 vertices of the 8-dim HyperCube



For $N = 2^{16} = 65,536 = 4^{8}$ the copies of Cl(1,25) fill in the 8-dim HyperCube as described by William Gilbert's web page: "... The n-bit reflected binary Gray code will describe a path on the edges of an n-dimensional cube that can be used as the initial stage of a Hilbert curve that will fill an n-dimensional cube. ...".

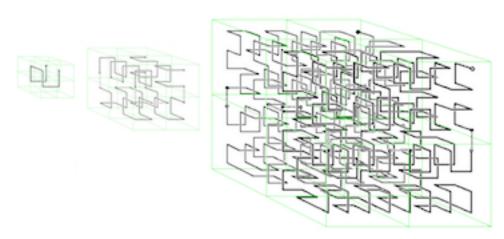
The vertices of the Hilbert curve are at the centers of the 2⁸ sub-8-HyperCubes whose edge lengths are 1/2 of the edge lengths of the original 8-dim HyperCube

As N grows, the copies of Cl(1,25) continue to fill the 8-dim HyperCube of E8 SpaceTime

using higher Hilbert curve stages from the 8-bit reflected binary Gray code subdividing the initial 8-dim HyperCube into more and more sub-HyperCubes.

If edges of sub-HyperCubes, equal to the distance between adjacent copies of Cl(1,25), remain constantly at the Planck Length, then the

full 8-dim HyperCube of our Universe expands as N grows to 2^16 and beyond similarly to the way shown by this 3-HyperCube example for N = 2^3, 4^3, 8^3 from Wiliam Gilbert's web page:



The Union of all Cl(1,25) tensor products is the Union of all subdivided 8-HyperCubes and

their Completion is a huge superposition of 8-HyperCube Continuous Volumes which Completion belongs to the Third Grothendieck Universe.

AQFT Quantum Code

Cerf and Adami in quantum-ph/9512022 describe virtual qubit-anti-qubit pairs (they call them ebit-anti-ebitpairs) that are related to negative conditional entropies for quantum entangled systems and are similar to fermion particle-antiparticle pairs. Therefore quantum information processes can be described by particle-antiparticle diagrams much like particle physics diagrams and **the Algebraic Quantum Field Theory of the Cl(1,25) E8 Physics Model should have a Quantum Code Information System** that is **based on structure of a unit cell in 26D String Theory** represented by **Real Clifford Algebra Cl(0,8) x Cl(0,8) x Cl(0,8) = Cl(0,24)** (see Appendix - Details of World-Line String Bohm Quantum Theory)

> Since Quantum Reed-Muller code [[256 , 0 , 24]] corresponds to Real Clifford Algebra Cl(0,8)

Tensor Product Quantum Reed-Muller code [[256 , 0 , 24]] x [[256 , 0 , 24]] x [[256 , 0 , 24]] corresponds to AQFT (Algebraic Quantum Field Theory) hyperfinite von Neumann factor algebra that is Completion of the Union of All Tensor Products of Cl(1.25)

Schwinger Sources, Hua Geometry, and Wyler Calculations

Fock "Fundamental of Quantum Mechanics" (1931) showed that it requires Linear Operators "... represented by a definite integral [of a]... kernel ... function ...".

Hua "Harmonic Analysis of Functions of Several Complex Variables in the Classical Domains" (1958) showed Kernel Functions for Complex Classical Domains.

Schwinger (1951 - see Schweber, PNAS 102, 7783-7788) "... introduced a description in terms of Green's functions, what Feynman had called propagators ... The Green's functions are vacuum expectation values of time-ordered Heisenberg operators, and the field theory can be defined non-perturbatively in terms of these functions ...[which]... gave deep structural insights into QFTs; in particular ... the structure of the Green's functions when their variables are analytically continued to complex values ...".

Wolf (J. Math. Mech 14 (1965) 1033-1047) showed that the Classical Domains (complete simply connected Riemannian symmetric spaces) representing 4-dim Spacetime with Quaternionic Structure are:

 $S1 \times S1 \times S1 \times S1 = 4 \text{ copies of } U(1)$ $S2 \times S2 = 2 \text{ copies of } SU(2)$ $CP2 = SU(3) / SU(2) \times U(1)$ S4 = Spin(5) / Spin(4) = Euclidean version of Spin(2,3) / Spin(1,3)

Armand Wyler (1971 - C. R. Acad. Sc. Paris, t. 271, 186-188) showed how to use Green's Functions = Kernel Functions of Classical Domain structures characterizing Sources = Leptons, Quarks, and Gauge Bosons, to calculate Particle Masses and Force Strengths

Schwinger (1969 - see physics/0610054) said: "... operator field theory ... replace[s] the particle with ... properties ... distributed througout ... small volumes of three-dimensional space ... particles ... must be created ... even though we vary a number of experimental parameters ... The properties of the particle ... remain the same ... We introduce a quantitative description of the particle source in terms of a source function ... we do not have to claim that we can make the source arbitrarily small ... the experimeter... must detect the particles ...[by]... collision that annihilates the particle ... the source ... can be ... an abstraction of an annihilation collision, with the source acting negatively, as a sink ... The basic things are ... the source functions ... describing the intermediate propagation of the particle ...".

Creation and Annihilation operators indicate a Clifford Algebra, and 8-Periodicity shows that the basic Clifford Algebra is formed by tensor products of 256-dim Cl(8) such as Cl(8) x Cl(8) = Cl(16) containing 248-dim E8 = 120-dim D8 + 128-dim D8 half-spinor whose maximal contraction is a realistic generalized Heisenberg Algebra h92 x A7 = 5-graded 28 + 64 + ((SL(8,R)+1) + 64 + 28 The Cl(1,25) E8 model Lagrangian over 4-dim Minkowski SpaceTime M4 is

GG + SM + Fermion Particle-AntiParticle + Higgs 4-dim M4 .

Consider the Fermion Term.

In the conventional picture, the spinor fermion term is of the form m S S* where m is the fermion mass and S and S* represent the given fermion. The Higgs coupling constants are, in the conventional picture, ad hoc parameters, so that effectively the mass term is, in the conventional picture, an ad hoc inclusion.

The Cl(1,25) E8 model constructs the Lagrangian integral such that the mass m emerges as the integral over the Schwinger Source spacetime region of its Kerr-Newman cloud of virtual particle/antiparticle pairs plus the valence fermion so that the volume of the Schwinger Source fermion defines its mass, which, being dressed with the particle/antiparticle pair cloud, gives quark mass as constituent mass.

Fermion Schwinger Sources correspond to the Lie Sphere Symmetric space Spin(10) / Spin(8)xU(1)

which has

local symmetry of the Spin(8) gauge group from which the first generation spinor fermions are formed as +half-spinor and -half-spinor spaces and

Bounded Complex Domain D8 of type IV8 and Shilov Boundary Q8 = RP1 x S7

Consider the GG + SM term from Gauge Gravity and Standard Model Gauge Bosons. The process of breaking Octonionic 8-dim SpaceTime down to Quaternionic (4+4)-dim M4 x CP2 Kaluza-Klein creates differences in the way gauge bosons "see" 4-dim Physical SpaceTime. There 4 equivalence classes of 4-dimensional Riemannian Symmetric Spaces with Quaternionic structure consistent with 4-dim Physical SpaceTime:

S4 = 4-sphere = Spin(5) / Spin(4) where Spin(5) = Schwinger-Euclidean version of the Anti-DeSitter subgroup of the Conformal Group that gives MacDowell-Mansouiri Gravity

CP2 = complex projective 2-space = SU(3) / U(2) with the SU(3) of the Color Force

S2 x S2 = SU(2)/U(1) x SU(2)/U(1) with two copies of the SU(2) of the Weak Force

S1 x S1 x S1 x S1 = U(1) x U(1) x U(1) x U(1) = 4 copies of the U(1) of the EM Photon (1 copy for each of the 4 covariant components of the Photon)

The Gravity Gauge Bosons (Schwinger-Euclidean versions) live in a Spin(5) subalgebra of the Spin(6) Conformal subalgebra of D4 = Spin(8). They "see" M4 Physical spacetime as the 4-sphere S4 so that their part of the Physical Lagrangian is

Gravity Gauge Boson Term

S4 .

an integral over SpaceTime S4.

The Schwinger Sources for GRb bosons are the Complex Bounded Domains and Shilov Boundaries for Spin(5) MacDowell-Mansouri Gravity bosons.

However, due to Stabilization of Condensate SpaceTime

by virtual Planck Mass Gravitational Black Holes,

for Gravity, the effective force strength that we see in our experiments

is not just composed of the S4 volume and the Spin(5) Schwinger Source volume,

but is suppressed by the square of the Planck Mass.

The unsuppressed Gravity force strength is the Geometric Part of the force strength.

The Standard Model SU(3) Color Force bosons live in a SU(3) subalgebra of the SU(4) subalgebra of D4 = Spin(8). They "see" M4 Physical spacetime as the complex projective plane CP2 so that their part of the Physical Lagrangian is

SU(3) Color Force Gauge Boson Term

CP2.

an integral over SpaceTime CP2.

The Schwinger Sources for SU(3) bosons are the Complex Bounded Domains and Shilov Boundaries for SU(3) Color Force bosons.

The Color Force Strength is given by

the SpaceTime CP2 volume and the SU(3) Schwinger Source volume.

Note that since the Schwinger Source volume is dressed with the particle/antiparticle pair cloud, the calculated force strength is

for the characteristic energy level of the Color Force (about 245 MeV).

The Standard Model SU(2) Weak Force bosons live in a SU(2) subalgebra of the U(2) local group of CP2 = SU(3) / U(2) They "see" M4 Physical spacetime as two 2-spheres S2 x S2 so that their part of the Physical Lagrangian is

SU(2) Weak Force Gauge Boson Term

S2xS2 .

an integral over SpaceTime S2xS2.

The Schwinger Sources for SU(2) bosons are the Complex Bounded Domains and Shilov Boundaries for SU(2) Weak Force bosons.

However, due to the action of the Higgs mechanism,

for the Weak Force, the effective force strength that we see in our experiments is not just composed of the S2xS2 volume and the SU(2) Schwinger Source volume, but is suppressed by the square of the Weak Boson masses.

The unsuppressed Weak Force strength is the Geometric Part of the force strength.

The Standard Model U(1) Electromagnetic Force bosons (photons) live in a U(1) subalgebra of the U(2) local group of CP2 = SU(3) / U(2) They "see" M4 Physical spacetime as four 1-sphere circles S1xS1xS1xS1 = T4 (T4 = 4-torus) so that their part of the Physical Lagrangian is

(U(1) Electromagnetism Gauge Boson Term

T4 .

an integral over SpaceTime T4.

The Schwinger Sources for U(1) photons

are the Complex Bounded Domains and Shilov Boundaries for U(1) photons.

The Electromagnetic Force Strength is given by

the SpaceTime T4 volume and the U(1) Schwinger Source volume.

Schwinger Sources as described above are continuous manifold structures of Bounded Complex Domains and their Shilov Boundaries but

the E8 model at the Planck Scale has spacetime condensing out of Clifford structures forming a Leech lattice underlying 26-dim String Theory of World-Lines with 8 + 8 + 8 = 24-dim of fermion particles and antiparticles and of spacetime.

The automorphism group of a single 26-dim String Theory cell modulo the Leech lattice is the Monster Group of order about 8 x 10^53.

(see Appendix - Details of World-Line String Bohm Quantum Theory

When a fermion particle/antiparticle appears in E8 spacetime it does not remain a single Planck-scale entity because Tachyons create a cloud of particles/antiparticles.

The cloud is one Planck-scale Fundamental Fermion Valence Particle plus an effectively neutral cloud of particle/antiparticle pairs forming a Kerr-Newman black hole. That cloud constitutes the Schwinger Source.

Its structure comes from the 24-dim Leech lattice part of the Monster Group which is $2^{(1+24)}$ times the double cover of Co1, for a total order of about 10^26.

(Since a Leech lattice is based on copies of an E8 lattice and since there are 7 distinct E8 integral domain lattices there are 7 (or 8 if you include a non-integral domain E8 lattice) distinct Leech lattices. The physical Leech lattice is a superposition of them, effectively adding a factor of 8 to the order.)

The volume of the Kerr-Newman Cloud is on the order of 10^{27} x Planck scale, so the Kerr-Newman Cloud should contain about 10^{27} particle/antiparticle pairs and its size should be about $10^{(27/3)}$ x $1.6 \times 10^{(-33)}$ cm = roughly $10^{(-24)}$ cm.

Force Strength and Boson Mass Calculation

Cl(8) bivector Spin(8) is the D4 Lie algebra two copies of which are in the Cl(1,25) E8 model Lagrangian (as the D4xD4 subalgebra of the D8 subalgebra of E8)

GG + SM + Fermion Particle-AntiParticle + Higgs 4-dim M4 .

with the Higgs term coming from integrating over the CP2 Internal Symmetry Space of M4 x CP2 Kaluza-Klein by the Mayer-Trautman Mechanism

This shows that the Force Strength is made up of two parts:

the relevant spacetime manifold of gauge group global action

and

the relevant symmetric space manifold of gauge group local action.

The 4-dim spacetime Lagrangian GG SM gauge boson term is: the integral over spacetime as seen by gauge boson acting globally of the gauge force term of the gauge boson acting locally for the gauge bosons of each of the four forces:

U(1) for electromagnetism

SU(2) for weak force

SU(3) for color force

Spin(5) - compact version of antiDeSitter Spin(2,3) subgroup of Conformal Spin(2,4) for gravity by the MacDowell-Mansouri mechanism.

In the conventional picture,

for each gauge force the gauge boson force term contains the force strength,

which in Feynman's picture is the amplitude to emit a gauge boson,

and can also be thought of as the probability = square of amplitude,

in an explicit (like g IFI^2) or an implicit (incorporated into the IFI^2) form.

Either way, the conventional picture is that the force strength g is an ad hoc inclusion.

The Cl(1,25) E8 model does not put in force strength g ad hoc,

but constructs the integral such that

the force strength emerges naturally from the geometry of each gauge force.

To do that, for each gauge force:

1 - make the spacetime over which the integral is taken be spacetime as it is seen by that gauge boson, that is, in terms of the symmetric space with global symmetry of the gauge boson:

the U(1) photon sees 4-dim spacetime as $T^{4} = S1 \times S1 \times S1 \times S1$ the SU(2) weak boson sees 4-dim spacetime as S2 x S2 the SU(3) weak boson sees 4-dim spacetime as CP2 the Spin(5) of gravity sees 4-dim spacetime as S4

2 - make the gauge boson force term have the volume of the Shilov boundary corresponding to the symmetric space with local symmetry of the gauge boson. The nontrivial Shilov boundaries are:

for SU(2) Shilov = RP^1xS^2 for SU(3) Shilov = S^5 for Spin(5) Shilov = RP^1xS^4

The result is (ignoring technicalities for exposition) the geometric factor for force strengths.

Each gauge group is the global symmetry of a symmetric space S1 for U(1) S2 = SU(2)/U(1) = Spin(3)/Spin(2) for SU(2) CP2 = SU(3)/SU(2)xU(1) for SU(3) S4 = Spin(5)/Spin(4) for Spin(5)

Each gauge group is the local symmetry of a symmetric space U(1) for itself SU(2) for Spin(5) / SU(2)xU(1) SU(3) for SU(4) / SU(3)xU(1) Spin(5) for Spin(7) / Spin(5)xU(1)

The nontrivial local symmetry symmetric spaces correspond to bounded complex domains

SU(2) for Spin(5) / SU(2)xU(1) corresponds to IV3 SU(3) for SU(4) / SU(3)xU(1) corresponds to B^6 (ball) Spin(5) for Spin(7) / Spin(5)xU(1) corresponds to IV5

The nontrivial bounded complex domains have Shilov boundaries SU(2) for Spin(5) / SU(2)xU(1) corresponds to IV3 Shilov = RP^1xS^2 SU(3) for SU(4) / SU(3)xU(1) corresponds to B^6 (ball) Shilov = S^5 Spin(5) for Spin(7) / Spin(5)xU(1) corresponds to IV5 Shilov = RP^1xS^4

Very roughly, think of the force strength as integral over global symmetry space of physical (ie Shilov Boundary) volume = = strength of the force. That is:

the geometric strength of the force is given by the product of the volume of a 4-dim thing with global symmetry of the force and the volume of the Shilov Boundary for the local symmetry of the force.

When you calculate the product volumes (using some tricky normalization stuff), you see that roughly:

Volume product for gravity is the largest volume so since (as Feynman says) force strength = probability to emit a gauge boson means that the highest force strength or probability should be 1 the gravity Volume product is normalized to be 1, and so (approximately):

> Volume product for gravity = 1 Volume product for color = 2/3Volume product for weak = 1/4Volume product for electromagnetism = 1/137

There are two further main components of a force strength:

1 - for massive gauge bosons, a suppression by a factor of 1 / M^2

2 - renormalization running (important for color force)

Consider Massive Gauge Bosons:

Gravity as curvature deformation of SpaceTime, with SpaceTime as a condensate of Planck-Mass Black Holes, must be carried by virtual Planck-mass black holes, so that the geometric strength of gravity should be reduced by 1/Mp^2

The weak force is carried by weak bosons,

so that the geometric strength of the weak force should be reduced by 1/MW^2 That gives the result (approximate):

gravity strength = G (Newton's G) color strength = 2/3 weak strength = G_F (Fermi's weak force G) electromagnetism = 1/137

Consider Renormalization Running for the Color Force:: That gives the result: gravity strength = G (Newton's G) color strength = 1/10 at weak boson mass scale weak strength = G_F (Fermi's weak force G) electromagnetism = 1/137 The use of compact volumes is itself a calculational device, because it would be more nearly correct,

instead of the integral over the compact global symmetry space of the compact physical (ie Shilov Boundary) volume=strength of the force to use

the integral over the hyperbolic spacetime global symmetry space of the noncompact invariant measure of the gauge force term.

However, since the strongest (gravitation) geometric force strength is to be normalized to 1, the only thing that matters is ratios,

and the compact volumes (finite and easy to look up in the book by Hua) have the same ratios as the noncompact invariant measures.

In fact, I should go on to say that continuous spacetime and gauge force geometric objects are themselves also calculational devices, and

that it would be even more nearly correct to do the calculations with respect to a discrete generalized hyperdiamond Feynman checkerboard.

Fermion Mass Calculations

In the CI(1,25) E8 model, the first generation spinor fermions are seen as +half-spinor and -half-spinor spaces of CI(1,7) = CI(8). Due to Triality, Spin(8) can act on those 8-dimensional half-spinor spaces similarly to the way it acts on 8-dimensional vector spacetime.

Take the spinor fermion volume to be the Shilov boundary corresponding to the same symmetric space on which Spin(8) acts as a local gauge group that is used to construct 8-dimensional vector spacetime:

the symmetric space Spin(10) / Spin(8)xU(1) corresponding to a bounded domain of type IV8 whose Shilov boundary is RP^1 x S^7

Since all first generation fermions see the spacetime over which the integral is taken in the same way (unlike what happens for the force strength calculation), the only geometric volume factor relevant for calculating first generation fermion mass ratios is in the spinor fermion volume term.

Cl(1,25) E8 model fermions correspond to Schwinger Source Kerr-Newman Black Holes,

so the quark mass in the CI(1,25) E8 model is a constituent mass.

Fermion masses are calculated as a product of four factors:

V(Qfermion) x N(Graviton) x N(octonion) x Sym

V(Qfermion) is the volume of the part of the half-spinor fermion particle manifold S^7 x RP^1 related to the fermion particle by photon, weak boson, or gluon interactions.

N(Graviton) is the number of types of Spin(0,5) graviton related to the fermion. The 10 gravitons correspond to the 10 infinitesimal generators of Spin(0,5) = Sp(2). 2 of them are in the Cartan subalgebra.

6 of them carry color charge, and therefore correspond to quarks.

The remaining 2 carry no color charge, but may carry electric charge and so may be considered as corresponding to electrons. One graviton takes the electron into itself, and the other can only take the first generation electron into the massless electron neutrino. Therefore only one graviton should correspond to the mass of the first-generation electron.

The graviton number ratio of the down quark to the first-generation electron is therefore 6/1 = 6.

N(octonion) is an octonion number factor relating up-type quark masses to down-type quark masses in each generation.

Sym is an internal symmetry factor, relating 2nd and 3rd generation massive

leptons to first generation fermions. It is not used in first-generation calculations.

The first generation down quark constituent mass : electron mass ratio is:

The electron, E, can only be taken into the tree-level-massless neutrino, 1, by photon, weak boson, and gluon interactions.

The electron and neutrino, or their antiparticles, cannot be combined to produce any of the massive up or down quarks.

The neutrino, being massless at tree level, does not add anything to the mass formula for the electron.

Since the electron cannot be related to any other massive Dirac fermion, its volume V(Qelectron) is taken to be 1.

Next consider a red down quark i.

By gluon interactions, i can be taken into j and k, the blue and green down quarks. By also using weak boson interactions,

it can also be taken into I, J, and K, the red, blue, and green up quarks.

Given the up and down quarks, pions can be formed from quark-antiquark pairs,

and the pions can decay to produce electrons and neutrinos.

Therefore the red down quark (similarly, any down quark)

is related to all parts of S^7 x RP^1,

the compact manifold corresponding to { 1, i, j, k, E, I, J, K }

and therefore a down quark should have

a spinor manifold volume factor V(Qdown quark) of the volume of S^7 x RP^1.

The ratio of the down quark spinor manifold volume factor to the electron spinor manifold volume factor is $V(Qdown quark) / V(Qelectron) = V(S^7x RP^1)/1 = pi^5 / 3.$

Since the first generation graviton factor is 6, md / me = $6 V(S^7 \times RP^1) = 2 pi^5 = 612.03937$

As the up quarks correspond to I, J, and K, which are the octonion transforms under E of i, j, and k of the down quarks, the up quarks and down quarks have the same constituent mass

mu = md.

Antiparticles have the same mass as the corresponding particles. Since the model only gives ratios of masses, the mass scale is fixed so that the electron mass me = 0.5110 MeV. Then, the constituent mass of the down quark is md = 312.75 MeV, and the constituent mass for the up quark is mu = 312.75 MeV. These results when added up give a total mass of first generation fermion particles: Sigmaf1 = 1.877 GeV As the proton mass is taken to be the sum of the constituent masses of its constituent quarks

mproton = mu + mu + md = 938.25 MeV

which is close to the experimental value of 938.27 MeV.

The third generation fermion particles correspond to triples of octonions. There are $8^3 = 512$ such triples.

The triple { 1,1,1 } corresponds to the tau-neutrino.

The other 7 triples involving only 1 and E correspond to the tauon:

{ E, E, E }

{ E, E, 1 }

{ E, 1, E }

{ 1, E, E }

{1, 1, E}

{ 1, E, 1 }

{ E, 1, 1 }

The symmetry of the 7 tauon triples is the same

as the symmetry of the first generation tree-level-massive fermions,

3 down, quarks, the 3 up quarks, and the electron,

so by the Sym factor the tauon mass should be the same as

the sum of the masses of the first generation massive fermion particles.

Therefore the tauon mass is calculated at tree level as 1.877 GeV.

The calculated tauon mass of 1.88 GeV is a sum of first generation fermion

masses, all of which are valid at the energy level of about 1 GeV.

However, as the tauon mass is about 2 GeV,

the effective tauon mass should be renormalized

from the energy level of 1 GeV at which the mass is 1.88 GeV

to the energy level of 2 GeV.

Such a renormalization should reduce the mass.

If the renormalization reduction were about 5 percent,

the effective tauon mass at 2 GeV would be about 1.78 GeV.

The 1996 Particle Data Group Review of Particle Physics gives a tauon mass of 1.777 GeV.

All triples corresponding to the tau and the tau-neutrino are colorless.

The beauty quark corresponds to 21 triples.

They are triples of the same form as the 7 tauon triples involving 1 and E, but for 1 and I, 1 and J, and 1 and K,

which correspond to the red, green, and blue beauty quarks, respectively.

The seven red beauty quark triples correspond to the seven tauon triples, except that

the beauty quark interacts with 6 Spin(0,5) gravitons while the tayon interacts with only two

while the tauon interacts with only two.

The red beauty quark constituent mass should be the tauon mass times the third generation graviton factor 6/2 = 3, so the red beauty quark mass is mb = 5.63111 GeV.

The blue and green beauty quarks are similarly determined to also be 5.63111 GeV.

The theoretical model calculated Beauty Quark mass of 5.63 GeV

corresponds to a pole mass of 5.32 GeV,

which is somewhat higher than the conventional value of 5.0 GeV.

However, the theoretical model calculated value

of the color force strength constant alpha_s at about 5 GeV is about 0.166, while the conventional value

of the color force strength constant alpha_s at about 5 GeV is about 0.216, and

the theoretical model calculated value

of the color force strength constant alpha_s at about 90 GeV is about 0.106, while the conventional value

of the color force strength constant alpha_s at about 90 GeV is about 0.118.

Triples of the type { 1, I, J } , { I, J, K }, etc.,

do not correspond to the beauty quark, but to the truth quark.

The truth quark corresponds to those 512 - 1 - 7 - 21 = 483 triples,

so the constituent mass of the red truth quark

is 161 / 7 = 23 times the red beauty quark mass,

and the red T-quark mass is

mt = 129.5155 GeV

The blue and green truth quarks are similarly determined to also be 129.5155 GeV. This is the value of the Low Mass State of the Truth calculated in the Cl(1,25) E8 model. The Middle Mass State of the Truth Quark has been observed by Fermilab since 1994. The Low and High Mass States of the Truth Quark have, in my opinion, also been observed by Fermilab but the Fermilab and CERN establishments disagree.

These results when added up give a total mass of third generation fermion particles:

Sigmaf3 = 1,629 GeV

E8 Physics Calculation Results

Here is a summary of E8 Physics model calculation results. Since ratios are calculated, values for one particle mass and one force strength are assumed. Quark masses are constituent masses. Most of the calculations are tree-level, so more detailed calculations might be even closer to observations.

Dark Energy : Dark Matter : Ordinary Matter = 0.75 : 0.21 : 0.04

Fermions as Schwinger Sources have geometry of Complex Bounded Domains with Kerr-Newman Black Hole structure size about $10^{(-24)}$ cm.

Particle/Force	Tree-1	Level	Higher-Order	
e-neutrino	0		0 for nu_1	
mu-neutrino	0		9 x 10^(-3) eV for nu_2	
tau-neutrino	0		5.4 x $10^{(-2)}$ eV for nu_3	
electron	0.5110			
down quark	312.8		charged pion = 139 MeV	
up quark	312.8	MeV	proton = 938.25 MeV	
			neutron - proton = 1.1 MeV	
muon	104.8	MeV	106.2 MeV	
strange quark	625	MeV		
charm quark	2090	MeV		
tauon	1.88			
beauty quark	5.63			
truth quark (low stat	ce) 130	GeV	(middle state) 174 GeV	
			(high state) 218 GeV	
W+	80.326			
W-	80.326	GeV		
WO	98.379	GeV	Z0 = 91.862 GeV	
Mplanck 1.	217x10^19	Gev		
Higgs VEV (assumed)	252.5	GeV		
Higgs (low state)		GeV	(middle state) 182 GeV	
miggs (iow state)	120		(high state) 239 GeV	
			(high state) 259 dev	
Gravity Gg (assumed)	1			
$(Gg) (Mproton^2 / Mplanck^2) \qquad 5 \times 10^{-39}$				
EM fine structure		.03608		
Weak Gw	0.2			
Gw(Mproton^2 / (Mw+^2			2)) $1.05 \times 10^{(-5)}$	
Color Force at 0.245			0.106 at 91 GeV	
00101 1010C ut 0.213	0.01	200		
Kobayashi-Maskawa parameters for W+ and W- processes are:				
d	S		b	
u 0.975	0.222		0.00249 -0.00388i	
c -0.222 -0.000161i		-0.00		
t 0.00698 -0.00378i				
The phase angle d13 is taken to be 1 radian.				
			-	

Appendix -Schwinger Source: Monster Size and Mandelbrot Julia Structure

This Appendix is motivated by discussion with Jonathan Dickau.

Abstract

Planck Scale is about 10⁽⁻³³⁾ cm. Schwinger Souce Scale is about 10⁽⁻²⁴⁾ cm, a scale about 10⁹ larger thant the Planck Scale. The number of particles in the Schwinger Source cloud is determined by the Monster Group Symmetry of the Planck Scale Unit Cells of E8 Physics (viXra 1602.0319). Schwinger Sources have external structure related to Kerr-Newman Black Holes and Bounded Complex Domains whose Bergman Kernels correspond to the Green's Functions of the Schwinger Source. Schwinger Source internal structure is determined by the Octonionic Mandelbrot Set corresponding to each Unit Cell and their Julia Sets. Julia Sets give the Green's Function Potential and Field Lines of the Schwinger Source.

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Schwinger Source Size and the Monster Group

Fock "Fundamental of Quantum Mechanics" (1931) showed that it requires Linear Operators "... represented by a definite integral [of a]... kernel ... function ...".

Hua "Harmonic Analysis of Functions of Several Complex Variables in the Classical Domains" (1958) showed Kernel Functions for Complex Classical Domains.

Schwinger (1951 - see Schweber, PNAS 102, 7783-7788) "... introduced a description in terms of Green's functions, what Feynman had called propagators ... The Green's functions are vacuum expectation values of time-ordered Heisenberg operators, and the field theory can be defined non-perturbatively in terms of these functions ...[which]... gave deep structural insights into QFTs; in particular ... the structure of the Green's functions when their variables are analytically continued to complex values ...".

Wolf (J. Math. Mech 14 (1965) 1033-1047) showed that the Classical Domains (complete simply connected Riemannian symmetric spaces) representing 4-dim Spacetime with Quaternionic Structure are:

S1 x S1 x S1 x S1 x S1 = 4 copies of U(1) S2 x S2 = 2 copies of SU(2) CP2 = SU(3) / SU(2)xU(1)S4 = Spin(5) / Spin(4) = Euclidean version of Spin(2,3) / Spin(1,3)

Armand Wyler (1971 - C. R. Acad. Sc. Paris, t. 271, 186-188) showed how to use Green's Functions = Kernel Functions of Classical Domain structures characterizing Sources = Leptons, Quarks, and Gauge Bosons, to calculate Particle Masses and Force Strengths

Schwinger (1969 - see physics/0610054) said: "... operator field theory ... replace[s] the particle with... properties ... distributed throughout ... small volumes of three-dimensional space ... particles ... must be created ... even though we vary a number of experimental parameters ... The properties of the particle ... remain the same ... We introduce a quantitative description of the particle source in terms of a source function ... we do not have to claim that we can make the source arbitrarily small ... the experimeter... must detect the particles ...[by]... collision that annihilates the particle ... the source ... can be ... an abstraction of an annihilation collision, with the source acting negatively, as a sink ... The basic things are ... the source functions ... describing the intermediate propagation of the particle ...".

Schwinger Sources can be described by continuous manifold structures of Bounded Complex Domains and their Shilov Boundaries but

the Cl(16)-E8 model at the Planck Scale has spacetime condensing out of Clifford structures forming a Leech lattice underlying 26-dim String Theory of World-Lines with 8 + 8 + 8 = 24-dim of fermion particles and antiparticles and of spacetime.

The automorphism group of a single 26-dim String Theory cell modulo the Leech lattice is the Monster Group of order about 8 x 10^53.

When a fermion particle/antiparticle appears in E8 spacetime it does not remain a single Planck-scale entity because Tachyons create a cloud of particles/antiparticles. The cloud is one Planck-scale Fundamental Fermion Valence Particle plus an effectively neutral cloud of particle/antiparticle pairs forming a Kerr-Newman black hole. That Kerr-Newman cloud constitutes the E8 Physics model Schwinger Source.

The cloud structure comes from the 24-dim Leech lattice part of the Monster Group which is $2^{(1+24)}$ times the double cover of Co1, for a total order of about 10²⁶.

Since a Leech lattice is based on copies of an E8 lattice and since there are 7 distinct E8 integral domain lattices there are 7 (or 8 if you include a non-integral domain E8 lattice) distinct Leech lattices. The physical Leech lattice is a superposition of them, effectively adding a factor of 8 to the order,

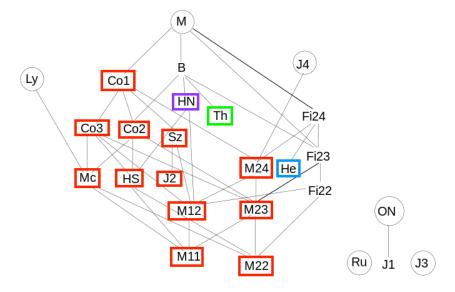
so the volume of the Kerr-Newman Cloud is on the order of $10^{27} \times Planck$ scale and the Kerr-Newman Cloud should contain about 10^{27} particle/antiparticle pairs and its size should be about $10^{(27/3)} \times 1.6 \times 10^{(-33)}$ cm = roughly $10^{(-24)}$ cm.

The Monster Group is of order

8080 , 17424, 79451, 28758, 86459, 90496, 17107, 57005, 75436, 80000, 00000 =

2^46 . 3^20 . 5^9 . 7^6 . 11^2 . 13^3 . 17. 19. 23. 29. 31. 41. 47. 59 . 71 or about 8 x 10^53

This chart (from Wikipedia) shows the Monster M and other Sporadic Finite Groups



The order of Co1 is $2^21.3^9.5^4.7^2.11.13.23$ or about 4×10^{18} . Aut(Leech Lattice) = double cover of Co1.

The order of the double cover 2.Co1 is $2^22.3^9.5^4.7^2.11.13.23$ or about 0.8 x 10^19. Taking into account the non-sporadic part of the Leech Lattice symmetry according to the ATLAS at brauer.maths.qmul.ac.uk/Atlas/v3/spor/M/ the Schwinger Source Kerr-Newman Cloud Symmetry s $2^(1+24)$.Co1 of order 139511839126336328171520000 = 1.4 x 10^26

Co1 and its subgroups account for 12 of the 19 subgroups of the Monster M. Of the remaining 7 subgroups, Th and He are independent of the Co1 related subgroups and HN has substantial independent structure.

Th = Thompson Group. Wikipedia says "... Th ... was ... constructed ... as the automorphism group of a certain lattice in the 248-dimensional Lie algebra of E8. It does not preserve the Lie bracket of this lattice, but

does preserve the Lie bracket mod 3, so is a subgroup of the Chevalley group E8(3). The subgroup preserving the Lie bracket (over the integers) is a maximal subgroup of the Thompson group called the Dempwolff group (which unlike the Thompson group is a subgroup of the compact Lie group E8) ...

the Thompson group acts on a vertex operator algebra over the field with 3 elements. This vertex operator algebra contains the E8 Lie algebra over F3, giving the embedding of Th into E8(3) ...

The Schur multiplier and the outer automorphism group of ... Th ... are both trivial. Th is a sporadic simple group of order $215 \cdot 310 \cdot 53 \cdot 72 \cdot 13 \cdot 19 \cdot 31$ = 90745943887872000 \approx 9 x 10^16 ...".

He = Held Group. Wikipedia says "... The smallest faithful complex representation has dimension 51; there are two such representations that are duals of each other. It centralizes an element of order 7 in the Monster group. ... the prime 7 plays a special role in the theory of the group ... the smallest representation of the Held group over any field is the 50 dimensional representation over the field with 7 elements ... He ... acts naturally on a vertex operator algebra over the field with 7 elements ... The outer automorphism group has order 2 and the Schur multiplier is trivial. ... He is a sporadic simple group of order 210 \cdot 33 \cdot 52 \cdot 73 \cdot 17 = 4030387200 \approx 4 x 10⁴9 ...".

HN = Harada-Norton Group. Wikipedia says "... The prime 5 plays a special role ... it centralizes an element of order 5 in ... the Monster group ...and as a result acts naturally on a vertex operator algebra over the field with 5 elements ... it acts on a 133 dimensional algebra over \mathbf{F}_5 with a commutative but nonassociative product ... Its Schur multiplier is trivial and its outer automorphism group has order 2 ... HN is a sporadic simple group of order $2^{14} \cdot 3^6 \cdot 5^6 \cdot 7 \cdot 11 \cdot 19$ = 273030912000000 \approx 3 x 10^14 ... HN has an involution whose centralizer is of the form 2.HS.2, where HS is the Higman-Sims group ... of order $2^9 \cdot 3^2 \cdot 5^3 \cdot 7 \cdot 11 = 44352000 \approx 4 \times 10^{7}$...[whose] Schur multiplier has order 2 ...[and whose] outer automorphism group has order 2 ... HS is ... a subgroup of ... the Conway groups Co0, Co2 and Co3 ...".

Co1 x Th x He x HN / HS together have order about $4 \times 9 \times 4 \times 10^{(18+16+9+7)}$ = about 10^52 which is close to the order of M = about 10^54.

The components of the Monster Group describe the composition of Schwinger Sources:

Co1 gives the number of particles in the Schwinger Source Kerr-Newman Cloud emanating from a Valence particle in a Planck-scale cell of E8 Physics SpaceTime.

Th gives the 3-fold E8 Triality structure relating 8-dim SpaceTime to First-Generation Fermion Particles and AntiParticles.

He gives the 7-fold algebraically independent Octonion Imaginary E8 Integral Domains that make up 7 of the 8 components of Octonion Superposition E8 SpaceTime.

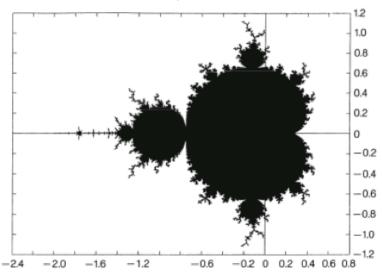
HN / HS gives the 5-fold symmetry of 120-element Binary Icosahedral E8 McKay Group beyond the 24-element Binary Tetrahedral E6 McKay Group at which level the Shilov Boundaries of Bounded Complex Domains emerge to describe SpaceTime and Force Strengths and Particle Masses.

Mandelbrot Sets

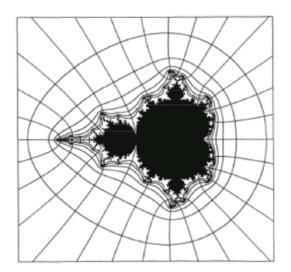
Peitgen, and Richter in The Beauty of Fractals (1986) say

"... the Mandelbrot set embodies a principle of the transition from order to chaos more general than the Feigenbaum universality. ... Mandelbrot's ingenuity was to look at complex numbers ... to follow the process ... on a plane ... The focus has shifted to the nature of boundaries between different regions. We can think of centers - attractors - which compete for influence on the plane: an initial point ... is driven by the process to one center or another, or it is on the boundary and cannot decide.

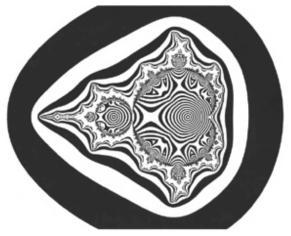
If the parameter is changed, the regions belonging to the attractors change, and with them the boundaries. It can happen that the boundary falls to dust, and this decay is one of the most important scenarios. ... Mandelbrot's process is ... $x \rightarrow x^2 + c \dots$



... Charged Mandelbrot set with equipotential and field lines ...



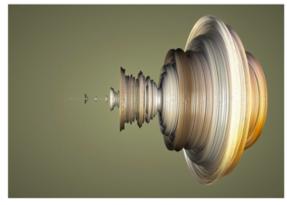
... Level sets ... in alternating colors for c in M ... Outside of M: equipotential lines ...



... Domains of index (c) = constant ... Indices organize according to Fibonacci sequences. Outside of M: equipotential lines ...".

The Complex Mandelbrot set is symmetric about the real axis, so it has symmetry of the dihedral group of order 2. For details see https://www.math.uwaterloo.ca/~wgilbert/FractalGallery/Mandel/MandelMath.html The symmetry group dihedral(2) tor the Mandelbrot set of $f(z) = z^2 + c$ can be expanded to the Binary Dihedral Group {2,2,2} by going from 2-dim Complex Numbers to Quaternions of 4-dim M4 SpaceTime. McKay says: "... D[4] {2,2,4-2} Generalized quaternion [4-2] ...". D[4] is the D4 Lie algebra Spin(8), the bivector Lie Algebra of the Cl(8) Clifford Algebra that by Real Clifford Algebra 8-Periodicity tensor product produces Cl(8)xCl(8) = Cl(16) which contains 248-dim E8 as 120-dim D8 + 128-dim half-spinor D8 and by completing the union of all tensor products of Cl(16) produces an AQFT. The corresponding String Theory, with Strings seen as World-Lines of Particles, has Planck-scale local lattice structure each cell of which has Monster Group symmetry.

Here is a Quaternionic Mandelbrot set image by Mikael Hvidtfeldt Christensen:

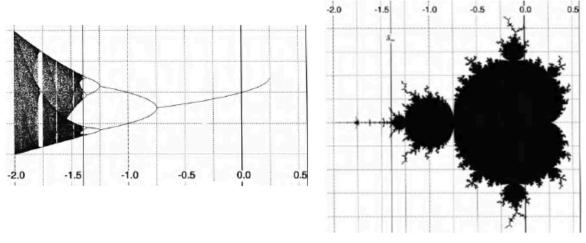


it is basically a 2-dim Mandelbrot set rotated about the real axis. An Octonionic Mandelbrot set would be similar, so the Complex Mandelbrot Set gives most of the useful structure.

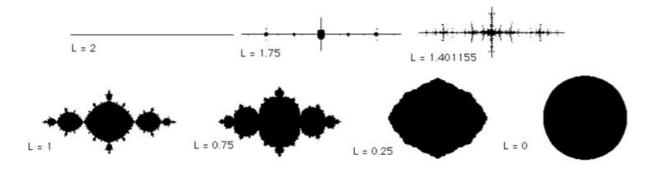
Julia Sets

Points of the Mandelbrot Set represent Julia Sets.

Characteristics of the Julia Sets and Bifurcations vary with their position on the Mandelbrot Set. First consider positions along the Real Axis from -L = -2 to -L = 0.25:



(images above from Peitgen, Jurgens and Saupe, Chaos and Fractals)



Lennart Carleson and Theodore W. Gamelin in their book Complex Dynamics say: "... Let us see how the Julia set changes shape as c moves along the real axis. If we move c to the right of 1/4, it leaves the Mandelbrot set and the Julia set becomes totally disconnected. ...the cauliflower set, corresponding to c = 1/4 ... is a simple closed Jordan curve ... though it cannot be a quasicircle due to the cusps. ... the Julia set for c = -3/5 ... is a quasicircle, symmetric with respect to R. ... at the left edge of the main cardioid we arrive at the point c = -3/4 ... There are two petals at - 1/2, which cycle back and forth. ... When we continue to the left of - 3/4, the fixed point bifurcates to an attracting cycle of length two, corresponding to the two petals.

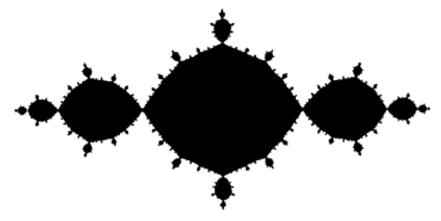


FIGURE 8. c = -1, superattracting cycle of period two.

This process is called "budding," and the point - 3/4 is the "root" of the bud. ...

For c = -1, we have the superattracting cycle $0 \rightarrow -1 \rightarrow 0$

pictured in Figure 8. The basic shape of the Julia set is preserved as

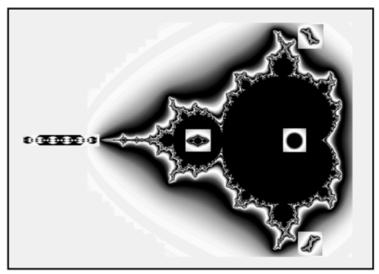
we cross from c = -3/5 over c = -3/4 to c = -1.

At c = -5/4 we have a parabolic cycle of petals of order 4, and there is further budding. Continuing to decrease c gives a sequence

c0 > c1 > c2 > ... of parameter values corresponding to parabolic cycles of order In the complementary intervals, has attracting cycles of order This behavior is known as the period doubling of Feigenbaum, and c n -> c oo = - 1.401.

In the interval [- 2, c oo] periods of many different orders occur ...".

Here, near their locations on the Mandlebrot Set, are some Julia Sets useful in describing Schwinger Source Geometry: c = -2, c = -1, c = i, c = 0, c = -i:



(image from Mandelbrot and Julia by Dany Shaanan and by Peitgen, Jurgens, and Saupe)

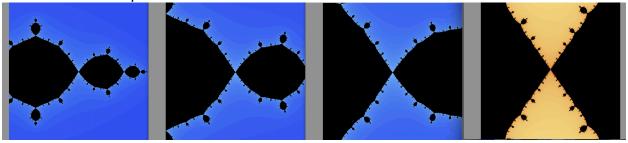
Schwinger Source Structure and Julia Sets

Planck scale is about 10⁽⁻³³⁾ cm. Schwinger Souce Scale is about 10⁽⁻²⁴⁾ cm. What is the structure of the cloud in the 10⁹ Planck units between those scales ?

My conjecture is that it may be Fractal Julia Set structure.

Mark McClure on the Math Stack Exchange 30 May 2013 said:

"... Julia sets of rational functions can be computed using an inverse iteration technique that shows them to be something close to self-similar. This helps explain the extreme regularity displayed when zooming into *most* Julia sets. For example, here we zoom in to the Julia set for $f(z) = z^2 - 1$ increasing the magnification by a factor of the Golden ratio with each step. ...



The first three images are at steps 0, 1, and 2. The fourth image is at step 41. Since $1.6^{41} = 2.3 \times 10^{8}$, the same similarity exists all the way down from Schwinger Source scale 10^{-24} cm to the Planck scale 10^{-33} cm.

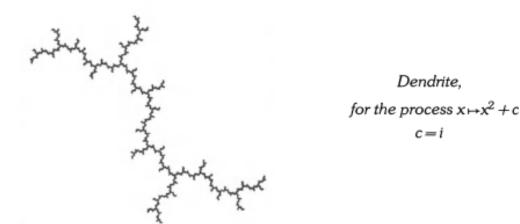
How would such a Julia Set emerge from a single Fundamental Fermion Particle ?

At the Planck-scale E8 Lattice level each Fundametal Fermion Particle is represented by an Octonion Basis Element

1 - Neutrino i - Red Down Quark j - Green Down Quark k - Blue Down Quark E - Electron I - Red Up Quark J - Green Up Quark K - Blue Up Quark

If the Red Down Quark represented by i is at the origin of Planck-scale E8 SpaceTime then a Virtual Cloud of Particles will form around it.

Let z be the Octonion representing the first Particle to appear in the Virtual Cloud. Then form the Octonion Product z^2 and add to it the Octonion i of the Red Down Quark and let that $z^2 + i$ represent the second particle to appear in the Virtual Cloud. Then iterate the process many times. Peitgen and Richter in Beauty of Fractals say "... for the process x -> $x^2 + c ... c = i$... Figure 12 shows the example c = i ...

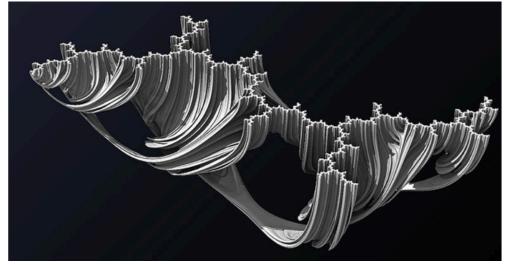


... Such dendrites have no interior, there is no attractor other than the one at infinity. The Julia set is now just the boundary of a single domain of attraction and contains those points that do not go to that attractor ...".

Note that the Beauty of Fractals material assumes 2-dim Complex Numbers whereas realistic physics requires 4-dim Quaternions for M4 Physical SpaceTime and 8-dim Octonions for Inflationary Era E8 Physics.

4-dim Quaternions are needed for j - Green Down Quark and k - Blue Down Quark A Quaternionic Julia set image by Prokofiev (wikimedia) shows the Julia Set for Imaginary Quaternion basis elements { i , j , k } with a cross-section in the XY plane

in which the "dendrite" Complex Julia Set is visible:



8-dim Octonions are needed for E - Electron and I - Red Up Quark and J - Green Up Quark and K - Blue Up Quark

Octonionic images would be similar to the Quaternionic with rotation about the real axis, so the Complex Julia Sets give most of the useful structure.

In the Octonion Julia Set, the 7+7 imaginaries +/- i , +/- j , +/- k , +/- E , +/- I , +/- J , +/- K are all located on the unit 7-sphere S7 centered on the origin c = 0.

Julia Sets for all points on that S7 are of the same type - dendrite - as for i and -i.

Geoffrey Dixon (see Division Algebras, Lattices, Physics, Windmill Tilting, section 4.1) has defined an X-Product for the unit Octonions on a 7-sphere S7 :

"... Let A, B, X be Octonions, with X a unit Octonion ...

Define A ox B = $(AX)(X^*B) = (A(BX)X^* = X((X^*A)B))$ the X-product of A and B. Because of the nonassociativity of O, A ox B =/= AB in general.

But remarkabley, for fixed X, the algebra Ox (O endowed with the X-product) is isomorphic to O itself. Modulo sign change each X gives rise to a distinct copy of O ...".

What about 1 - Neutrino and -1 Anti-Neutrino ?

The 1 and -1 of the Neutrino and Anti-Neutrino do not represent the 1 and -1 on the real axis of the Mandelbrot Set. They represent the 1 and -1 on the Julia Set S7 defined by the Dixon X-Products of the 7 imaginary basis elements {i,j,k,E,I,J,K}.

What about Standard Model Spin 1 Gauge Bosons ?

They can be represented as antisymmetric pairs of representative Fermions and therefore as points on the Julia Set S7 defined by the Dixon X-Products.

What about the Higgs Spin 0 Scalar ?

Higgs can be represented by the Julia Set of the point c = 0 on the Mandelbrot real axis.

What about the Conformal Spin(2,4) = SU(2,2) Graviphoton Spin 1 Bosons?

The Conformal Bosons of Gravity and Dark Energy can be represented by the Julia Set of the point c = -1 on the Mandelbrot real axis.

Peitgen and Richter in Beauty of Fractals say

"... The Inverse Iteration Method (IIM) ... should give a good picture of [the Julia Set] ... if ... it is uniformly distributed over [the Julia Set] ... Figure 26 ... show[s] ...[a] Julia Set from the quadratic family ... $x^2 + c$...[and c = -1] ...

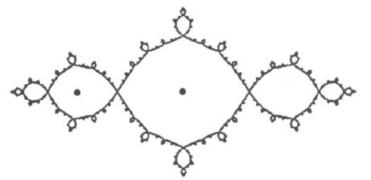
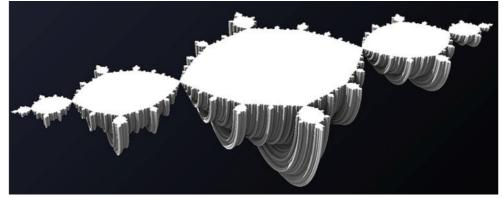


Fig. 26. J_R , $R(x) = x^2 + c$ and c = -1{0, -1} is a super-attractive cycle

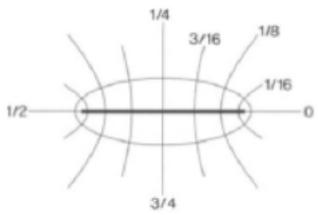
... the tips of [the Julia Set] are visited most frequently, while the branch points seem to be avoided most often. Nevertheless ... the non uniformity has little effect on Fig.26 ...". A Quaternionic Julia set image by Prokofiev (wikimedia) shows the Quaternion Julis Set for c = -1 with a cross-section in the XY plane. in which the corresponding Complex "San Marco fractal" is visible:

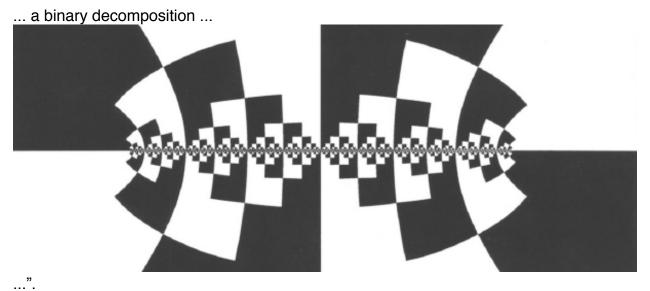


What about the Bohm Quantum Potential Spin 2 Bosons ?

The Bohm Quantum Potential Spin 2 Bosons can be represented by the Julia Set of the point c = -2 on the Mandelbrot real axis.

Peitgen and Richter in Beauty of Fractals say "... Equipotential and field lines for the Julia set of x -> $x^2 + c$, c = -2 ...





Peitgen, Jurgens, and Saupe in Chaos and Fractals say "... Encirclements for ... c = -2 ...



... for c = -2 ... the Julia set is a single connected set ...".

According to usefuljs.net web page on Juia Sets and The Mandelbrot Set:

"... Why is ... $J(z^2 - 2)$ a straight line?

It's easier to understand if we imagine the inverse iteration: start with a circle of radius 2 and then repeatedly apply the iteration function: $z \rightarrow \sqrt{(z - c)}$... c = -2 ...

Each iteration, we shift all points of the circle left by 2 (which discards half of the points). We then take the square root which has three effects:

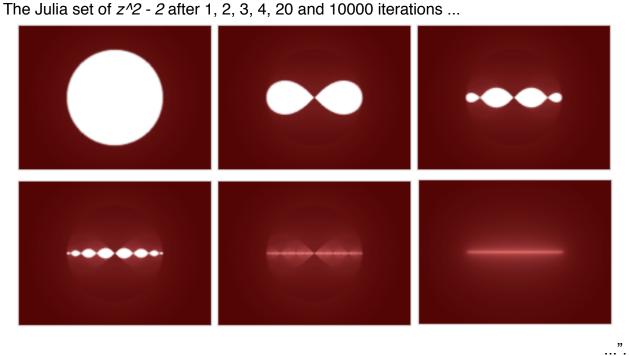
values whose magnitude is > 1 contract,

values whose magnitude is < 1 expand

and the square root creates a mirror image since each number has two square roots. The result is two teardrops that are pinched at the origin.

Repeat and you double the pinched teardrops each iteration while making them smaller. At infinity, the repeated pinching has made the tear drops infinitesimally small,

leaving a straight line segment. ...



Julia Sets of Schwinger Sources and Green's Functions

The Schwinger Source Particles that we deal with experimentally are Kerr-Newman Cloud Shilov Boundaries of Bounded Complex Domains that have symmetry from the 24-dim Leech lattice part of the Monster Group and have volume about 10²7 Planck Volumes and size about 10⁽⁻²⁴⁾ cm.

The Bounded Complex Domain structure of each Schwinger Source gives it (through Bergman Kernel) a Green's Function for its force interactions. The Green's Function is manifested in the interior of the Schwinger Source Cloud by Julia Set organization of the component small particles in the Cloud.

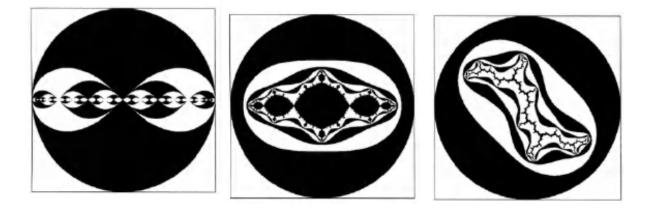
Each cell of the Planck-scale local lattice has a Mandelbrot structure that contains potential Julia Sets. When a Valence Particle manifests itself at a cell of the Planck-scale local lattice it uses a Julia set with matching Green's Function.

M. F. Barnsley, J. S. Geronimo, and A. N. Harrington say

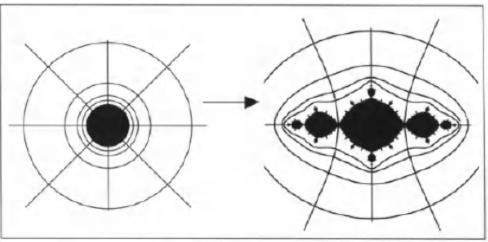
in Geometrical and Electrical Properties of Some Julia Sets (Georgia Tech August 1982) "... electrical properties of Julia sets of an arbitrary potential ... are developed with the aid of the Bottcher equation and Green's star domains ... We use Julia sets for $T(z) = (z - L)^2$ as examples and relate the electrical properties to the geometry of the Julia set ...".

Peitgen, Jurgens, and Saupe in Chaos and Fractals (1992) say

"... points for which the iteration escapes ... is called the escape set ... The iteration for all other initial values remains in a bounded region forever ... the prisoner set ... the boundary ... between the basins of attraction ... is ... the Julia set ... Encirclement of the Prisoner Set ...[by] iteration ...[of] approximation ... shad[ing] the encirclements ... using alternating black and white sets ... for c = -2 ... c = -1 ... c = i ...



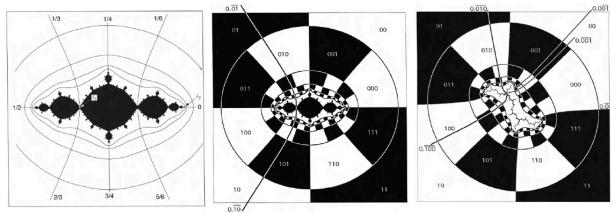
... Think of the prisoner set as a piece of metal charged with electrons ... produc[ing] an electrostatic field in the surrounding space ...[which has] field lines ... an electrostatic field ... is conservative ... there is ... a potential function ... equipotential surfaces ... on which the potential is constant ... are perpendicular everywhere to the direction of the electrostatic field ... the intensity of the field is inversely proportional to the distance between equipotential surfaces ... Riemann Mapping Theorem ...[gives] A one-to-one correspondence between the potential of the unit disk and the potential of any connected prisoner set ...



... Equipotential and field lines for c = -1.

The angles of the field lines are given in multiples of 2 pi ...

Binary decomposition for $c = -1 \dots [and] c = i \dots$



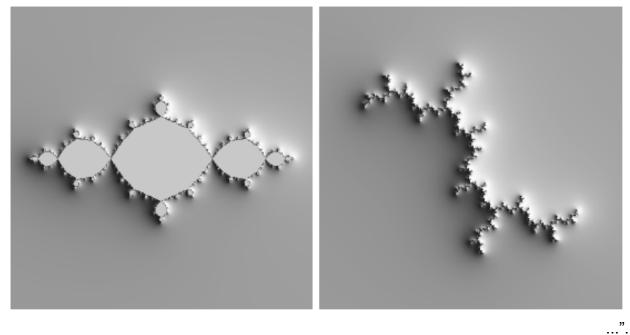
... potential ... level sets capture ... the magnitude of the iterates ...

Now ... turn to the binary decomposition of these level sets ...

There are 2ⁿ stage-n cells in a level set ...

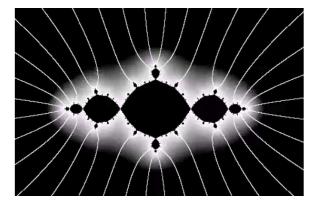
Binary decomposition allows us to approximate arbitrary field lines of the potential. the labelling of these cells converges to the binary expansion of the angles of the field lines passing through the cells ... Only in the limit ... do field lines become ... straight ... from the point of view of field line dynamics ... the dynamics of $z \rightarrow z^2 + c$, c =/= 0, acts like angle doubling, just as for c = 0

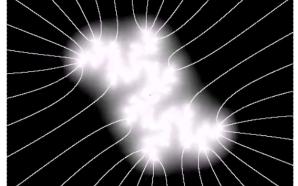
Tomoki Kawahira of the math department of Tokyo Institute of Technology says "...The black and white pictures below show ... Potential functions (Green functions) ... defined outside the (filled) Julia sets ...



Here are the corresponding Field Lines from 2008 YouTube of ImpoliteFruit for Julia fractal, X axis (Distance and field lines) and

Julia fractal, Y axis (Distance and field lines):





Appendix - E8 Physics and 256 Cellular Automata

Raymond Aschheim (email May 2015) said:

"... An elementary CA is defined by the next value (either 0 or 1) for a cell, depending on its ... value, and the ... value of it[s] left and of it[s] right neighbor cell (it is one dimensional, and involve only the first neighbors, and the cell itself) ... So the next value depends [on] 3 bits ... eight possible combination of three bits, and for each ... combination... the next value is either zero or one. So the[re] are 256 ... CAs ...".

Since due to Real Clifford 8-periodicity any Real Clifford Algebra Cl(8N)) can be seen as the tensor product of N copies of Cl(8), any Real Clifford Algebra has fundamental structure of Cl(8) = Cl(1,7) = 16x16 real matrix algebra so Cellular Automata correspondence with Cl(8) means that any Real Clifford Algebra can be described by Cellular Automata. Therefore Clifford Algebra E8 physics can also be seen in terms of Cellular Automata.

Each initial state for a CA rule for 1-dim nearest neighbor automata is a triple * * * in which each of the 3 * (left, middle, right) can be either 0 or 1. Each CA rule gives one of 2 outcomes 0 or 1 for each of the 8 states

so there are $2^8 = 256$ possible CA rules. The 8 states correspond to the 8 vectors of the Clifford Algebra Cl(8)

The CA rule that gives 0 for all 8 states corresponds to the 1 scalar 0-vector of CI(8) There are 8 CA rules that give 1 for one of the 8 states and 0 for the other 7 and they correspond to the 8 vectors of CI(8)

There are 28 CA rules that give 1 for 2 of the 8 states and 0 for the other 6 and they correspond to the 28 bivectors of Cl(8)

There are 56 CA rules that give 1 for 3 of the 8 states and 0 for the other 5 and they correspond to the 56 3-vectors of Cl(8)

There are 70 CA rules that give 1 for 4 of the 8 states and 0 for the other 4 and they correspond to the 70 4-vectors of Cl(8)

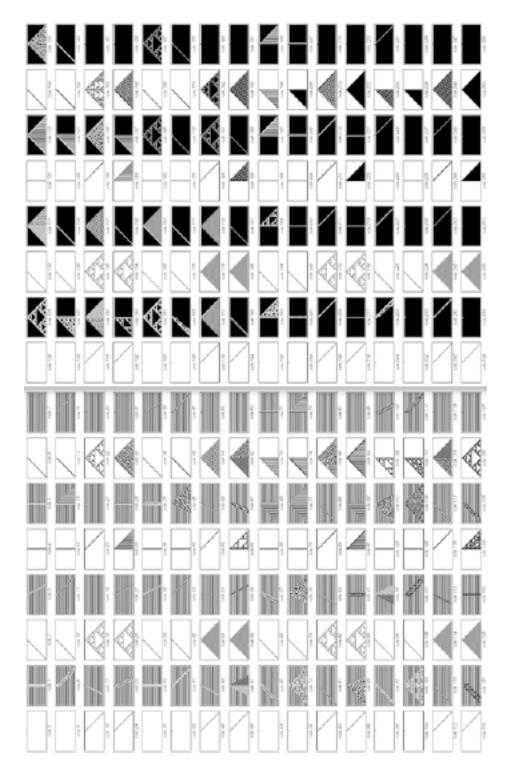
There are 56 CA rules that give 1 for 5 of the 8 states and 0 for the other 3 and they correspond to the 56 5-vectors of Cl(8)

There are 28 CA rules that give 1 for 6 of the 8 states and 0 for the other 2 and they correspond to the 28 6-vectors of Cl(8)

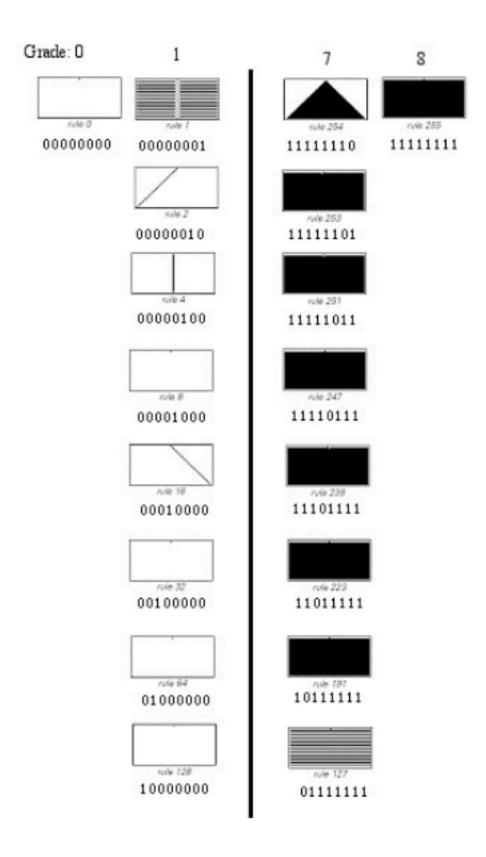
There are 8 CA rules that give 1 for 7 of the 8 states and 0 for the other 1 and they correspond to the 8 7-vectors of Cl(8)

There is 1 CA rule that gives 1 for all 8 states

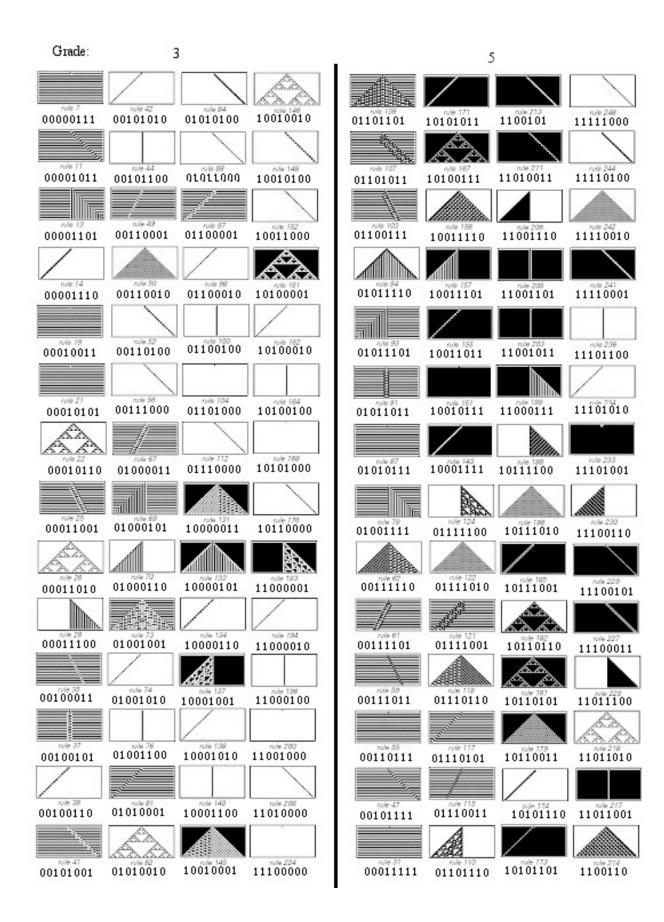
and it corresponds to the 1 pseudo-scalar 8-vector of Cl(8)



256 Cellular Automata 1 8 28 56 70 56 28 8 1 (images from "A New Kind of Science" by Stephen Wolfram (Wolfram 2002))



Grade:		2		6	
00000011	00010010	00110000	nde 129 1 00000001]
nde 5 00000101	nulo 20 00010100	7.00 65 01 000001	//// 130 10000010]
	00011000	nule 66 01000010	role 132 10000100	nule 123 01111011 1011101 11100111 111001	
лю в 00001001	nie 33 00100001	nule 68 01000100	nale 136 10001000	01110111 10111 1011 1011 1011 1011	
rule 10 00001010	00100010	01001000	nule 144 10010000	Image: 100 million Image:	
nule 32 00001100	nde 36 00100100	01010000	nule 160 10100000	nule 36 01011111 10101111 101011 1011 111 0011	
AND 17 00010001	00101000	Note 95 01100000	nile 192 11000000	nule 63 00111111 10011111 11010111 11010111	



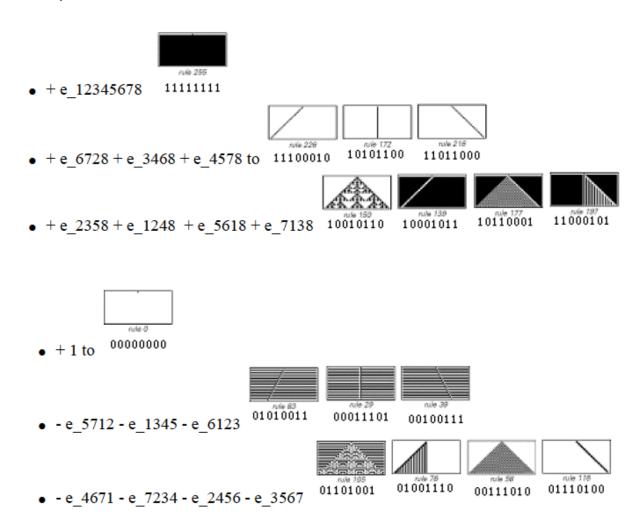
]
)
0

the 16 terms in the Cl(8) primitive idempotent

$$f = (1/2)(1 + e_{1248})(1/2)(1 + e_{2358})(1/2)(1 + e_{3468})(1/2)(1 + e_{4578}) =$$

=(1/16)(1 + e_1248 + e_2358 + e_3468 + e_4578 + e_5618 + e_6728 + e_7138 - e_3567 - e_4671 - e_5712 - e_6123 - e_7234 - e_1345 - e_2456 + e_J)

correspond to 16 of the 256 Cellular Automata

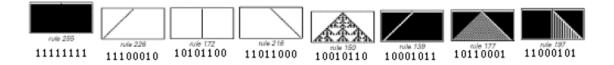


Note the Cl(0,8) = Cl(1,7) triality correspondences among:

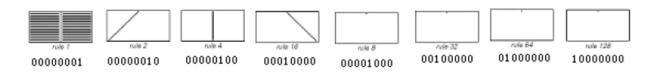
• the 8 <u>+half-spinors</u>



• the 8 -half-spinors

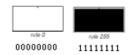


• the 8 vectors



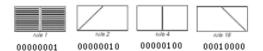
Note that:

the grade-0 scalars



are related to the Spinors and Primitive Idempotents of Cl(0,8);

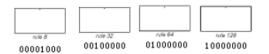
the grade-1 vectors 1, 2, 4, 16 (the subset sequence $2^{0} = 1$, $2^{1} = 2$, $2^{2} = 4$, $2^{4} = 16$ related to Fermat primes)



correspond to the 4 dimensions of physical spacetime;

- o 1 gives a succession of bands, the procession of time;
- o 2 gives a slope to the left, one of three space dimensions;
- o 4 gives a vertical slope, a second of three space dimensions;
- o 16 gives a slope to the right, the third of three space dimensions;

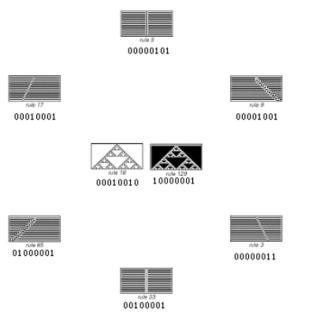
the grade-1 vectors 8, 32, 64, 128 (all giving all white)



correspond to the 4 dimensions of internal symmetry space;

- rule 18 = 00010010 is the first rule to include both 16 = 00010000 with right slope and 2 = 00000010 with left slope and is the first rule with traingular self-similar fractal structure;
- rule 30 = 00011110 is the first rule to include 16, 8, 4, and 2 and is in the self-dual grade-4 and is the first rule with triangular chaotic behavior.

8 of the grade-2 bivectors,



after <u>dimensional reduction to 4-dimensional physical spacetime</u>, correspond to <u>the 8 generators of color force SU(3)</u>, <u>whose root vector diagram</u> is illustrated above;

3 of the grade-2 bivectors,



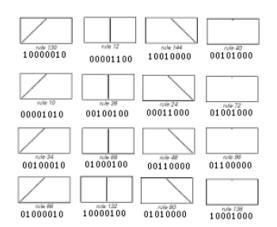
after dimensional reduction to 4-dimensional physical spacetime, correspond to the 3 generators of weak force SU(2);

1 of the grade-2 bivectors,



after <u>dimensional reduction to 4-dimensional physical spacetime</u>, correspond to <u>the 1 generator of electromagnetic</u> <u>U(1);</u>

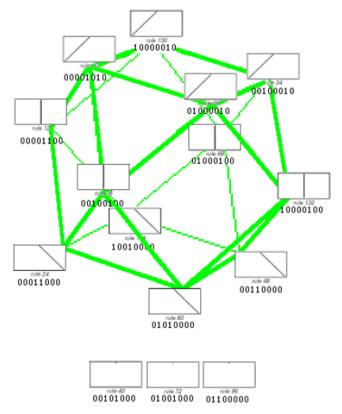
16 of the grade-2 bivectors,



after <u>dimensional reduction to 4-dimensional physical spacetime</u>, correspond to <u>the 16 generators of</u> <u>Gravity/Higgs/phase U(2,2)</u>. One of them

corresponds to the propagator phase U(1) while the other 15 correspond to the <u>Conformal</u> Group SU(2,2) = Spin(2,4) whose root vector diagram

nule 738 10001000



is a 12-vertex cuboctahedron (the other 3 bivectors corresponding to the 3 generators of the Cartan Subalgebra).

Appendix - Conformal Penrose Tiling, E6, and E8 Physics

Abstract

E8 Physics (viXra 1602.0319) is based on the 240 Root Vectors of E8 which E8 is contained in Cl(16) the completion of the union of all tensor products of which gives a generalized Hyperfinite II1 von Neumann factor AQFT with underlying Lagrangian structure given by the 240 Root Vectors of E8. E6 subalgebra of E8 with 72 Root Vectors describes a Complex version of Octonionic E8 Physics which describes Physics of Conformal Penrose Tiling such as described by Maria Ramirez-Solano in arXiv 1303.2000. Klee Irwin (quantumgravityresearch.org) has the idea that Penrose Tiling can encode the Hydrogen Spectrum, such as the Lyman series, using the STAR Penrose Tiling The relationship of the Hydrogen Lyman spectrum to the STAR Penrose Tiling may be explained by the facts that the pattern of the STAR Penrose Tiling is very similar to that of the Conformal Penrose Tiling and that the Conformal Group is the symmetry group of the Hydrogen Atom.

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Hydrogen Atom ... page 20

O. P. Shcherbak in Uspekhi Mat. Nauk 43:3 (1988) 125-160 said: "...

The non-standard representations of the groups H_2 , H_3 , H_4 are obtained if in the definition of the sets of generating mirrors the angle $\pi/5$ is replaced by the angle $2\pi/5$. The images of these representations are clearly reflection groups of the same name, the non-equivalence to the standard representation showing up by comparing the characters over (or under) the group H_2 .

The same applies to the groups $I_2(p)$, $p \ge 7$, where the number of nonequivalent representations acting like $I_2(p)$ is equal to the number of values $i, 1 \le i \le p/2$, mutually prime to p.

The main result of the present section is the establishment of a relation between the groups H_2 , H_3 , H_4 and the groups A_4 , D_6 , E_8 , respectively (Fig. 4). More precisely, the Coxeter groups H_2 , H_3 , H_4 are determined by the groups A_4 , D_6 , E_8 , the standard representations of the latter determining both the non-equivalent representations of the former.

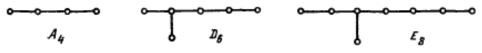


Fig. 4. The Coxeter graphs A4, D6, E8

We draw the Coxeter graphs of the groups A_4 , D_6 , E_8 as shown in Fig. 5.

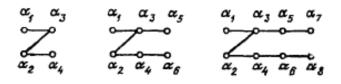


Fig. 5. Folding the graphs A_4 , D_6 , $E_8 \rightarrow H_2$, H_3 , H_4

Latham Boyle and Paul J. Steinhardt in arXiv 1608.08215 said "...

the Ammann pattern is a quasicrystal tiling in its own right, since the Ammann lines/ planes/hyperplanes divide up space into a finite number of polytopes arranged quasiperiodically in a crystallographically forbidden pattern ...

While a Penrose-like tiling has the simplifying property that all the edge lengths of all the tiles are the same, an Ammann pattern (regarded as a tiling) has the simplifying property that ... all the codimension-one tile "faces" join up to form infinite unbroken codimension-one affine spaces ... the Ammann pattern with orientational symmetry G is in many ways the simplest type of quasicrystal with orientational symmetry G. In particular, as far as we are aware, the Ammann pattern is the only type of quasicrystal (with orientational order G) that can be explicitly described by a closed-form analytic expression. The same is true for its diffraction pattern ...

quasicrystalline order with orientational symmetry G ... may be built up from (or decomposed into) 1D quasiperiodic constituents ... all of the different Ammann patterns (regardless of their symmetry or dimension) are described by essentially the same formula, so that the higher-dimension or higher-symmetry cases are no more complicated than the original one ...

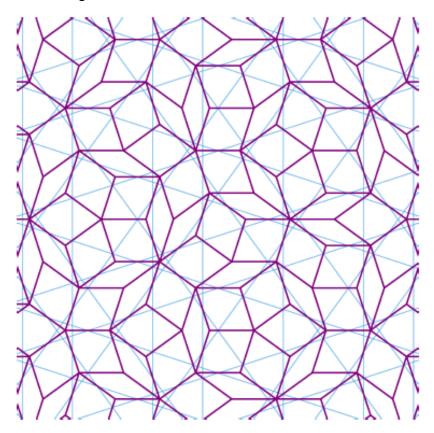


Figure 1: The thick purple lines show a portion of a Penrose tiling, while the thin blue lines show the corresponding Ammann pattern. Note that the Penrose tiling is built from two prototiles – a thin (36°) rhomb and a fat (72°) rhomb; and both prototiles are always decorated by the same characteristic pattern of Ammann lines.

the original Penrose tiling [Penrose STAR] ... in 2D, with 10-fold symmetry ... [corresponds to]

the non-crystallographic root system I^5_2 [designated as H2 by Shcherbak] which is paired with the crystallographic root system A4 ...[has] field extension ... Q(sqrt(5))

a Penrose tiling [can] ... be obtained by dualizing an Ammann (penta-)grid ... Consider an Ammann pattern in which the Ammann planes are arrayed along the J different directions ... These planes slice up d-dimensional Euclidean space into open ddimensional regions ("cells"). To each cell, we assign a set of J integer coordinates ... the cell lies between the hyperplanes labelled nj and nj + 1 ... The dualization procedure maps each cell in the Ammann pattern to a vertex in the corresponding Penrose tiling ...

non-crystallographic root system θ^{\parallel}	crystallographic partner θ	degree $N=d/d^{\parallel}$
$I_2^p \ (p \text{ any prime} \ge 5)$	A_{p-1}	(p-1)/2
$I_2^{2^m}$ (<i>m</i> any integer ≥ 3)	B_{2m-1}/C_{2m-1}	2^{m-2}
I_{2}^{12}	F_4	2
I_{2}^{30}	E_8	4
H_3	D_6	2
H_4	E_8	2

Table 2: The complete list of Coxeter pairs.

...

non-crystallographic root system θ_{\parallel}	crystallographic partner θ	field extension $\mathbb K$
I_2^5	A_4	$\mathbb{Q}(\sqrt{5})$
I_{2}^{8}	B_4/C_4	$\mathbb{Q}(\sqrt{2})$
I_{2}^{12}	F_4	$\mathbb{Q}(\sqrt{3})$
H_3	D_6	$\mathbb{Q}(\sqrt{5})$
H_4	E_8	$\mathbb{Q}(\sqrt{5})$

Table 3: Quadratic (N = 2) Coxeter pairs and their corresponding field extensions.

...".

Latham Boyle and Paul J. Steinhardt in arXiv 1608.08220 said "...

The Penrose tiles also have [an]... important feature:

the two tiles can each be decorated with a certain pattern of line segments that join together in a perfect Penrose tiling to form five infinite sets of parallel lines oriented along the five edges of a pentagon. The lines are spaced according to a 1D quasiperiodic sequence of long and short intervals called a "Fibonacci quasilattice" ... The five sets of 1D quasilattices collectively form an Ammann pattern

a Penrose-like tiling should be regarded as the dual of a more fundamental object: an Ammann pattern;

and this Ammann pattern, in turn, can be derived from the relationship between two naturally-paired irreducible reflection groups (which we call a "Coxeter pair")

Our focus in this paper is the analysis of the 1D quasilattices that serve as the building blocks for the Ammann patterns in higher dimensions ...

Although our ultimate purpose is higher-dimensional quasicrystal tilings ...

the 1D quasilattices studied here are important objects in their own right

•••

...

"1D quasilattices of degree two" or "quadratic 1D quasilattices". These are 1D quasiperiodic lattices constructed from just two intervals or "tiles" (call them L and S, for "long" and "short"), with just two different separations between successive L's, and just two different separations between successive S's (the simplest possibility compatible with quasiperiodicity) ...

In a generic (non-singular) self-similar quasilattice,

the line ... does not intersect any of the points in the lattice ...

•••

we identify the subset of quadratic 1D quasilattices that are not only self-similar under some 2 x 2 transformation T , but are exactly s-fold self-same;

that is, T^s maps the quasilattice xn to a new quasilattice x'n that is not merely locallyisomorphic, but actually identical to the original quasilattice (up to an overall rescaling)

[Case	λ_{\pm}	au	m_2^{\pm}/m_1^{\pm}	S'	L'
	1	$\frac{1}{2}(1\pm\sqrt{5})$	$\begin{pmatrix} 0 & 1 \\ 1 & 1 \end{pmatrix}$	$\frac{1}{2}(1\pm\sqrt{5})$	$\frac{L}{2}\frac{L}{2}$	$\frac{L}{2}S\frac{L}{2}$

for ... the special quasi-lattice ... where the scaling factor is the "golden ratio" ...

In this table, we use the convenient notation λ_{\pm}

and m_i^{\pm} where here the superscript/subscript "+" stands for the former subscript/superscript "||", while the "-" stands for " \perp ".

... which is the relevant case for ... systems with 5-fold or 10-fold [H2] order in 2D, some systems with icosahedral (H3) order in 3D,

and systems with with "hyper-icosahedral" (H4) order in 4D ...

we count the number of irreducible s-cycles ...

8	F_s^2	$\langle N_s \rangle / s$
1	1	0
2	1	1
3	2	1
4	3	1
5	5	2
6	8	2
7	13	4
8	21	5
9	34	8
10	55	11
11	89	18
12	144	25

Here we list tabulate the first 12 terms

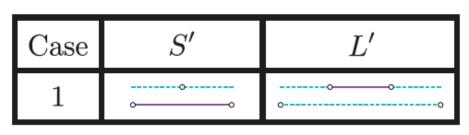
in the sequence F_s and the sequence $\langle N_s \rangle / s$,

for $\phi = (1 + \sqrt{5})/2$ (columns 1 and 2)

... the sequences of numbers ... appear as entries in the Online Encyclopedia

of Integer Sequences (OEIS) ...

The first column is OEIS sequence A000045 ("Fibonacci numbers"); the second column is A006206 ("Number of aperiodic binary necklaces of length n with no subsequence 00, excluding the necklace "0")



1D self-similar substitution rules relevant to constructing higherdimensional Ammann patterns and Penrose-like tilings

the short (solid, purple) and long (dashed, turqoise) prototiles are on the bottom, with their corresponding self-similar decimations into smaller tiles directly above.

Open circles indicate the endpoints of tiles. Complete tiles have have circles at both ends; half tiles have a circle at one end but none at the half-way point.

For example, Row 1 shows how

a short prototile S^\prime (bottom left) is subdivided into two halves of a long prototile:

S' = (L/2)(L/2) (top left);

and a long prototile L' (bottom right) is subdivided into L' = (L/2)S(L/2) (top right).

...".

Latham Boyle and Paul J. Steinhardt in arXiv 1608.08215 said "...

a Coxeter pair ... a non-crystallographic reflection group (of lower rank) has a natural crystallographic partner (of higher rank) ...

The H4 (4D hyper-icosahedral) tiling

Here the relevant Coxeter pair is ... { H4 , E8 }. The E8 root system has 240 roots: all 128 vectors of the form (1=2)(+/-1, +/-1, +/-1, +/-1, +/-1, +/-1, +/-1) (with an even number of minus signs),

along with all 112 vectors of the form (+/-1, +/-1, 0, 0, 0, 0, 0, 0, 0) (including all sign combinations and permutations of the coordinates) ... the 240 E8 roots project ... to yield two copies of the 120 H4 roots (an inner copy and an outer copy that is longer by [the Golden Ratio]) ... the minimal star ... is a 120-pointed star pointing towards the vertices of the 600-cell ... the unique reflection quasilattice corresponding to H4 is the H4 root quasilattice (i.e. the set of all integer linear combinations of the H4 roots) ...

there is a unique 4D space group corresponding to (the unique irreducible noncrystallographic roots system) H4

[The Coxeter group of H4 is of order 14,400 and contains 60 reflections, according to James E. Humphreys in his book Reflection Groups and Coxeter Groups]

The H3 (3D icosahedral) tilings ...

Here the relevant Coxeter pair is ... { H3 , D6 }. The D6 root system has 60 roots: all vectors obtained from (+/-1 , +/-1 , 0 , 0 , 0 , 0) by allowing all combinations of signs and all permutations of the coordinates ... the 60 D6 roots project to two copies of the 30 H3 roots (an inner copy and an outer copy that is longer by [the Golden Ratio] ... the 12 faces of the 6-cube in 6D ... are project[ed] ... to ... the 12 vertices of the icosahedron in 3D

•••

[The Coxeter group of H3 is of order 120 and contains 15 reflections, according to James E. Humphreys in his book Reflection Groups and Coxeter Groups] ...

the minimal star ... is a 12-pointed star pointing towards the vertices of the icosahedron ...

[the] Ammann pattern and Penrose tiling with [Golden Ratio (1/2)(1 +/- sqrt(5))] scaling ... is precisely the icosahedral tiling found by Socolar and Steinhardt in [1986] ...

The I_2^5 [H2] (2D 10-fold) tiling

Here the relevant Coxeter pair is ... { I_2^5 [H2], A4 }. The A4 root system has 20 roots: all vectors obtained from (+1, -1, 0, 0 } by allowing all permutations of the coordinates ...

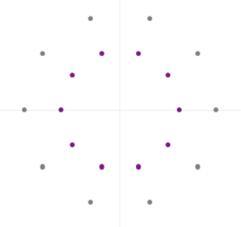


Figure 6: The 20 roots of A_4 , projected onto the Coxeter plane.

the underlying star ... points to the 5 vertices of a regular pentagon ...

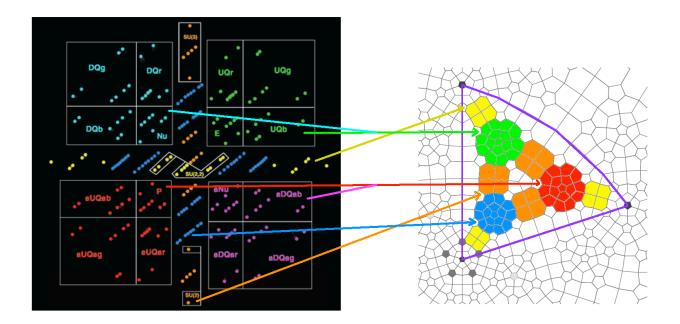
this case ... precisely recovers the original 10-fold Penrose tiling, with its standard Ammann decoration and inflation rule ...".

•••

E8 Root Vectors and E6 in Conformal Penrose Tiling

E8 Physics (viXra 1602.0319) is based on the 240 Root Vectors of E8 which E8 is contained in Cl(16) the completion of the union of all tensor products of which gives a generalized Hyperfinite II1 von Neumann factor AQFT with underlying Lagrangian structure given by the 240 Root Vectors of E8.

E6 subalgebra of E8 with 72 Root Vectors describes a Complex version of Octonionic E8 Physics which describes Physics of Conformal Penrose Tiling. Mapping of the 240 E8 Root Vectors to the 72 E6 Root Vectors



is 4 to 1 for 64 + 64 + 64 of E8 to 16 + 16 + 16 of E6 and 2 to 1 for 24 + 24 of E8 to 12 + 12 of E6 In arXiv 1303.2000 Maria Ramirez-Solano said:

"... The conformally regular pentagonal tiling of the plane ... The goal is to describe this tiling as a conformal substitution tiling, i.e. a tiling generated by a substitution rule with complex scaling factor > 1 and a finite number of prototiles, where each prototile is substituted with "extended-conformal" copies of the prototiles ...

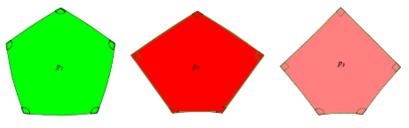
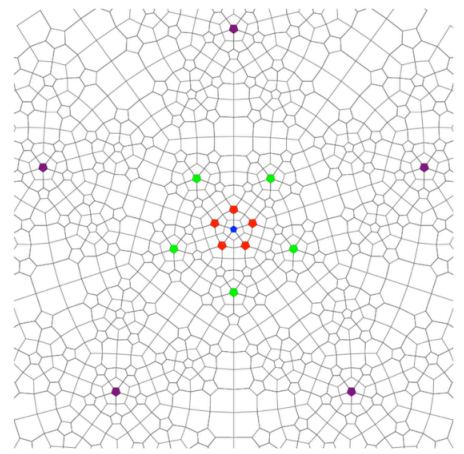


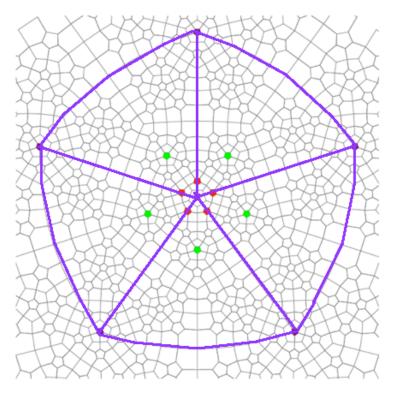
FIGURE 7. The prototiles of T. The interior angles are either $\pi/2$ or $2\pi/3.$

... We can construct a tiling ... where the tiles are ... conformally regular pentagons, and the tiling looks like



... The article "A regular pentagonal tiling of the plane" by Philip L. Bowers and Kenneth Stephenson in [22] gives a construction of this tiling using the theory of circle packings on the above combinatorics. They use circle packings to impose a natural geometry on the above combinatorics ...".

The central part of the tiling has 5 pentagonal sectors

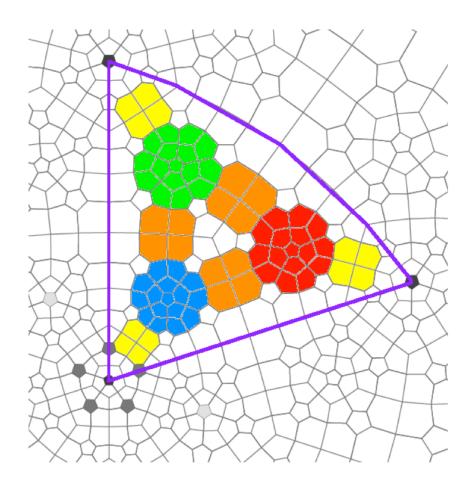


Each of the 5 pentagonal sectors of the tiling contains a 2-dim projected version of the 8-dim E8 Root Vector structure of E8 Physics corresponding to the Complex E6 subalgebra of Octonionic E8. The outer boundary of each sector is not a straight line but is curved with Conformal Symmetry and pentagonal sectors further out are conformally curved rather than straight-line pentagons.

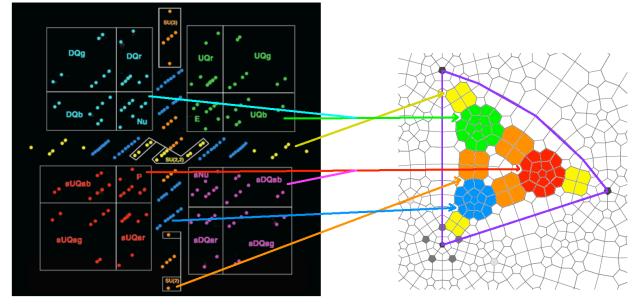
Each pentagonal sector represents the Complex part of Octonionic E8 Physics whose 240 E8 Root Vectors project to the 72 Root Vectors of E6 subalgebra of E8 which 72 E6 Root Vectors have the following physical interpretation

16 = 2x8 of which represent Complex Fermion Particles
16 = 2x8 of which represent Complex Fermion AntiParticles
16 = 2x(4+4) of which represent Complex (4+4)-dim Kaluza-Klein SpaceTime
12 of which represent the Standard Model
12 of which represent Gravity + Dark Energy

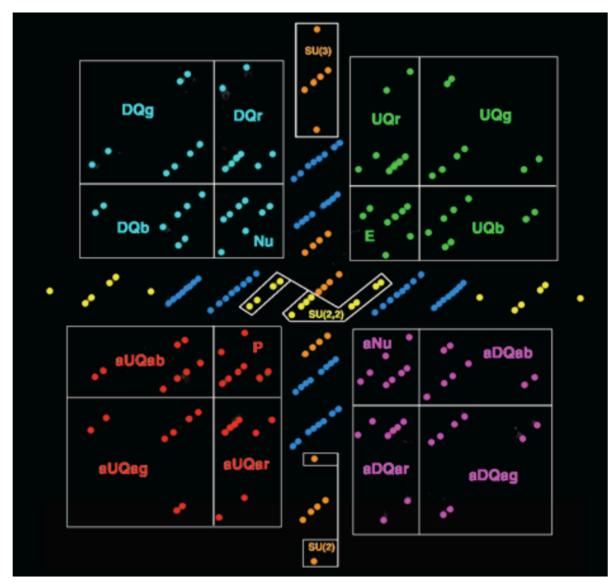
as shown in the following image of one of the pentagonal sectors:



The 240 E8 Root Vectors correspond to the 72 E6 Root vectors by a 4 to 1 map for 64 + 64 + 64 of E8 to 16 + 16 + 16 of E6 and a 2 to 1 map for 24 + 24 of E8 to 12 + 12 of E6



Here are more details of the E8 Root Vector Physical interpretations:



E = electron, UQr = red up quark, UQg = green up quark, UQb = blue up quark Nu = neutrino, DQr = red down quark, DQg = green down quark, DQb=blue down quark P = positron, aUQar = anti-red up antiquark,

aUQag = anti-green up antiquark, aUQab = anti-blue up antiquark

aNu = antineutrino, aDQar = anti-red down antiquark,

aDQag = anti-green down antiquark, aDQab = anti-blue down antiquark

Each Lepton and Quark has 8 components with respect to 4+4 dim Kaluza-Klein

6 orange SU(3) and 2 orange SU(2) represent Standard Model root vectors

24-6-2 = 16 orange represent U(2,2) Conformal Gravity Ghosts

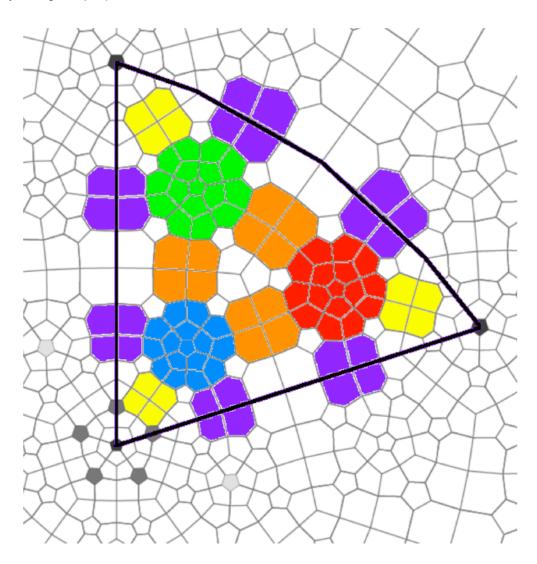
12 yellow SU(2,2) represent Conformal Gravity SU(2,2) root vectors

24-12 = 12 yellow represent Standard Model Ghosts

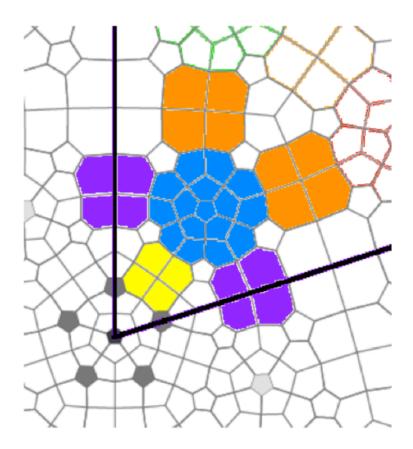
32+32 = 64 blue represent 4+4 dim Kaluza-Klein spacetime position and momentum

Connectors

In addition to the 72 E6 Root Vector tiles within a Pentagonal Sector there are 3 sets of 8 tiles (purple) that connect that Pentagonal Sector with an adjoining Pentagonal Sector. Those 3x8 = 24 tiles represent the Root Vectors of a D4 = Spin(8) Lie Group of rotations in the 8-dim space of the E8 Lattice that is projected into the plane of the Conformal Penrose Tiling, which give the directions of connections of the projected 240-vertex E8 Polytope with adjoining Polytopes of the E8 Lattice.



Each of the 3 vertices of the Pentagonal Sector is associated with 28 of the 72 E6 Root Vectors and 8 of the 24 Pentagonal Sector Connectors



in a Pentagonal Sector Vertex Configuration.

Collared Tiles and Dynamical Systems

In arXiv 1303.2000 Maria Ramirez-Solano said:

"... A group action is a triple (**X**,**G**, **P**) composed of a topological space **X**, an Abelian group **G**, and an action map **P** : **X** Å~ **G** \rightarrow **X** defined by **P**_g : **X** \rightarrow **X**, which is a homeomorphism for every **g** \in **G**,

and $\mathbf{P}_0 = \mathbf{id}$ and $\mathbf{P}_g \circ {}_h = {}_{g+h}$ for every $g, h \in G$.

A dynamical system is a group action ((X, d), G, P), where (X, d) is a compact metric space called the phase space, and the group action P is continuous. For short we write (X,G) instead of ((X, d), G, P). The study of the topological properties of dynamical systems is called topological dynamics, and the study of the statistical properties of dynamical systems is called ergodic theory. ...

The orbit set of a tiling **T** is defined by

$O(\mathbf{T}) := \{\mathbf{T} + \mathbf{x} \mid \mathbf{x} \in \mathbf{R}_2\},\$

where $T + x := \{t + x \mid t \in T\}$. The group R_2 acts on the orbit set O(T) of a tiling T by translation, for if T' is in the orbit set, then so is T' + x for all $x \in R_2$.

The orbit set O (**T**) is equipped with a metric **d** : O (**T**) x O (**T**) \rightarrow [0, ∞ [defined by d (T, T') < 1/r if there is **x**, **x**' \in **B**_{1/r} (0) such that (**T** - **x**) \cap **B**_r (0) = (**T**' - **x**') \cap **B**_r (0) i.e. if they agree on a ball of radius **r** centered at the origin up to a small wiggle ... The continuous hull W_T of a tiling **T** is defined as

the completion of the metric space (O (T), d)

····

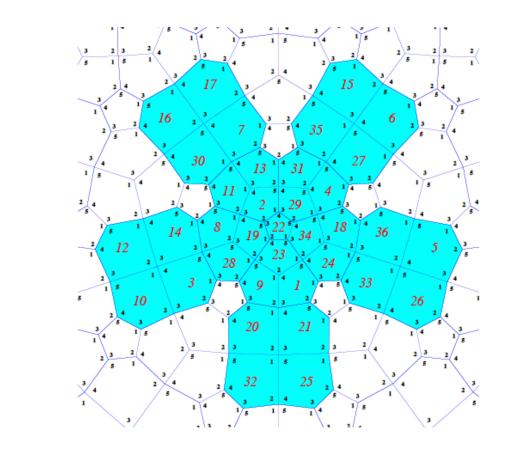
The same definition of **d** extends to W_T , and (W_T, d) is a metric space. The group \mathbf{R}_2 acts also on the hull by translation, for if **T**' is in W_T then so is $\mathbf{T}' + \mathbf{x}$ for any $\mathbf{x} \in \mathbf{R}_2 \dots$ A patch P is a finite subset of a tiling **T**. A tiling satisfies the finite local complexity (FLC) if for any $\mathbf{r} > 0$ there are finitely many patches of diameter less than \mathbf{r} up to a group of motion **G**, usually translation. The finite local complexity (FLC) is also called finite pattern condition ... if a tiling **T** satisfies the FLC condition then the metric space (W_T , **d**) is compact. Hence, if a tiling **T** satisfies the FLC condition, then (W_T , \mathbf{R}_2) is a topological

dynamical system. The action $\mathbf{P} : W_T \times \mathbf{R}_2 \rightarrow W_T$ given by $\mathbf{P}_x (\mathbf{T}') := \mathbf{T}' + \mathbf{x}$ is continuous by definition of the metric. ...".

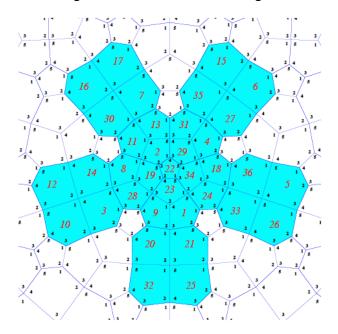
In arXiv 1304.2652 Maria Ramirez-Solano said:

"... For an aperiodic FLC Euclidean substitution tiling of the plane, there is a recipe for writing its continuous hull as an inverse limit ...

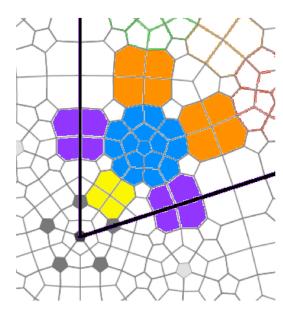
In [arXiv 1303.5676] we constructed a compact topological space for the combinatorics of "A regular pentagonal tiling of the plane", which we call the continuous hull. We also constructed a substitution map on the space which turns out to be a homeomorphism, and so the pair given by the continuous hull and the substitution map yields a dynamical system. In this paper we show how we can write this dynamical system as another dynamical system given by an inverse limit and a right shift map ... If we can label the tiles of a tiling not only by their own type but by the pattern of their nearest neighbors, then we call such labels collared tiles ...



The Pentagonal Sector Vertex Configurations are Collared Tiles:



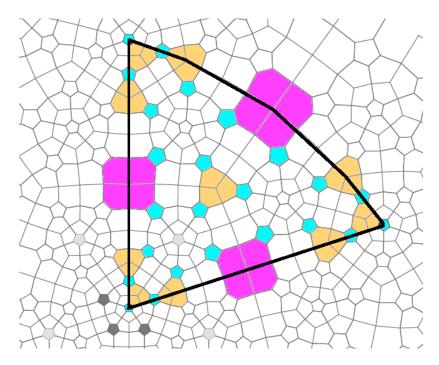
..."



Outer Automorphisms Triality, Connectors, and Bohm Quantum Potential

Raymond Ascheim asked

about physical interpretation of the remaining Tiles in a Pentagonal Sector



My view is that they are analogous to the Triality of D4 = Spin(8), that is, that they represent Outer Automorphisms of the E8 Physics Structure:

The yellow Tiles are in 3-fold configurations and are directly related to Triality such as

the central 3 Tiles representing Triality among the 3 Pentagonal Sector Configurations.

The magenta Tiles represent

isomorphisms of pairs of Pentagonal Sector Configurations and Connectors to pairs in adjoining Pentagonal Sectors.

The 15+9 = 24 cyan Tiles represent the Bohm Quantum Potential in this way: Joe Polchinski in "String Theory, Volume 1, An Introduction to the Bosonic String" said: "... we find at m² = - 4 / alpha' the tachyon,

and at $m^2 = 0$ the 24 x 24 states of the graviton, dilaton, and antisymmetric tensor ...". In my view, the 24x24 states are represented by the 24 cyan tiles

as an Outer Automorphism - type symmetry of an E8 Physics String Theory based on Strings being physically interpreted as World-Lines of Particles -

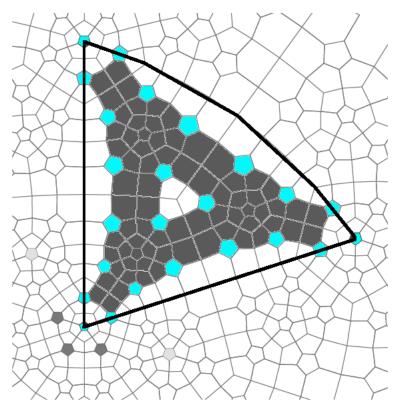
see viXra 1602.0319 especially page 229 and following pages -

and the 24x24 traceless symmetric spin-2 particle that Polchinski calls "graviton" is in reality the carrier of the Bohm Quantum Potential.

Here are some more details of how the Bohm Quantum Potential works:

In each Pentagonal Sector of the Conformal Penrose Tiling,

the 72 dark gray E6 Root Vector tiles contain the projection of all 240 E8 Root Vectors (48 tiles get 4x48 = 192 E8 Root Vectors and 24 tiles get 2x24 = 48 E8 Root Vectors)



and the 24 cyan tiles represent the 24 dimensions of the Little Group subgroup of the Lorentz group of 26-dim Bosonic String Theory with Strings interpreted as World-Lines of the Particles of E8 Physics. Joe Polchinski in "String Theory, Volume 1, An Introduction to the Bosonic String" said: "... we find at $m^2 = -4$ / alpha' the tachyon, and at $m^2 = 0$ the 24 x 24 states of the graviton, dilaton, and antisymmetric tensor ..." with dilaton being 24x24 trace and graviton being 24x24 traceless symmetric matrices. My physical interpretation differs from Polchinski's, as I see the 24 x 24 traceless symmetric matrices as the carrier of Bohm Quantum Potential.

"... Bohm's Quantum Potential can be viewed as an internal energy of a quantum system ..." according to Dennis, de Gosson, and Hiley (arXiv 1412.5133) and Peter R. Holland says in "The Quantum Theory of Motion" (Cambridge 1993): "... the total force ... from the quantum potential ... does not ... fall off with distance ... because ... the quantum potential ... depends on the form of ...[the quantum state]... rather than ... its ... magnitude ...".

The Bohm Quantum Potential connects physical E8 Physics configurations

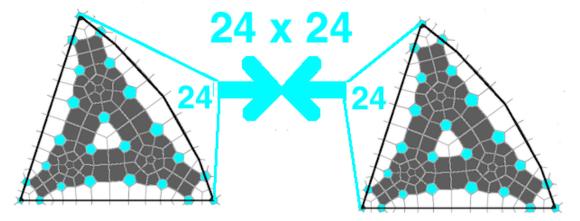
with each other using Resonance. Resonance is discussed by Carver Mead in "Collective Electrodynamics" (MIT 2000):

"... we can build ... a resonator from ... electric dipole ... configuration[s] ... [such as Tubulin Dimers] Any ... configuration ... couples to any other on its light cone, whether past or future. ... The total phase accumulation in a ... configuration ... is the sum of that due to its own current, and that due to currents in other ... configurations ... far away ...

The energy in a single resonator alternates between the kinetic energy of the electrons (inductance), and the potential energy of the electrons (capacitance). With the two resonators coupled, the energy shifts back and forth between the two resonators in such a way that the total energy is constant ... The conservation of energy holds despite an arbitrary separation between the resonators ... Instead of scaling linearly with the number of charges that take part in the motion, the momentum of a collective system scales as the square of the number of charges! ... it is clear that collective quantum systems do not have a classical correspondence limit. ...".

The Bohm Quantum Potential interacts between two Pentagonal Sectors by 24 Bohm Carrier Tiles of one Pentagonal Sector carrying E8 Configuration Information and comparing it with

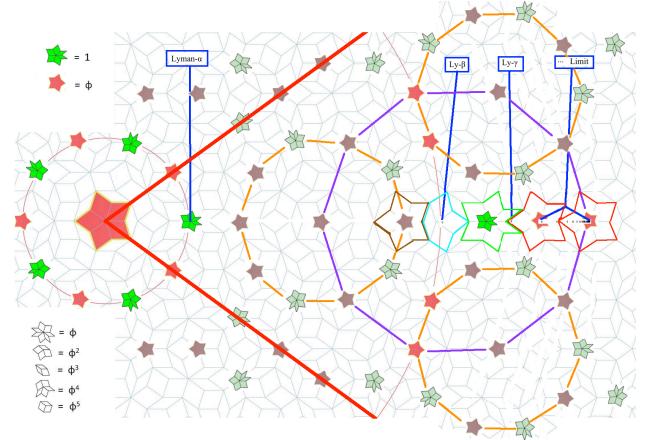
24 Bohm Carrier Tiles of the Other Sector carrying E8 Configuration Information. If the resulting 24×24 Matrix shows that the two E8 Configurations are similar, then a Bohm Quantum Potential Resonant Connection is established.



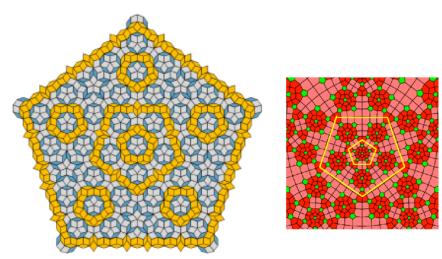
The Bohm Quantum Potential 24x24 Matrix is traceless because Configuration Resonance is sensitive to similarity rather than dilation scale and is symmetric because Configuration Resonance is symmetric between Sectors.

Hydrogen Atom

Klee Irwin (quantumgravityresearch.org) has the idea that Penrose Tiling can encode the Hydrogen Spectrum, such as the Lyman series, using the STAR Penrose Tiling



The relationship of the Hydrogen Lyman spectrum to the STAR Penrose Tiling may be explained by the facts that the pattern of the STAR Penrose Tiling is very similar to that of the Conformal Penrose Tiling



and that the Conformal Group is the symmetry group of the Hydrogen Atom.

Appendix - Tetrahedra and E8 Physics

The simplest polyhedron in 3-dim Flat Space is the Tetrahedron. You can combine Tetrahedra in 3-dim Flat Space but to avoid gaps in the combined structure you must curve 3-dim Space and effectively go to 4-dim Space to build 600-cell {3,3,5} polytopes two of which can be combined to produce the 240-polytope that leads to the 8-dim Gossett polytope of the E8 Lie Algebra of Cl(16)-E8 Physics whose AQFT therefore corresponds to a 4D Feynman Checkerboard Quantum Theory constructed with Tetrahedra-based structures.

If you do not curve the 3-dim space, there are two possibly useful structures:

Tetrahedral Clusters whose Periodicity corresponds to that of Real Clifford Algebras giving a correspondence with the AQFT of Cl(16)-E8 Physics

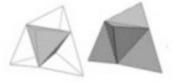
QuasiCrystals and their Approximants whose phason disorder seems to be a measure of an information deficit, and failure of equivalence, with respect to Cl(16)-E8 Physics.

The Wikipedia entry on the 600-cell says:

"... the 600-cell ... is the convex regular polytope ...]{3,3,5}. Its boundary is composed of 600 tetrahedral cells with 20 meeting at each vertex ... they form 1200 triangular faces, 720 edges, and 120 vertices. The edges form 72 flat regular decagons. Each vertex of the 600-cell is a vertex of six such decagons. ... Its vertex figure is an icosahedron ... It has a dihedral angle of 164.48 degrees. ...

Each cell touches, in some manner, 56 other cells.

[4+1 = 5] One cell contacts each of the four faces;

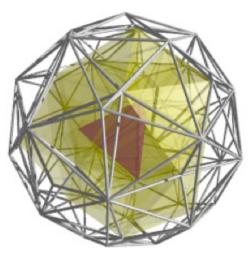


2x6 + 5 = 17] two cells contact each of the six edges, but not a face;



10x4 + 17 = 57] and ten cells contact each of the four vertices, but not a face or edge.

This image shows the 600-cell in cell-first perspective projection into 3D. ...



... The nearest cell to the 4d viewpoint is rendered in solid color,

lying at the center of the projection image.

The cells surrounding it (sharing at least 1 vertex) are rendered in transparent yellow.

[They are a 57G Maximal Contact Grouping]

The remaining cells are rendered in edge-outline.

Cells facing away from the 4D viewpoint have been culled for clarity. ...".

Sections of 600-cell

Sadoc and Mosseri in their book "Geometrical Frustration" (Cambridge 1999, 2006), say: "...

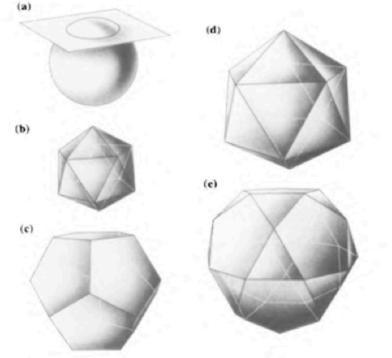


Fig. A5.1. The $\{3, 3, 5\}$ polytope. Different flat sections in S^3 (with one site on top) give the following successive shells; (a) an icosahedral shell formed by the first 12 neighbours, (b) a dodecahedral shell, (c) a second and larger icosahedral shell, (d) an icosidodecahedral shell on the equatorial sphere. Then other shells are symmetrically disposed in the second 'south' hemi-hypersphere, relative to the equatorial sphere (e).

- $\omega = \pi/2$: the 'equatorial' sphere is tiled by 30 vertices which form a regular icosidodecahedron. For larger values of ω , the situation is then symmetrical with respect to the equatorial sphere.
- $\omega = 3\pi/5$: an icosahedron.

 $\omega = 2\pi/3$: a dodecahedron.

 $\omega = 4\pi/5$: an icosahedron.

. . .

 $\omega = \pi$: one vertex at the south pole $x_0 = -R$, $x_1 = x_2 = x_3 = 0$.

Table A5.1. Sections of the {3, 3, 5} polytope (with an edge length equal to $2\tau^{-1}$) beginning with a vertex

Section	X_0	$(x_1, x_2, x_3)^{\dagger}$	Vertex number	Shape
0	2	(0, 0, 0)	1	point
1	τ	$(1, 0, \tau^{-1})$	12	icosahedron
2	1	(1, 1, 1)	20	dodecahedron
		$(\tau, \tau^{-1}, 0)$		
3	τ^{-1}	$(\tau, 0, 1)$	12	icosahedron
4	0	(2, 0, 0)	30	icosidodecahedror
		$(\tau, 1, \tau^{-1})$		
5	$-\tau^{-1}$	$(\tau, 0, 1)$	12	icosahedron
6	-1	(1, 1, 1)	20	dodecahedron
		$(\tau, \tau^{-1}, 0)$		
7	$-\tau$	$(1, 0, \tau^{-1})$	12	icosahedron
8	$^{-2}$	(0, 0, 0)	1	point

¹Cyclic permutation with all possible changes of signs. $\tau = (1 + \sqrt{5})/2$.

... Another ... description consists of fixing a polytope cell center at the north pole ...

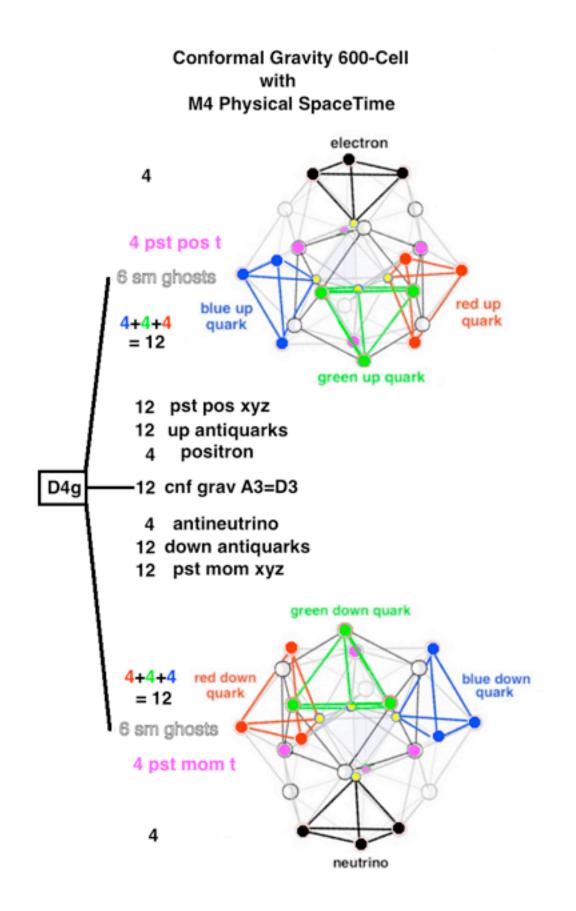
Table A5.2. Section of the {3, 3, 5} polytope (edge length $2\tau^{-1}\sqrt{2}$) beginning with a cell

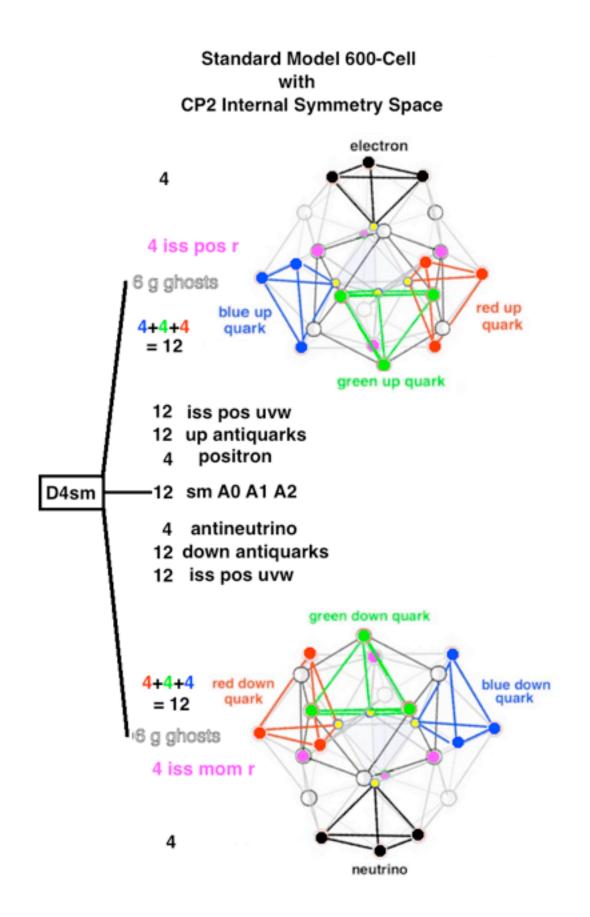
Section	x_0	(x_1, x_2, x_3)	Vertex number	Shape
0	τ^2	$(\tau^{-1}, \tau - 1, \tau^{-1})^{\dagger}$	4	tetrahedron
1	$\sqrt{5}$	$(au^{-1}, au - 1, au^{-1})^{\dagger} (-1, 1, 1)$	4	tetrahedron
2	2	(2, 0, 0)	6	octahedron
3	τ	(τ, τ, τ^{-2})	12	distorted
4	1	$(\sqrt{5}, 1, 1)$	12	cubo-octahedron
5	τ^{-1}	$(\tau^2, \tau^{-1}, \tau^{-1})$	12	
6	τ^{-2}	(τ, τ, τ)	4	tetrahedron
7	0	(2, 2, 0)	12	cubo-octahedron
8	$-\tau^{-2}$	$(-\tau, \tau, \tau)$	4	tetrahedron
-	_			
14	$-\tau^2$	$(-\tau^{-1}, \tau^{-1}, \tau^{-1})$	4	tetrahedron

Permutation with an even number of sign changes. $\tau = (1 + \sqrt{5})/2$. Distorted cubooctahedra are such that their square faces are changed into golden rectangles.

At the north pole and its antipodal south pole are Maximal Contact Groupings (57G) with 4+4+6+12 = 26 vertices.

...".





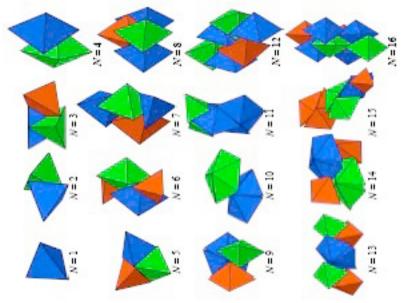
The 57G - 600-cell - 240 E8 construction with tetrahedra requires the initial flat 3-dim space to be curved

What happens if you require the 3-dim space to remain flat ?

If you construct with (exactly regular) tetrahedra in 3-dim space that remains flat that is like making a tetrahedral dense packing of flat 3-dim space.

The densest such packing now known is described by Chen, Engel, and Glotzer in arXiv 1001.0586 :

"... We present the densest known packing of regular tetrahedra with density Phi = 4000 / 4671 = 0.856347 ...



... The dimer structures are remarkable in the relative simplicity of the 4-tetrahedron unit cell as compared to the 82-tetrahedron unit cell of the quasicrystal approximant, whose density is only slightly less than that of the densest dimer packing. The dodecagonal quasicrystal is the only ordered phase observed to form from random initial configurations of large collections of tetrahedra at moderate densities. It is thus interesting to note that for some certain values of N, when the small systems do not form the dimer lattice packing, they instead prefer clusters (motifs) present in the quasicrystal and its approximant, predominantly pentagonal dipyramids. This suggests that the two types of packings - the dimer crystal and the quasicrystal/ approximant - may compete, raising interesting questions about the relative stability of the two very different structures at finite pressure. ...".

If you regard a Tetrahedron as a pair of Binary Dipoles

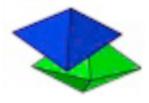


then the Chen - Engel - Glotzer high (0.85+) density configurations have the same 8-periodicity property as the Real Clifford Algebras:

#Binary Dipoles	Maximum Density		Success	Motifs,	
M	Numerical, $\hat{\phi}$	Analytical, ϕ	Rate	Structural Description	
2	0.367346	18/49	100%	1 monomer	
4	0.719486	ϕ_2	100%	2 monomers, transitive [22]	
6	0.666665	2/3	21%	3 monomers, three-fold symmetric	
8	0.856347	4000/4671	80%	2 dimers (positive + negative)	
10	0.748096	ϕ_5	22%	1 pentamer, asymmetric	
12	0.764058	ϕ_6	11%	2 dimers + 2 monomers	
14	0.749304	3500/4671	15%	2×2 dimers minus 1 monomer	
16	0.856347	4000/4671	44%	2×2 dimers, identical to $N=4$	
13	0.766081		-	1 pentagonal dipyramid + 2 dimers	
20	0.829282	ϕ_{10}	2%	2 pentagonal dipyramids	
22	0.794604		-	1 nonamer + 2 monomers	
24	0.856347	4000/4671	3%	3×2 dimers, identical to $N=4$	
26	0.788728		4%	1 pentagonal dipyramid + 4 dimers	
28	0.816834		3%	2 pentagonal dipyramids + 2 dimen	
30	0.788693		-	Disordered, non-optimal	
32	0.856342	4000/4671	< 1%	4×2 dimers, identical to $N=4$	
:	1				
164x8	0.850267			Quasicrystal approximant [21]	

The Binary Pair of one Tetrahedron corresponds to the Cl(2) Real Clifford Algebra, isomorphic to the Quaternions, with graded strucure 1+2+1.

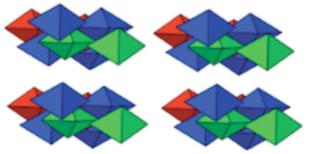
The 4 Binary Pairs of 4 Tetrahedra (2 Dimers) correspond to Cl(2x4) = Cl(8). The Large N Limit of 4N Tetra Clusters = = Completion of Union of All 4N Tetra Clusters would correspond to the same generalized Hyperfinite II1 von Neumann factor of Cl(16)-E8 Physics that gives a natural Algebraic Quantum Field Theory structure. Geometrically E8 = CI(16) half-spinors + CI(16) BiVectors



represents CI(8) Clifford Algebra Vectors and Half-Spinors



represents CI(16) Vectors



represents Cl(16) half-spinors

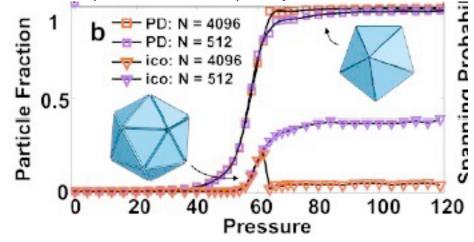
What about the QuasiCrystal / approximant in flat 3-dim space ?

Haji-Akbari1, Engel, Keys, Zheng, Petschek, Palffy-Muhoray, and Glotzer in arXiv 1012.5138 say: "... a fluid of hard tetrahedra undergoes a first-order phase transition to a dodecagonal quasicrystal,

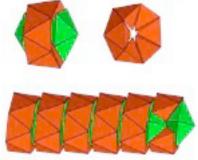
which can be compressed to a packing fraction of $\phi = 0.8324$. By compressing a crystalline approximant of the quasicrystal, the highest packing fraction we obtain is $\phi = 0.8503$.

...

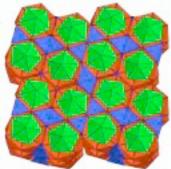
To obtain dense packings of hard regular tetrahedra, we carry out Monte-Carlo (MC) simulations ... of a small system with 512 tetrahedra and a large system with 4096 tetrahedra. ... The large system undergoes a first order transition on compression of the fluid phase and forms a quasicrystal. ...



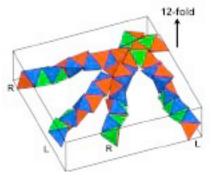
... the quasicrystal consists of a periodic stack of corrugated layers ... Recurring motifs are rings of twelve tetrahedra that are stacked periodically to form "logs"...



... Perfect quasicrystals are aperiodic while extending to infinity; they therefore cannot be realized in experiments or simulations, which are, by necessity, finite. ... Quasicrystal approximants are periodic crystals with local tiling structure identical to that in the quasicrystal. Since they are closely related, and they are often observed in experiments, we consider them as candidates for dense packings. The dodecagonal approximant with the smallest unit cell (space group) has 82 tetrahedra ...



... At each vertex we see the logs of twelve-member rings (shown in red) capped by single PDs (green). The logs pack well into squares and triangles with additional, intermediary tetrahedra (blue). The vertex configuration of the tiling is ...



...".

...

The QuasiCrystal approximant is not as dense as the 4N Tetra Cluster packing, so I do not think it is as useful for fundamental physics as the 4N Tetra packing.

The true QuasiCrystal is less dense than the QuasiCrystal approximant, so I

regard it as being less useful for fundamental physics. However,

as Sadoc and Mosseri say in their book "Geometrical Frustration" (Cambridge 2005) "... quasiperiodic structures [can be] derived from the eight-dimensional lattice E8. using the cut and project method, it is possible to generate a four-dimensional quasicrystal having the symmetry of the [600-cell] polytope {3,3,5} ... a shell-by-shell analysis ... recalls in some respects ... the Fibonacci chain ...

Table A9.1. Number of vertices on shells surrounding the origin in the E8 lattice. The first shell is a Gosset polytope in eight dimensions

Ν	Squared radius r^2	Vertices on E8 shell
1	1/2	240
2	1	2160
3	3/2	6720

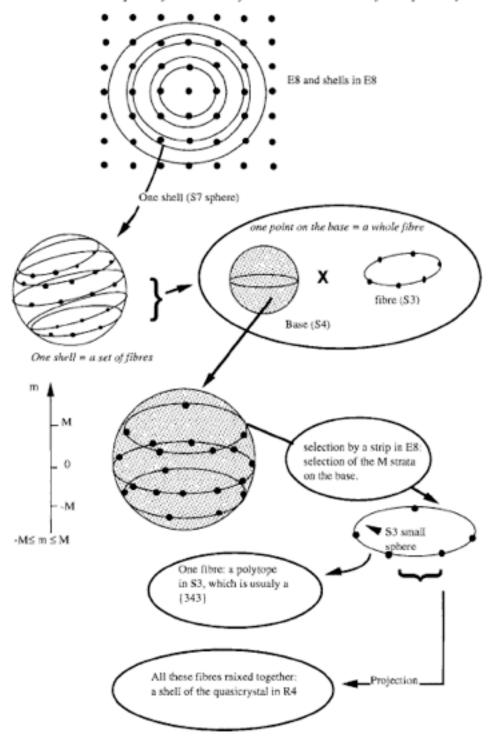


Fig. A9.1. Scheme summarizing the four-dimensional construction method: take an E8 shell, considered as a discrete fibration of S^7 , select the fibres which map (H-map) onto a stratum M of the base of the fibration, and finally orthogonally map (O-map) the selected sites onto R^4 .

The relationship between QuasiCrystals and QuasiCrystal approximants is

discussed by An Pang Tsai in an IOP review "Icosahedral clusters, icosahedral order and stability of quasicrystals - a view of metallurgy":

"... we overview the stability of quasicrystals ... in relation to phason disorder ...

the phonon variable leads to long wavelength and low energy distortion of crystals, the phason variable in quasicrystals leads to a ... type of distortion ...

Let a two-dimensional lattice points sit at the corners of squares in a grid. ... a strip with a slope of an irrational number ... golden mean ... is ... a Fibonacci sequence and is exactly a one-dimensional guasicrystal ...

... [if] the slope of the strip is ... a rational number ... [it]... is a periodic sequence ... [and]... is called an approximant ...

in the approximant where the sequence changes by a flip ... This flip is called phason flip ... a flipping of tiles in two-dimensions or three-dimensions ...

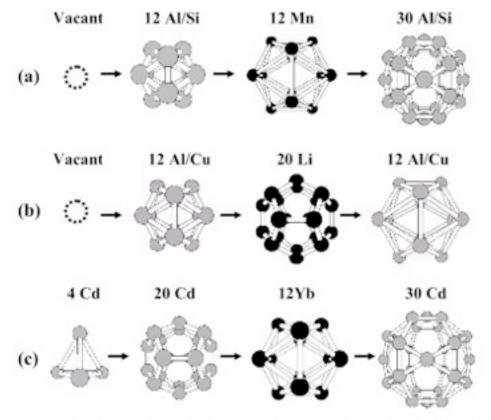


Figure 3. Concentric structures of three types of icosahedral clusters derived from three 1/1 approximants of quasicrystals. (a) The Al-Mn-Si class or Mackay icosahedral cluster: the center is vacant, the 1st shell is an Al/Si icosahedron, the 2nd shell is a Mn icosahedron, and the 3rd shell is an Al/Si icosidodecahedron. (b) The Zn-Mg-Al class or Bergman cluster: an example is R-AlLiCu: the center is vacant, the 1st shell is an Al/Si icosahedron, the 2nd shell is a Li dodecahedron, the 3rd shell is a larger Al/Cu icosahedron. (c) The Cd-Yb class: the center is a Cd tetrahedron, the 1st shell is a Cd dodecahedron, the 2nd shell is a Yb icosahedron, and the 3rd shell is a Cd icosidodecahedron.

... 'phason strain' ... is the characteristic disorder for quasicrystals but does not exist in crystals ...

a fully annealed stable iQc [icosahedral quasicrystal]... is almost free of phason disorder ...".

Appendix - 4-dim M4 Spacetime Feynman Checkerboard

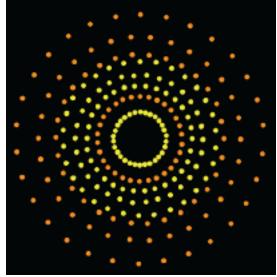
The main body of this paper discusses E8 Root Vectors and their relationship with continuous structures such as symmetric spaces E8 / D8 and D8 / D4xD4 etc useful in describing E8 Physics and doing E8 Physics calculations.

However, from a fundamental point of view, it is useful to describe E8 Physics in terms of discrete structures such as E8 Lattices and Gossett Polytopes in 8-dim and D4 Lattices and 600-cells and 24-cells in 4-dim Kaluza-Klein subspaces which leads to construction of 4-dim M4 Feynman Checkerboards with Planck-scale Lattice Spacings.

The 240 vertices of the E8 Gosset polytope in 8-dim have physical interpretations that produce a Local Classical Lagrangian for Gravity and the Standard Model. Embedding E8 in the Real Clifford Algebra Cl(1,25) and taking the completion of the union of all tensor products of Cl(1,25) gives a realistic Algebraic Quantum Field Theory (AQFT).

An equivalent Quantum Field Theory can be constructed using Tetrahedra, 57G, 600-cells, and the E8 Gossett polytope along with a generalized Feynman Checkerboard in 4 SpaceTime dimensions.

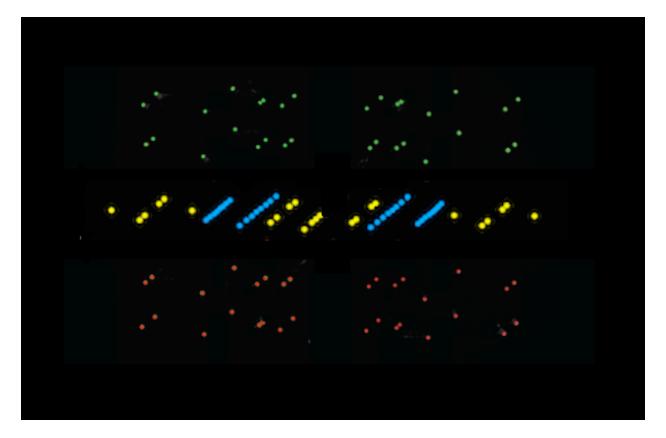
To begin, consider the 240 Root Vectors, based on 8-dim Octonionic spacetime being seen as <u>4+4</u> -dim Quaternionic M4 x CP2 Kaluza-Klein Spacetime:



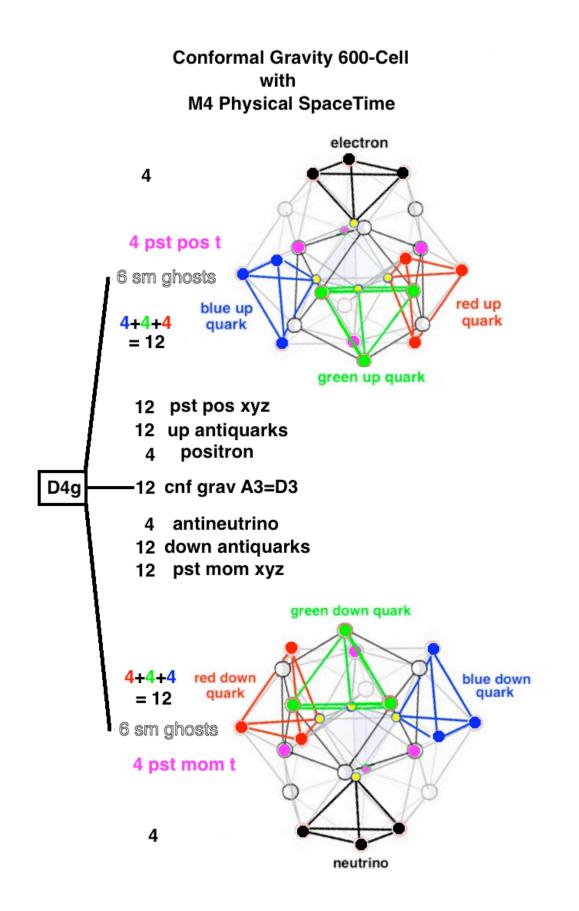
120 of the 240 (yellow dots) represent aspects of First-Generation Fermions, Gauge Bosons and Ghosts, and Position and Momentum related to M4 Physical Spacetime. 120 of the 240 (orange dots) represent aspects of First-Generation Fermions, Gauge Bosons and Ghosts, and Position and Momentum related to CP2 = SU(3) / SU(2)xU(1)Internal Symmetry Space. In the above 2-dim projection the CP2 120 have larger radii from the center than the M4 120 by a factor of the Golden Ratio. Now go to my preferred represention of the 240 E8 Root Vectors in 2-dim / 3-dim space in a square / cube configuration.

Split 8-dim Kaluza-Klein E8 SpaceTime into its two 4-dimensional components: M4 Physical SpaceTime and CP2 = SU(3 / SU(2)xU(1) Internal Symmetry Space

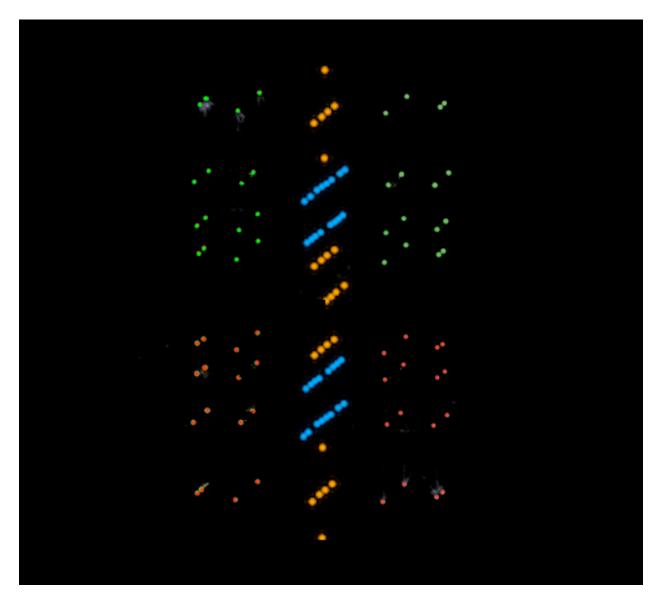
Let one 600-cell represent Gravity and physics of Physical SpaceTime. Here is a projection of its 120 vertices whose physical interpretations are: red and green = M4 Components of Fermions, blue = M4 Physical SpaceTime, yellow = D4g of Conformal Gravity and Standard Model Ghosts



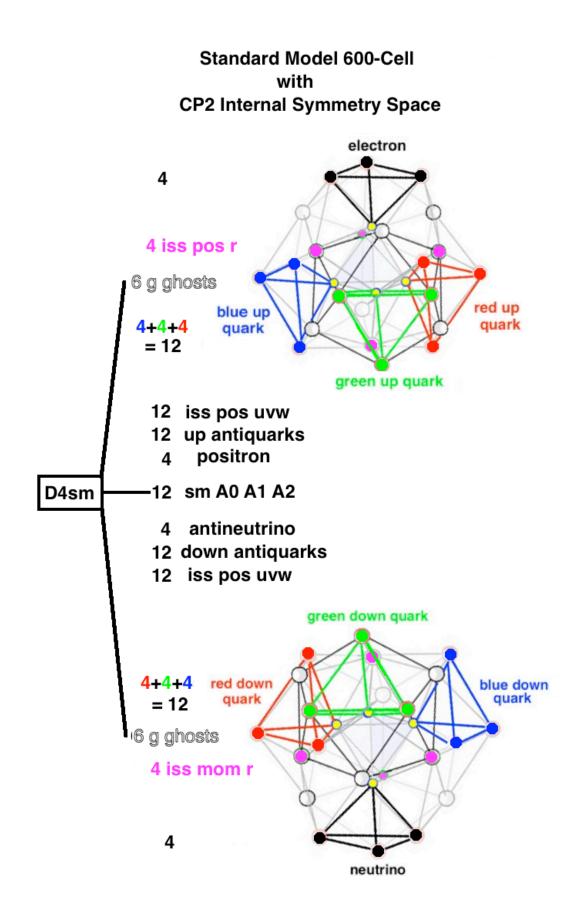
Here is how those 120 vertices appear in cell-centered sections of the D4g 600-cell:



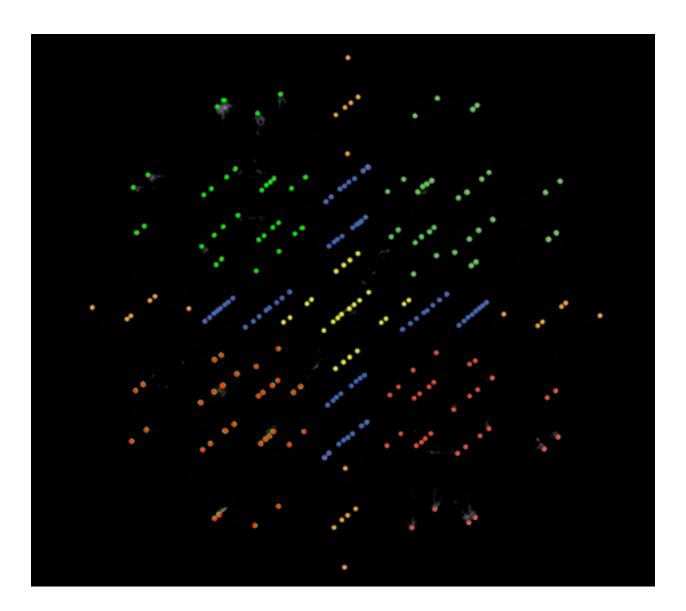
Let the other 600-cell represent the Standard Model and its Internal Symmetry Space. Here is a projection of its 120 vertices whose physical interpretations are: red and green = CP2 Components of Fermions, blue = CP2 Internal Symmetry Space, orange = D4sm of the Standard Model and Conformal Gravity Ghosts



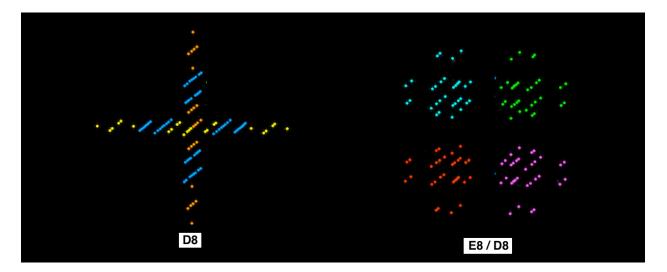
Here is how those 120 vertices appear in cell-centered sections of the D4sm 600-cell:



The 120 vertices of the D4g 600-cell and the 120 vertices of the D4sm 600-cell combined form the 240 vertices of the E8 Root Vectors of E8 Physics:



E8 lives inside the Real Clifford Algebra Cl(16) as E8 = D8 + Cl(16) half-spinors so



240 E8 Root Vectors = 112 D8 Root Vectors + 128 Cl(16) half-spinors

E8 Lattice = D8 Lattice + ([1] + D8 Lattice) where the lattice shifting glue vector [1] = (1/2, ..., 1/2)

Appendix - Feynman Checkerboard Quantum Theory

Conway and Sloane, in their book Sphere Packings, Lattices, and Groups (3rd edition, Springer, 1999), in chapter 4, section 7.3, pages 119-120) define a packing [where the glue vector [1] = (1/2, ..., 1/2)]

D+n = Dn u ([1] + Dn)

and say:

"... D+n is a lattice packing if and only if n is even. D+3 is the tetrahedral or diamond packing ... and D+4 = Z4. When n = 8 this construction is especially important, the lattice **D+8 being known as E8** ...".

Therefore

E8 Lattice = D8 Lattice + ([1] + D8 Lattice)

There are 7 independent E8 Integral Domain Lattices. Physically, the D8 Lattice represents SpaceTime and Gauge Bosons while the ([1] + D8 Lattice) represents Fermions.

At high energies (for example, during Inflation) E8 Physics is Octonionic and there is only one generation of fermions, so the first generation is the only generation. Therefore, each charged Dirac fermion particle, and its antiparticle, correspond to one imaginary Octonion, to one associative triangle, and to one E8 lattice so each Fermion propagates in its own **E8 8D Feynman Checkerboard Lattice**:

red	Down Ç	Quark		r	ed Up	Quark		•
	green	Down Qı	lark	Electro	n gr	een Up	o Quark	
		blue	Down Qu	uark		bl	ue Up Ç	uark
	rD	gD	bD	Е	rU	gŬ	bU	
	-	-	77	Ð			1-	
	I	J	K	Ε	1	J	K	
				j				
				/ /				
				ik				
	J	j	J		I	J	K	
	/ \	/ \	/ \		/ \	/ \	/ \	
	iK	IK	Ik		Ei	Ej	Ek	
	3E8	6E8	4E8	7E8	1E8	2E8	5E8	

Since all the E8 lattices have in common the vertices { ± 1 , $\pm i$, $\pm j$, $\pm k$, $\pm e$, $\pm ie$, $\pm je$, $\pm ke$ }, all the charged Dirac fermions can interact with each other. Composite particles, such as Quark-AntiQuark mesons and 3-Quark hadrons, propagate on the common parts of the E8 lattices involved. The uncharged neutrino fermion, which corresponds to the Octonion real axis with basis {1}, propagates on the 8th Kirmse E8 Lattice that is not an independent Octonion Integral Domain.

If a preferred Quaternionic Structure is introduced into an Octonionic E8 Lattice then the Octonionic E8 Lattice is transformed into Quaternionic Lattice structure. The Quaternionic Integral Domain Lattice is the D4 Lattice.

D8 Lattice is transformed to D4g + D4sm

([1] + D8 Lattice) is transformed to ([1] + D4g) + ([1] + D4sm)

so

E8 is transformed to { D4g + ([1] + D4g) } + { D4 sm + ([1] + D4sm) }

E8 = D+4g + D+4sm

D+4g corresponds to the 600-cell containing D4g

D+4sm corresponds to the 600-cell containing D4sm

Conway and Sloane (Sphere Packings, Lattices, and Groups - Springer) (Chapter 4, eq. 49) give equations for the number of vertices N(m) in the m-th layer of the D+4 HyperDiamond lattice where d is a divisor (including 1 and m) of m: for m odd: N(m) = 8 SUM(dlm) dfor m even: N(m) = 24 SUM(dlm, d odd) d Here are the numbers of vertices in some of the layers of the D4+ lattice. The even-numbered layers correspond to the even D4 sublattice: m=norm of layer N(m)=no. vert. 0 1 1 $8 = 1 \times 8$ $24 = 1 \times 24$ 2 3 $32 = (1 + 3) \times 8$ 4 24 = 1 x 24 5 $48 = (1 + 5) \times 8$ $96 = (1 + 3) \times 24$ 6 7 $64 = (1 + 7) \times 8$ 8 $24 = 1 \times 24$ $104 = (1 + 3 + 9) \times 8$ 9 $144 = (1 + 5) \times 24$ 10 11 $96 = (1 + 11) \times 8$ 12 $96 = (1 + 3) \times 24$ $112 = (1 + 13) \times 8$ 13 14 $192 = (1 + 7) \times 24$ 15 $192 = (1 + 3 + 5 + 15) \times 8$ $24 = 1 \times 24$ 16 $144 = (1 + 17) \times 8$ 17

First Stage of 4D Feynman Checkerboard:

D+4g vertices have HyperOctahedron 8 nearest-neighbors {+/-1,+/-i,+/-j,+/-k} where 4-dim 1,i,j,k are descendants of 8-dim 1,i,j,k to be used as 4D Feynman Checkerboard Primary Links representing the 4-dim M4 Physical SpaceTime of the Kaluza-Klein of E8 Physics whose 4 basis elements are {1,i,j,k} each of which has 8 momentum components with respect to 8-dim SpaceTime to represent 4x8 = 32 of 600-cell vertices.

D+4g vertices have 24-cell 24 next-nearest neighbors representing the 12 Conformal Gravitons (Root Vectors of U(2,2) and 12 Ghosts of Standard Model Gauge Bosons that live on the nearest-neighbor links and represent 24 of 600-cell vertices.

D+4g vertices have 6-semi-HyperCube 32 next-next-nearest neighbors representing 4 M4 Physical SpaceTime components of 8 First-Generation Fermion Particles. Fermion AntiParticles are represented by Particles moving backward in Time for representation of 2x32 = 64 of 600-cell vertices.

D+4g odd (1 and 3) layers correspond to Vectors and Fermion Spinors which are related by Triality. D+4g even (2) layers correspond to BiVectors.

From each vertex of the 4D Feynman Checkerboard the First Stage uses a Triad of Quantum Choice Vectors.

Second Stage of 4D Feynman Checkerboard:

D+4sm vertices have HyperOctahedron 8 nearest-neighbors {+/-1,+/-i,+/-j,+/-k} where 4-dim 1,i,j,k are descendants of 8-dim E,I,J,K to be used as 4D Feynman Checkerboard Secondary Links representing the 4-dim CP2 Internal Symmetry Space of the Kaluza-Klein of E8 Physics whose 4 basis elements are {1,i,j,k} each of which has 8 momentum components with respect to 8-dim SpaceTime to represent 4x8 = 32 of 600-cell vertices.

D+4sm vertices have 24-cell 24 next-nearest neighbors representing the 12 Standard Model Gauge Bosons and

12 Ghosts of Conformal Gravitons (Root Vectors of U(2,2)

that live on the nearest-neighbor links and represent 24 of 600-cell vertices.

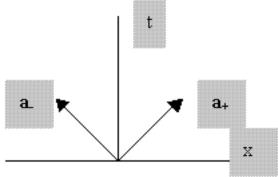
D+4sm vertices have 6-semi-HyperCube 32 next-next-nearest neighbors representing 4 CP2 Internal Symmetry Space components of 8 First-Generation Fermion Particles. Fermion AntiParticles are represented by Particles moving backward in Time for representation of 2x32 = 64 of 600-cell vertices.

D+4g odd (1 and 3) layers correspond to Vectors and Fermion Spinors which are related by Triality. D+4g even (2) layers correspond to BiVectors.

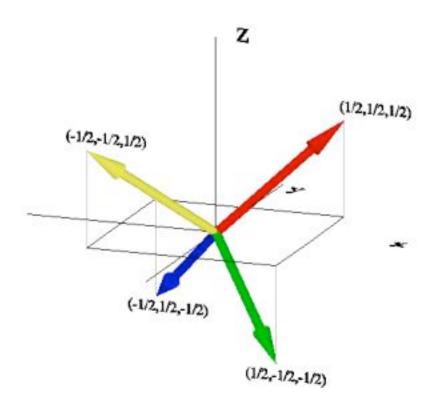
From each vertex of the 4D Feynman Checkerboard the Second Stage uses a second Triad of Quantum Choice Vectors.

A significant consequence of using two Triads of Quantum Choice Vectors is the emergence of Second and Third Generation Fermions.

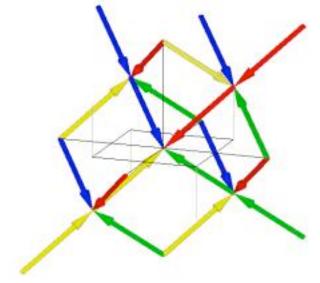
In my earlier paper (arXiv quant-ph/9503015) I used a simpler version of 4D **Feynman Checkerboard which is useful for showing consistency with the Dirac equation** using the following approach: The Feynman Checkerboard in 1+3 SpaceTime dimensions reproduces the Dirac equation, using work of Urs Schreiber and George Raetz. (See my paper at CERN-CDS-EXT-2004-030) A very nice feature of the George Raetz web site is its illustrations, which include an image of a vertex of a 1+1 dimensional Feynman Checkerboard



and an image of a projection into three dimensions of a vertex of a 1+3 dimensional Feynman Checkerboard



and an image of flow contributions to a vertex in a HyperDiamond Random Walk from the four nearest neighbors in its past



Urs Schreiber wrote on the subject:

Re: Physically understanding the Dirac equation and 4D

in the newsgroup sci.physics.research on 2002-04-03 19:44:31 PST (including an appended forwarded copy of an earlier post) and again on 2002-04-10 19:03:09 PST as found on the web page http://www-stud.uni-essen.de/~sb0264/spinors-Dirac-checkerboard.html

and the following are excerpts from those posts:

"... I know ... the ... lanl paper ...[<u>http://xxx.lanl.gov/abs/quant-ph/9503015</u>]... and I know that Tony Smith does give

a generalization of Feynman's summing prescription from 1+1 to 1+3 dimensions.

But I have to say that I fail to see that this generalization reproduces the Dirac propagator in 1+3 dimensions, and that I did not find any proof that it does.

Actually, I seem to have convinced myself that it does not, but I may of course be quite wrong.

I therefore take this opportunity to state my understanding of these matters.

First, I very briefly summarize (my understanding of) Tony Smith's construction: The starting point is the observation that the left I-> and right I+> going states of the 1+1 dim checkerboard model can be labeled by complex numbers

l-> ---> (1 + i) l+> ---> (1 - i)

(up to a factor) so that multiplication by the negative imaginary unit swaps components:

 $\begin{array}{l} (-i) \ (1 \ + \ i)/2 = (1 \ - \ i)/2 \\ (-i) \ (1 \ - \ i)/2 = (1 \ + \ i)/2 \end{array}.$

Since the path-sum of the 1+1 dim model reads

phi = sum over all possible paths of (-i eps m)^(number of bends of path) =

= sum over all possible paths of product over all steps of one path of -i eps m (if change of direction after this step generated by i) 1 (otherwise)

this makes it look very natural to identify the imaginary unit appearing in the sum over paths with the "generator" of kinks in the path.

To generalize this to higher dimensions, more square roots of -1 are added,

which gives the quaternion algebra in 1+3 dimensions.

The two states I+> and I-> from above, which were identified with complex numbers, are now generalized to four states identified with the following quaternions

(which can be identified with vectors in M⁴ indicating the direction in which a given path is heading at one instant of time):

(1 + i + j + k) (1 + i - j - k) (1 - i + j - k) (1 - i - j + k)

which again constitute a (minimal) left ideal of the algebra

(meaning that applying i,j, or k from the left on any linear combination of these four states gives another linear combination of these four states).

Hence,

now i,j,k are considered as "generators" of kinks in three spatial dimensions and the above summing prescription naturally generalizes to

phi = sum over all possible paths of product over all steps of one path of

-i eps m (if change of direction after this step generated by i)

-j eps m (if change of direction after this step generated by j)

-k eps m (if change of direction after this step generated by k)

1 (otherwise)

The physical amplitude is taken to be

A * e^(i alpha)

where A is the norm of phi and alpha the angle it makes with the x0 axis.

As I said, this is merely my paraphrase of Tony Smith's proposal as I understand it.

I fully appreciate that the above construction is a nice (very "natural") generalization of the summing prescription of the 1+1 dim checkerboard model.

But if it is to describe real fermions propagating in physical spacetime, this generalized path-sum has to reproduce the propagator obtained from the Dirac equation in 1+3 dimensions, which we know to correctly describe these fermions. Does it do that?

....

Hence I have taken a look at the material [that] ... George Raetz ... present[s] ... titled "The HyperDiamond Random Walk", found at

http://www.pcisys.net/~bestwork.1/QRW/the_flow_quaternions.htm , which is mostly new to me. ...

I am posting this in order to make a suggestion for a more radical modification

[The]... equation ... DQ = (iE)Q ... is not covariant.

That is because of that quaternion E sitting on the left of the spinor Q in the rhs of [the] equation

The Dirac operator D is covariant,

but the unit quaternion E on the rhs refers to a specific frame.

Under a Lorentz transformation L one finds

 $L DQ = iE LQ = L E' Q \iff DQ = E'Q$ now with $E' = L \iff E L$ instead of E.

This problem disappears

when the unit quaternion E is brought to the *right* of the spinor Q.

What we would want is an equation of the form DQ = Q(iE).

In fact, demanding that the spinor Q be an element of the minimal left ideal generated by the primitive projector P = (1+y0)(1+E)/4,

so that $Q = \dot{Q}' P$,

one sees that DQ = Q(iE) almost looks like the the *Dirac-Lanczos equation*.

(See hep-ph/0112317, equation (5) or ... equation (9.36) [of]... W. Baylis, Clifford (Geometric) Algebras, Birkhaeuser (1996) ...).

To be equivalent to the Dirac-Lanczos equation, and hence to be correct,

we need to require that D = y0 @0 + y1 @1 + y2 @2 + y3 @3

instead of ... = @0 + e1 @1 + e2 @2 + e3 @3.

All this amounts to sorting out

in which particular representation we are actually working here.

In an attempt to address these issues, I now redo the steps presented on http://www.pcisys.net/~bestwork.1/QRW/the-flow-quaternions.htm

with some suitable modifications to arrive at the correct Dirac-Lanczos equation (this is supposed to be a suggestion subjected to discussion):

So consider a lattice in Minkoswki space generated by a unit cell spanned by the four (Clifford) vectors r = (y0 + y1 + y2 + y3)/2 g = (y0 + y1 - y2 - y3)/2 b == (y0 - y1 + y2 - y3)/2 y = (y0 - y1 - y2 + y3)/2 .

(yi are the generators of the Dirac algebra {yi,yj} = diag(+1,-1,-1,-1)_ij.)

This is Tony Smith's "hyper diamond".

(Note that I use Clifford vectors instead of quaternions.) Now consider a "Clifford algebra-weighted" random walk along the edges of this lattice, which is described by four Clifford valued "amplitudes": Kr, Kg, Kb, Ky and such that @r Kr = k (Kg y2 y3 + Kb y3 y1 + Ky y1 y2) @b Kb = k (Ky y2 y3 + Kr y3 y1 + Kg y1 y2) @g Kg = k (Kr y2 y3 + Ky y3 y1 + Kb y1 y2) @y Ky = k (Kb y2 y3 + Kg y3 y1 + Kr y1 y2). (This is geometrically motivated. The generators on the rhs are those that rotate the unit vectors corresponding to the amplitudes into each other. "k" is some constant.)

Note that I multiply the amplitudes from the *right* by the generators of rotation, instead of multiplying them from the left.

Next, assume that this coupled system of differential equations is solved by a spinor Q Q = Q' (1+y0)(1+iE)/4E = (y2 y3 + y3 y1 + y1 y2)/sqrt(3) with Kr = r Q Kg = g Q Kb = b Q Ky = y Q.

This ansatz for solving the above system by means of a single spinor Q is, as I understand it, the central idea.

But note that I have here modified it on the technical side:

Q is explicitly an algebraic Clifford spinor in a definite minial left ideal,

E squares to -1, not to +1,

and the Ki are obtained from Q by premultiplying with the Clifford basis vectors defined above.

Substituting this ansatz into the above coupled system of differential equations one can form one covariant expression by summing up all four equations:

(r @r + g @g + b @b + y @y) Q = k sqrt(3) Q E The left hand side is immediate. To see that the right hand side comes out as indicated simply note that r + g + b + y = y0 and that Q y0 = Q by construction.

The above equation is the Dirac-Lanczos-Hestenes-Guersey equation, the algebraic version of the equation describing the free relativistic electron.

The left hand side is the flat Dirac operator r @r + g @g + b @b + y @y = ym @m and the right hand side, with k = mc / (hbar sqrt(3)), is equal to the mass term i mc / hbar Q.As usual, there are a multitude of ways to rewrite this. If one wants to emphasize biquaternions then premultiplying everything with y0 and splitting off the projector P on the right of Q to express everything in terms of the, then also biquaternionic, Q' (compare the definitions given above) gives Lanczos' version (also used by Baylis and others).

I think this presentation improves a little on that given on George Raetz's web site:

The factor E on the right hand side of the equation is no longer a nuisance but a necessity.

Everything is manifestly covariant (if one recalls that algebraic spinors are manifestly covariant when nothing non-covariand stands on their *left* side). The role of the quaternionic structure is clarified,

the construction itself does not depend on it.

Also, it is obvious how to generalize to arbitrary dimensions.

In fact, one may easily check that for 1+1 dimensions the above scheme reproduces the Feynman model.

While I enjoy this, there is still some scepticism in order as long as a central questions remains to be clarified:

How much of the Ansatz K(r,g,b,y) = (r,g,b,y) Q is whishful thinking?

For sure,

every Q that solves the system of coupled differential equations that describe the amplitude of the random walk on the hyper diamond lattice also solves the Dirac equation.

But what about the other way round? Does every Q that solves the Dirac equation also describe such a random walk. ...".

My proposal to answer the question raised by Urs Schreiber

Does every solution of the Dirac equation also describe a HyperDiamond Feynman Checkerboard random walk?

uses symmetry.

The hyperdiamond random walk transformations include the transformations of the Conformal Group:

rotations and boosts (to the accuracy of lattice spacing); translations (to the accuracy of lattice spacing); scale dilatations (to the accuracy of lattice spacing): and special conformal transformations (to the accuracy of lattice spacing).

Therefore, to the accuracy of lattice spacing, the hyperdiamond random walks give you all the conformal group Dirac solutions, and since the full symmetry group of the Dirac equation is the conformal group, the answer to the question is "Yes".

Thanks to the work of Urs Schreiber:

The HyperDiamond Feynman Checkerboard in 1+3 dimensions does reproduce the correct Dirac equation.

Here are some references to the **conformal symmetry of the Dirac equation**:

R. S. Krausshar and John Ryan in their paper Some Conformally Flat Spin Manifolds, Dirac Operators and Automorphic Forms at math.AP/022086 say:

"... In this paper we study Clifford and harmonic analysis on some conformal flat spin manifolds. ... manifolds treated here include RPn and S1 x S(n-1).

Special kinds of Clifford-analytic automorphic forms associated to the different choices of are used to construct Cauchy kernels, Cauchy Integral formulas, Green's kernels and formulas together with Hardy spaces and Plemelj projection operators for Lp spaces of hypersurfaces lying in these manifolds. ...

Solutions to the Dirac equation are called Clifford holomorphic functions or monogenic functions.

Such functions are covariant under ... conformal or Mobius transformations acting over Rn u {oo}. ...".

Barut and Raczka, in their book Theory of Group Representations and Applications (World 1986), say, in section 21.3.E, at pages 616-617:

"... E. The Dynamical Group Interpretation of Wave Equations.

... Example 1. Let G = O(4,2).

Take U to be the 4-dimensional non-unitary representation in which the generators of G are given in terms of the 16 elements of the algebra of Dirac matrices as in exercise 13.6.4.1.

Because $(1/2)L_56 = gamma_0$ has eigenvalues n = +/-1,

taking the simplest mass relation mn = K, we can write

(m gamma_0 - K) PSI(dotp) = 0, where K is a fixed constant.

Transforming this equation with the Lorentz transformation of parameter E $PSI(p) = exp(i \in N) PSI(p)$

N = (1/2) gamma_0 gamma

gives

 $(gamma^u p_u - K) PSI(p) = 0$

which is the Dirac equation ...".

P. A. M. Dirac, in his paper Wave Equations in Conformal Space, Ann. Math. 37 (1936) 429-442, reprinted in The Collected Works of P. A. M. Dirac: Volume 1: 1924-1948, by P. A. M. Dirac (author), Richard Henry Dalitz (editor), Cambridge University Press (1995), at pages 823-836, said:

"... by passing to a four-dimensional conformal space ...

a ... greater symmetry of ... equations of physics ... is shown up, and their invariance under a wider group is demonstrated. ...

The spin wave equation ... seems to be the only

simple conformally invariant wave equation involving the spin matrices. ... This equation is equivalent to the usual wave equation for the electron, except ...[that it is multiplied by]... the factor (1 + alpha_5),

which introduces a degeneracy. ...".

Here are some comments on Lorentz Invariance based on D4 Lattice properties:

The D4 lattice nearest neighbor vertex figure, the 24-cell,

is the 4HD HyperDiamond lattice next-to-nearest neighbor vertex figure.

Fermions move from vertex to vertex along links.

Gauge bosons are on links between two vertices, and so can also be considered as moving from vertex to vertex along links.

The only way a translation or rotation can be physically defined is by a series of movements of a particle along links.

A TRANSLATION is defined as a series of movements of a particle along links, each of which is

the CONTINUATION of the immediately preceding link IN THE SAME DIRECTION. An APPROXIMATE rotation, within an APPROXIMATION LEVEL D,

is defined with respect to a given origin as a series of movements of a particle along links among vertices ALL of which

are in the SET OF LAYERS LYING WITHIN D of norm (distance²) R from the origin, that is,

the SET OF LAYERS LYING BETWEEN norm R-D and norm R+D from the origin. Conway and Sloane (Sphere Packings, Lattices, and Groups - Springer) pp. 118-119 and 108, is the reference that I have most used for studying lattices in detail.

(Conway and Sloane define the norm of a vector x to be its squared length xx.) In the D4 lattice of integral quaternions,

layer 2 has the same number of vertices as layer 1, N(1) = N(2) = 24.

Also (this only holds for real, complex, quaternionic, or octonionic lattices), K(m) = N(m)/24 is multiplicative,

meaning that, if p and q are relatively prime, K(pq) = K(p)K(q).

The multiplicative property implies that:

 $K(2^{a}) = K(2) = 1$ (for a greater than 0) and

 $K(p^a) = 1 + p + p^2 + \dots + p^a$ (for a greater than or equal to 0).

So,

for the D4 lattice,

there is always an arbitrarily large layer (norm $xx = 2^a$, for some large a) with exactly 24 vertices, and

there is always an arbitrarily large layer(norm xx = P, for some large prime P) with 24(P+1) vertices (note that Mersenne primes are adjacent to powers of 2), and

given a prime number P whose layer is within D of the origin,

which layer has N vertices,

there is a layer kP with at least N vertices within D of any other given layer in D4. Some examples I have used are chosen so that

the 2^a layer adjoins the prime 2^a +/- 1 layer.

Notation in the following table is based on the minimal norm of the D4 Lattice being 1. This is the second definition (equation 90) of the D4 Lattice in

Chapter 4 of Sphere Packings, Lattices, and Groups, 3rd ed., by Conway and Sloane (Springer 1999) who note that the Dn lattice is the checkerboard lattice in n dimensions.

m=norm of layer	N(m)=no. vert.	K(m) = N(m) / 24
1	24	1
2	24	1
3	96	4
4	24	1
5	144	6
б	96	4
7	192	8
8	24	1
9	312	13
10	144	6
11	<u>288</u>	12
12	96	4
13	336	14
14	192	8
15	576	24
16	24	1
17	432	18
18	312	13
19	480	20
20	144	6
127	3,072	128
128	24	1
65,536=2^16	24	1
65,537	1,572,912	65,538
2,147,483,647	51,539,607,552	2,147,483,648
2,147,483,648=2^31	24	1

Appendix - Renormalization, NCG, and Tquark mass states

Truth Quark Mass from Renormalization to Planck Mass

Alvarez-Gaume, Polchinski, and Wise in Nuclear Physics B221 (1983) 495-523 said: "... there are Higgs boson self-energy graphs involving gravitons such as fig 1.



Fig. 1. Large gravitational loop contribution to the Higgs boson mass.

This graph ceases to make sense at some scale \land where our understanding of gravity breaks down, but its contribution from momenta below \land can be estimated as $\land \land 4 / M$ Planck $\land 2$.

Unless \land is far below the Planck scale (i.e. $\land < 10^{(-9)}$ M_Planck), this is much larger than the actual Higgs mass. The contribution of fig. 1 must ... be canceled very precisely against a bare mass

The idea of driving SU(2) x U(1) symmetry breaking via a heavy quark Yukawa has been used in ... preprints by Ibanez and Ellis et al. discussing the need to include radiative corrections ... and observing that a large top quark Yukawa would drive SU(2)x U(1) breaking. Ibanez has also derived the same renormalization group equations which we give ...

The full renormalization group equations for the parameters in the lagrangian (25) are given in the appendix. They have been calculated using both component and superfield formalisms. We repeat here the equations of interest. In the running we neglect the contribution of gaugino masses, the Fayet-Iliopoulos *D*-term ξ , the Higgs self-coupling μ and all Yukawa couplings except g_U^{33} . For the masses, $m_{H'}^2$, $m_{U_s^2}^2$ and $m_{O_3}^2$ we have

$$\mu \frac{\partial}{\partial \mu} \begin{bmatrix} m_{H'}^2 \\ m_{U_s^0}^2 \\ m_{Q_3}^2 \end{bmatrix} = \frac{\left(g_U^{33}\right)^2}{8\pi^2} \begin{bmatrix} 3 & 3 & 3 \\ 2 & 2 & 2 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} m_{H'}^2 \\ m_{U_s^0}^2 \\ m_{Q_3}^2 \end{bmatrix} + \frac{|A_U^{33}|^2 \left(g_U^{33}\right)^2}{8\pi^2} \begin{bmatrix} 3 \\ 2 \\ 1 \end{bmatrix} m_g^2, \quad (45a)$$

and for the other masses

$$\mu \frac{\partial}{\partial \mu} m_i^2 = 0.$$
 (45b)

Note that the gauge interactions make no contribution to (45), so all masses-squared would remain positive and equal to m_g^2 [cf. eq. (27)] in the absence of large Yukawa couplings^{*}. The sign in (45) corresponds to decreasing masses-squared at low energy and the 3:2:1 weighting implies that $m_{H'}^2$ is driven negative for a sufficiently large Yukawa coupling. This is the source of SU(2) × U(1) breakdown.

Weak interaction breakdown occurs for top-quark masses between 100 and 195 GeV.

The renormalization group equation for g_U^{33}

$$\mu \frac{\partial}{\partial \mu} g_U^{33} = \frac{3}{8\pi^2} \left(g_U^{33} \right)^3 - \frac{1}{8\pi^2} g_U^{33} \left\{ \frac{8}{3} e_3^2 + \frac{3}{2} e_2^2 + \frac{13}{18} e_1^2 \right\},\tag{46}$$

...".

tends to attract the top quark mass towards a fixed point of about 125 GeV.

125 GeV is in the range of the 130 GeV Light Truth Quark of E8 Physics.

Rabindra Mohapatra in Unification and Supersymmetry Third Edition (Springer 2003, 1992, 1986) said:

"... Alvarez-Gaume, Polchinski, and Wise ... note that the effective potential ... has been defined at the Planck scale ... To study their behavior at lower energies the parameters must be extrapolated down to the TeV scale. Since the nature of the extrapolation is determined by radiative corrections, the various parameters ... will change from their values at the Planck scale ... If the process of extrapolation makes the (mass)^2 of the Higgs ... negative, then ... it will give rise to electroweak symmetry breaking ... It is ... possible to write the renormalization group equations for the various parameters in order to study their extrapolation from the Planck mass down to the TeV scale ... for only SU(2)L x U(1) to occur ... mt lies in the range 100 GeV \leq mt \leq 190 GeV

a ... scheme for dynamical electroweak symmetry breaking has been proposed, based on the idea ...[of]... top-quark condensates ...

The question of the dynamical breaking of this symmetry by the formation of < t_L , t_R > condensate can be studied in a manner identical to that used by Nambu and Jona-Lasino in their classic paper on the application of the BCS model to particle physics. Working in the bubble approximation, one can convince oneself that, for M^2 < N_c / 2 / 8 pi^2

... t tbar condensate forms and electroweak symmetry is broken.

To get quantitative prediction from this we follow the procedure of Bardeen, Hill, and Lindner ... We see that the low-energy theory looks exactly like the standard model ... studies of the renormalization group evolution of coupling constants in the standard model ... have established that, regardless of what the numerical values of λ and h at $\mu = \Lambda$ are, they go to an almost fixed point at low energies ...

for the idea of the t tbar condensates to be useful, the t-quark must be heavy. In fact ... we must have $mt > 95 \text{ GeV} \dots$

one can predict mt and mH, as a function of Λ . As Λ increases, mt goes down; but if we keep $\Lambda \leq MP1$, we get mt ≥ 250 GeV in the minimal model ...".

250 GeV is in the range of the 250 GeV Heavy Truth Quark of E8 Physics.

• • •

NCG and 130 GeV Tquark Light Mass State

Connes has constructed a realistic physics model in 4-dim spacetime based on **NonCommutative Geometry (NCG) of M x F** where M = 4-dim spacetime and $F = C \times H \times M3(C)$ and C = Complex Numbers, H = Quaternions, and M3(C) = 3x3 Complex Matrices.

E8 has been used as a basis for physics models such as those by Lisi (arXiv 1506.08073) and Smith (viXra 1508.0157) so the purpose of this paper is to show a connection between Connes NCG Physics and E8.

Connes NCG is described by van den Dungen and van Suijlekom in arXiv 1204.0328 where they say: "... this review article is to present

the applications of Connes' noncommutative geometry to elementary particle physics.

the noncommutative description of the Standard Model does not require the introduction of extra spacetime dimensions,

its construction is very much like the original Kaluza-Klein theories.

In fact, **one starts with a product M x F of ordinary four-dimensional spacetime M with an internal space F** which is to describe the gauge content of the theory. Of course, spacetime itself still describesmthe gravitational part.

The main difference with Kaluza-Klein theories is that the additional space is a discrete ... space whose structure is described by a ... noncommutative algebra ... This is very much like the description of spacetime M

by its coordinate functions as usual in General Relativity,

which form an algebra under pointwise multiplication:

 $(x^{mu} x^{nu})(p) = x^{mu}(p) x^{nu}(p)$

Such commutative relations are secretly used in any physics textbook.

However, for a discrete space, ... propose to describe F by matrices ...

yielding a much richer internal (algebraic) structure ...

one can also describe a metric on F in terms of algebraic data,

so that we can fully describe the geometrical structure of M x F .

This type of noncommutative manifolds are called almost-commutative (AC)

...

Given an AC manifold M x F ... the group of diffeomorphisms ... generalized to such noncommutative spaces combines ordinary diffeomorphisms of M with gauge symmetries ... we obtain a combination of general coordinate transformations on M with the respective groups ... U(1) x SU(2) x SU(3) ... [whose]... finite space is ...

internal space F ...[=]... C x H x M3(C)

... to construct a Lagrangian from the geometry of M x F . This is accomplished by ... a simple counting of the eigenvalues of a Dirac operator on M x F

which are lower than a cutoff $\land \dots$ we derive local formulas (integrals of Lagrangians) \dots using heat kernel methods \dots

The fermionic action is given as usual by an inner product.

The Lagrangians that one obtains in this way ... are the right ones, and in addition minimally coupled to gravity.

This is unification with gravity of ... the full Standard Model. ... We study conformal invariance ... with particular emphasis on the Higgs mechanism

coupled to the gravitational background

the Lagrangian derived ... from the relevant noncommutative space is not just the Standard Model Lagrangian, but it implies that there are relations between some of the Standard Model couplings and masses

If we would assume that the mass of the top quark is much larger than all other fermion masses, we may neglect the other fermion masses. In that case ...

m_top ≤ sqrt(8/3) Mw [= sqrt(8/3) 80 = 130 GeV]

we shall evaluate the renormalization group equations (RGEs) for the Standard Model from ordinary energies up to the ... GUT ... unification scale ...

The scale ∧12 ... is given by ... 1.03 x 10^13 GeV ...

The [scale] /23 is given by ... 9.92 x 10^16 GeV ...

we have ... included the simple case wherewe ignore the Yukawa coupling of the tauneutrino

[as is realistic with no neutrino see-saw mechanism] ... Numerical results [are]...

∧gut (10^16 GeV) ... m_top (GeV) 186.0 ... m_h (GeV) 188.1 ...

∧gut (10^13 GeV) ... m_top (GeV) 183.2 ... m_h (GeV) 188.3 ...".

If you do a naive extrapolation down to the Higgs VeV 250 GeV energy scale where the compositeness of a Higgs as Tquark condensate system might become evident (the Non-perturbativity Boundary)

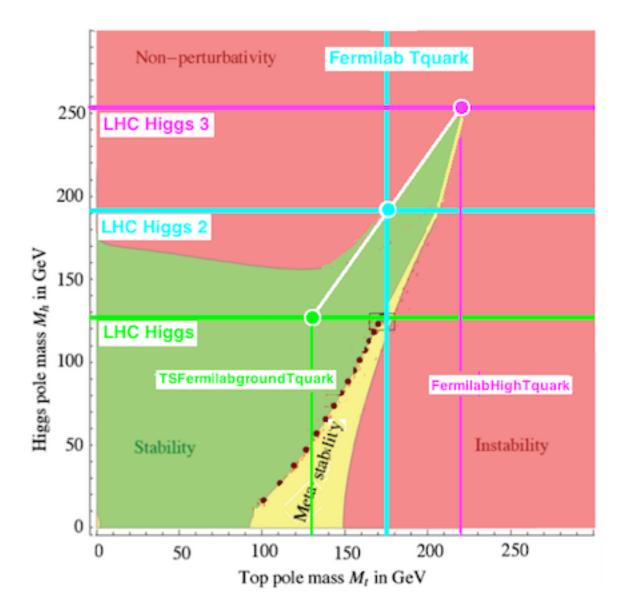
∧comp (250 GeV) ... m_top (GeV) 173.2 ... m_h (GeV) 189

so the naively extrapolated

NCG masses for the Tquark-Higgs Middle Mass States are consistent with those of the E8 model of Smith (viXra 1508.0157)

Further,

the Basic Ground State NCG Tquark mass of 130 GeV is consistent with that of the E8 model of Smith (viXra 1508.0157) Here is a chart showing the 3 Mass States of the Smith E8 model (viXra 1508.0157): the green dot in the Stable region (green) has the 130 GeV Tquark mass state that is also calculated by NCG; the cyan dot on the Non-perturbativity Boundary has the 173 GeV Tquark and 189 GeV Higgs mass states that are also calculated by NCG; I have not seen where NCG may or may not calculate High-Mass (220 and 250 GeV) Tquark and Higgs mass states indicated by the magenta dot at the Critical Point.



Structure of M and F of NCG

The **M of NCG** is 4-dim Spacetime, a discrete version of which is the Integral Domain of Integral Quaternions whose vertex figure (nearest neighbors to the origin) is the 24-cell Root Vector Polytope of the 28-dim D4 Lie Algebra which contains as a subalgebra the 15-dim D3 Lie Algebra of the Conformal Group Spin(2,4) = SU(2,2) for MacDowell-Mansouri Gravity plus Conformal Dark Energy.

4-dim Riemannian Spacetime can be Wick Rotated to 4-dim Euclidean Space which can be compactified to the 4-sphere S4 which can be discretized as the 600-cell



so the M of NCG can be locally represented as a 600-cell which has 120 vertices.

F of NCG is the 24-dim algebra C + H + M3(C).

Identify the 24 generators of F with the 24 elements of the Binary Tetrahedral Group and therefore **identify F with the Tetrahedron** of which it is the symmetry group. NCG, by using M x F as its basic structure, puts a copy of F at each point of M.

Consider a flat 2-dim subspace of M, and add to it F Tetrahedra following this construction recipe from a Don Davis 8 Sep 1999 sci math post:

"... build ... a hollow torus of 300 cells ... as follows:

lay out a 5x10 grid of unit edges. omit the lefthand and lower boundaries' edges, because we're going to roll this grid into a torus later.

thus, the grid contains 100 edges: 50 running N-S, and 50 running EW.

attach one tetrahedron to each edge from above the grid.

the opposite edges of these tetrahedra will form a new 5x10 grid,

whose vertices overlie the centers of the squares in the lower grid.

thus, these 100 tetrahedra now form an egg-carton shape,

with 50 squarepyramid cups on each side.

divide each cup into two non-unit tetrahedra,

by erecting a right-triangular wall across the cup, corner-to-corner.

make the upper cups' dividers run NE/SW,

and make the upside-down lower cups' dividers run NW/SE.

note that the egg-carton is now a solid flat layer, one tetrahedron deep,

containing 100 unit tetra- hedra and 200 non-unit tetrahedra.

when we shrink the right-triangular dividing walls into equilateral triangles, we distort each egg-cup into a pair of unit-tetrahedra.

at the same time,

the opening of each egg-cup changes from a square to a bent rhombus. as the square openings bend,

the flat sheet of 300 tethrahedra is forced to wrap around into a hollow torus with a one-unit- thick shell.

surprisingly,

this bends each 5x10 grid into a toroidal sheet of 100 equilateral triangles. each grid's short edge is now a pentagon that threads through the donut hole. the grid's long edge is now a decagon that wraps around both holes in its donut. the two grids' long edges are now linked decagons.

this wrapping cannot occur in R3, but it works fine in R4.

I admit that this part of my presentation is not easy to visualize.

perhaps a localized visualization image will help:

as an upper egg-cup is squeezed in one direction,

the edge-tetrahedra around it rotate,

squeezing the nearby lower egg-cups in the other direction.

this forces the flat sheet into a saddle-shape.

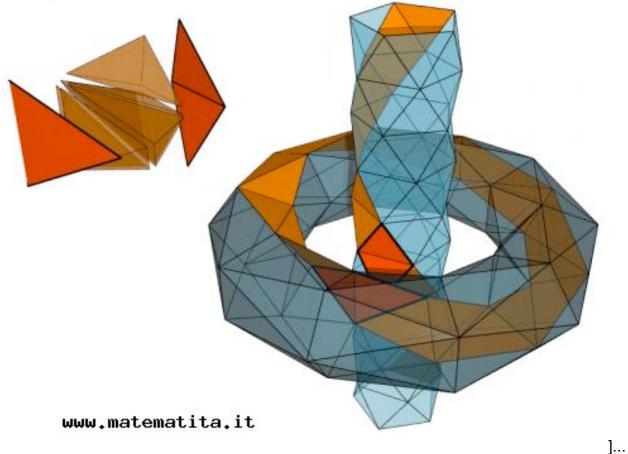
in R4, when this saddle-bending happens across the whole egg-carton at once, the carton's edges can meet to make the toroidal sheet.

•••

build each solid torus[of]... two solid tori of 150 cells each ... as follows: using 100 tetrahedra, assemble 5 solid icosahedra (this is possible in R4). daisy-chain five such icosahedra pole-to-pole ... between every pair of adjacent icosahedra, surround the common vertex with 10 tetrahedra. each solid torus has a decagonal "axis" running through the centers and poles of the icosahedra. each solid torus contains 5*20 + 5*10 = 150tetrahedra, and its surface is tiled with 100 equilateral triangles. on this surface, six triangles meet at every vertex.

•••

we will link these solid tori, like two links of a chain. with the hollow torus acting as a glue layer between them ...[



finally,

put one solid torus inside the hollow toroidal sheet,

attaching the 100 triangular faces of the solid

to the 100 triangles of the sheet's inner surface.

this gives us a fat solid torus,

10 units around and 4 units thick, containing 450 tetrahedral cells.

nevertheless, its surface has only 100 triangular faces.

thread the second 150-cell solid torus through this fat torus,

and attach the two solids' triangular faces. this is the 600-cell polytope ...".



Combine the M 600-cell (yellow) with the F 600-cell expanded by the Golden Ratio (orange)



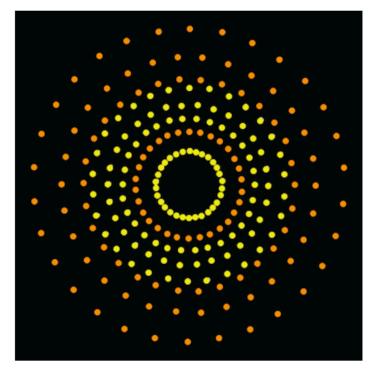


to get the 120+120 = 240-vertex 8-dim E8 polytope which is the Root Vector Polytope of the Lie Algebra E8

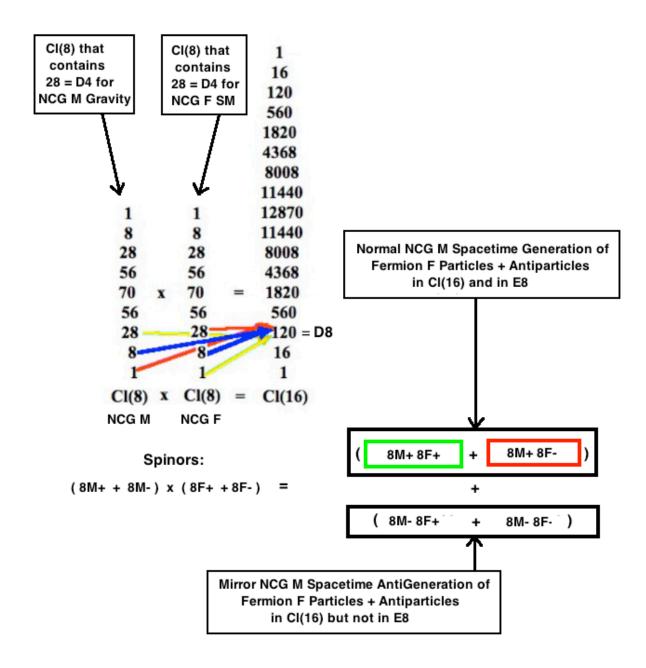
In this way the 8-dim space of E8 Root Vectors is seen as being made up of two independent 4-dim spaces: a Rational Number 4-dim space of yellow M dots

and

an Algebraic Extension by the Golden Ratio 4-dim space of orange F dots



The Lie Algebra E8 lives in the Clifford Algebra $Cl(16) = Cl(8) \times Cl(8)$

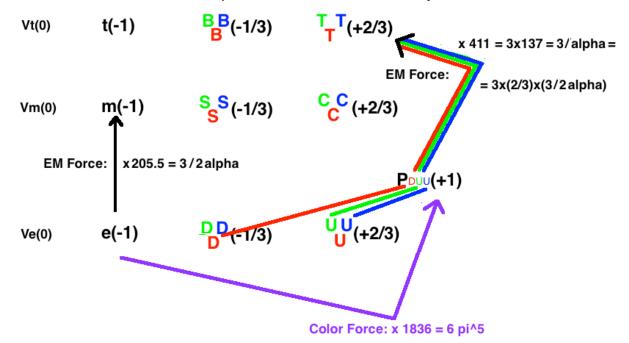


This is the basic structure of the Cl(1,25) E8 Physics Model

(see viXra 1508.0157)

Appendix - Mendel Sachs and Particle Masses

Mendel Sachs, in his books "General Relativity and Matter" (1982) and "Quantum Mechanics from General Relativity" (1986) calculated electron / muon and Proton / Tquark mass ratios substantially consistent with



Cl(1,25) E8 Physics masses e = 0.511 MeV, m = 106 MeV, P = 938 MeV, T = 128.5 GeV saying (my comments set off by brackets [[]]):

"... the inertial mass of an elementary (spinor) particle [i]s

determined by the curvature of space-time in its vicinity, representing

the coupling of this particle to its environment of particle-antiparticle pairs ...

[[In Cl(1,25) E8 Physics the particle-antiparticle pairs form a Schwinger Source Kerr-Newman Black Hole]]

Because the coupling of the observed electron to the pairs ... is electromagnetic, the electron's mass is proportional to the fine structure constant ...

[[In Cl(1,25) E8 Physics the gauge symmetry of the force determines the geometry of the Schwinger Source and its Green's Function.]]

The electron mass is one member of a mass doublet, predicted by this theory. The other member, the muon, arises because occasionally the observed electron can excite a pair of the background, which in turn changes the features of the geometry of space-time in the vicinity of the electron. ...

[[In Cl(1,25)E8 Physics the "excite" producing second and third generations is due to World-Lines traversing CP2 Internal Symmetry Space as well as M4 Physical Spacetime of M4xCP2 Kaluza-Klein]] Because the excitation of the pair is due to an electromagnetic force,

the new mass ... is 3 / 2 alpha = 206 times greater than the old mass. ...

This theory also predicts that the proton should have a sister member of a doublet ...

To compute the inertial mass of the electron, consider first the frame of reference whose spatial origin is at the site of the observed electron, with the pairs of the background in motion relative to this point

Using the method of Green's functions ... we see that the quaternion metrical field ... in the linear approximation, reduce to an integral equation with ... solutions ...[that]... are the linear approximation ... to the spin-affine connection field ... the solutions ... of the integral Equation ... lead directly to the (squared) mass eigenvalues ... the eigenvalues of the mass operator are the absolute values of the squares of the matrix elements above

•••

The pairs interact with each other in a way that makes them appear to some 'observed' constituent electron as 'photons'. ... Nevertheless,the pairs do have 'inertia' by virtue of their bound electrons and positrons that are not , in fact, annihilated. ... From a distance greater than a 'first Bohr orbit' of one of the particle components of a pair, it appears, as a unit , to be an electrically neutral object. But as the (observed) electron comes sufficiently close to the pair so as to interact with its separate components, energy is used up in exciting the pair, thereby decreasing the relative speed between the pair and the observed electron.

If the primary excitation of a pair (as 'seen' by the observed electron) is quadrupolar, and if the ground state of the pair corresponds to n = 1; then the

first excited Bohr orbital with a quadrupolar component is the state with n' = 3.

[[Quadrupolar implies 4+4 Kaluza-Klein of Cl(1,25) E8 Physics]]

With these values ... it follows that the ratio of mass eigenvalues is ... 3 / 2 alpha = 206 ... The reason for this is that the curvature of space-time, in the vicinity of the observed electron, that gives rise to its inertia, is a consequence of the electromagnetic coupling between the matter components of the system. ...

Summing up, the inertial mass of an elementary (spinor) particle was determined by the curvature of space-time in its vicinity, representing the coupling of this particle to its environment of particle-antiparticle pairs.

[[Green's functions for each force imply geometric structure of Schwinger Sources]]

The significant domain of space populated by pairs that contributes to the electron mass is the order of 10^{-15} cm ,,,

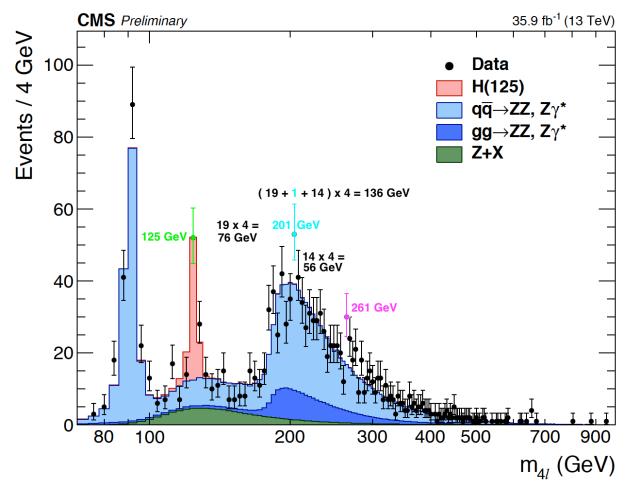
[[Schwinger Source size in Cl(1,25) E8 Physics is much smaller, about 10⁽⁻²⁴⁾ cm]]

Because the coupling of the observed electron to the pairs - that gives it inertia - is electromagnetic, the electron's mass is proportional to the fine structure constant - which is a measure of the strength of this coupling. ...".

Appendix - Experiments Observing Higgs-Tquark 3-state System

LHC 2016 Sees 3 Higgs Mass States

At 35.9 /fb = 3.59 Quadrillion events in the Higgs -> ZZ -> 4I channel CMS PAS HIG-16-041 (Figure 3 left) indicated 3 Higgs Mass States:



The histogram, discussed at Moriond March 2017, has bins of 4 GeV width, so that CMS analysis shows two higher Higgs mass states:

middle-mass Higgs state (cyan) with mass 201 GeV

high-mass Higgs state (magenta) with mass 261 GeV

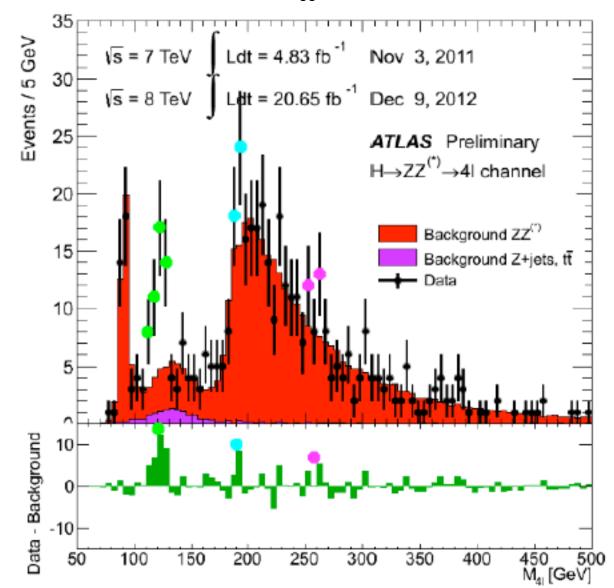
The CMS observation of 261 GeV for the high-mass Higgs state is somewhat higher than the theoretical value given by Koichi Yamawaki in hep-ph/9603293 where he says: "... the four-fermion theory in the presence of gauge interactions (... gauged Nambu-Jona-Lasinio (NJL) ... model) can become renormalizable and nontrivial ... The Higgs boson was predicted as a tbar-t bound state ... Its mass was ... calculated by BHL ... [Bardeen-Hill-Lindner] ... through the full RG equation ... the result being ... MH = mt x 1.1 at 10^19 GeV ...[which gives]... MH = 239 +/- 3 GeV ..."

The CMS observation of 201 GeV for the middle-mass Higgs state is also somewhat higher than the theoretical value given by Hashimoto, Tanabashi, and Yamawaki in hep-ph/0311165 where they say:

"... We perform the most attractive channel (MAC) analysis in the top mode standard model with TeV-scale extra dimensions for ...[Kaluza-Klein type]... dimension... D=8 ... $m_t = 172-175$ GeV and $m_H=176-188$ GeV ...".

In both cases

the CMS observed mass is about 20 GeV higher than the theoretical mass which is close enough to show that the theory is fundamentally realistic but indicates that further experimental data and study of data analysis and consideration of refinements of the theoretical models would be useful.



In Run-1 ATLAS had seen indications of Higgs mass states around 190 and 260 GeV:

In my CI(1,25) E8 physics model (viXra 1602.0319) the Higgs is not seen as a single fundamental scalar particle, but rather the Higgs is seen as a fermionic condensate and part of a 3-state Higgs-Tquark System:

Non-perturbativity **Fermilab Tquark** 250 LHC Higgs 3 200 LHC Higgs 2 Higgs pole mass Mh in GeV 150 LHC Higgs 100 TSFermilabgroundTquark FermilabHighTguark 50 Stability Instability 0 250 0 100 200 50 150 Top pole mass M_t in GeV

3 Higgs and Tquark Mass States are decribed in detail in pages 148-152

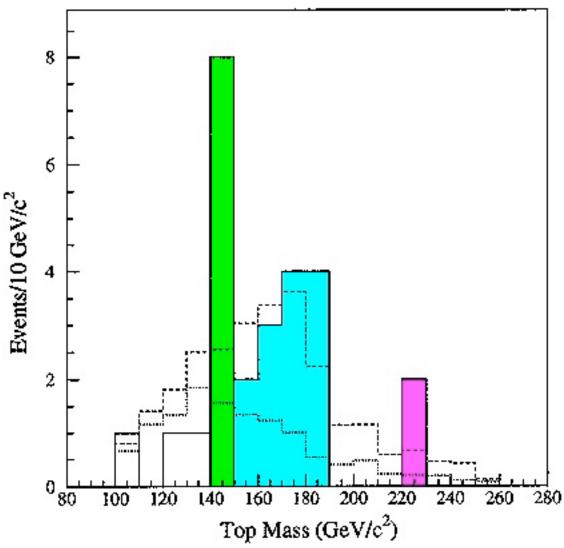
The 3 Higgs and Tquark Mass States are:

125 GeV H and 130 GeV Tq in Normal Stable Region 200 GeV H and 174 GeV Tq at Triviality / Composite H of K-K M4xCP2 260 GeV H and 220 GeV Tq at Vacuum Instability Critical Point / H VEV

The 3 Truth Quark Mass States corresponding to 3 Higgs Mass States have been observed by Fermilab. See pages 144-147

Why did Fermilab dismiss Low and High Truth Quark Mass States ? See page 153

A Graphic Overview of Experimental Results is at page 159



In 1994 a semileptonic histogram from CDF (FERMILAB-PUB-94/097-E)

showed all three states of the T-quark:

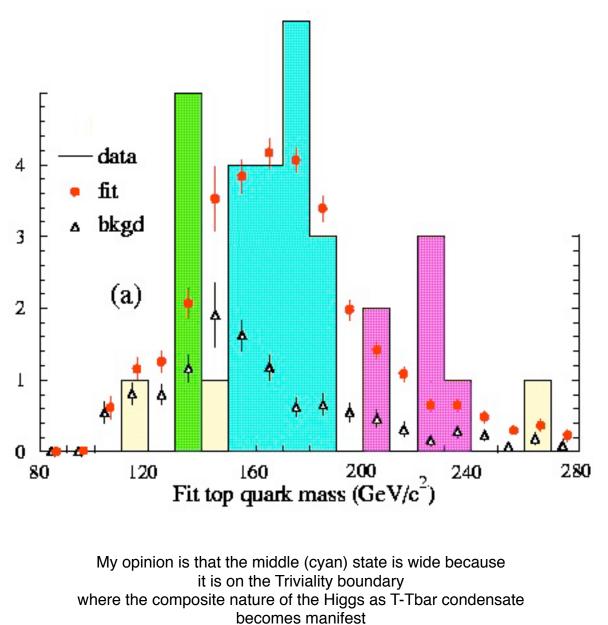
The green bar represents a bin in the 140-150 GeV range containing Semileptonic events considered by me to represent the Truth Quark.

The cyan bar represents a broader peak in the 160-180 GeV range that includes the 174 GeV Truth Quark at the Triviality Boundary of the H-Tq System.

The magenta bar represents a bin in the 220-230 GeV range of the Truth Quark at the Critical Point of the Higgs - Truth Quark System.

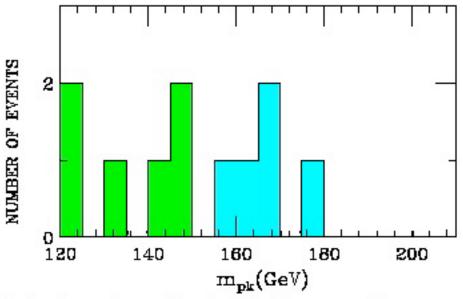
Why did Fermilab dismiss Low and High Mass States ? See page 153

The same three Tquark mass states were seen in 1997 by D0 (hep-ex/9703008) in this semileptonic histogram:



and

the low (cyan) state is narrow because it is in the usual non-trivial region where the T-quark acts more nearly as a single individual particle.

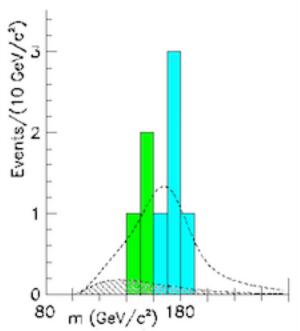


In February 1998 a dilepton histogram of 11 events from CDF (hep-ex/9802017)

The distribution of m_{pk} values determined from 11 CDF dilepton events available empirically.

shows both the low (green) state and the middle (cyan) T-quark state but

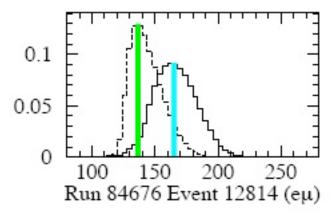
in October 1998 CDF revised their analysis by using only 8 Dilepton CDF events (hep-ex/9810029)



CDF kept the 8 highest-mass dilepton events, and threw away the 3 lowest-mass dilepton events that were indicated to be in the 120-135 GeV range, and shifted the

mass scale upward by about 10 GeV, indicating to me that Fermilab was attempting to discredit the low-mass T-quark state by use of cuts etc on its T-quark data.

In his 1997 Ph.D. thesis Erich Ward Varnes (Varnes-fermilab-thesis-1997-28 at page 159) said: "... distributions for the dilepton candidates. For events with more than two jets, the dashed curves show the results of considering only the two highest ET jets in the reconstruction ...

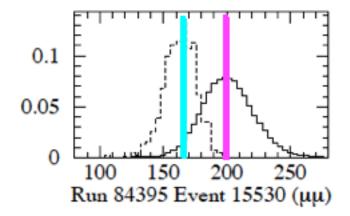


..." (colored bars added by me)

The event for all 3 jets (solid curve) seems to me to correspond to decay of a middle (cyan) T-quark state with one of the 3 jets corresponding to

decay from the Triviality boundary to the Normal Stable Region (green) T-quark state, whose immediately subsequent decay corresponds to the 2-jet (dashed curve) event at the low (green) energy level.

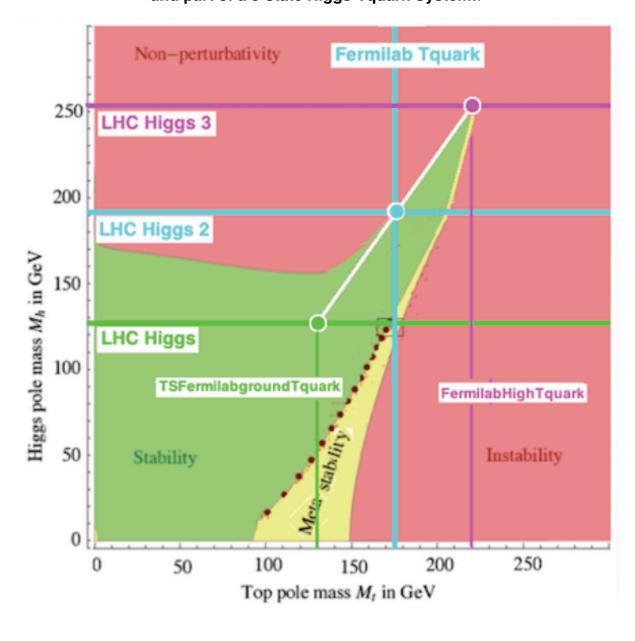
In the Varnes thesis there is one dilepton event with 3 jets (solid curve)



that seems to me to correspond to decay of a high (magenta) T-quark state with one of the 3 jets corresponding to

decay from the Critical Point down to the Triviality Boundary (cyan) T-quark state, whose immediately subsequent decay corresponds to the 2-jet (dashed curve) event.

In my CI(1,25) E8 physics model (viXra 1602.0319) the Higgs is not seen as a single fundamental scalar particle, but rather the Higgs is seen as a fermionic condensate and part of a 3-state Higgs-Tquark System:.



The Green Dot where the White Line originates in our Normal Stable Region is the low-mass state of a 130 GeV Truth Quark and a 125 GeV Higgs.

The Cyan Dot where the White Line hits the Triviality Boundary leaving the Ordinary Phase is **the middle-mass state of a 174 GeV Truth Quark and Higgs around 200 GeV**. It corresponds to the Higgs mass calculated by Hashimoto, Tanabashi, and Yamawaki in hep-ph/0311165 where they say:

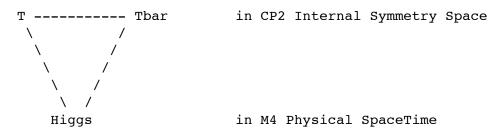
"... We perform **the most attractive channel (MAC)** analysis in the top mode standard model with TeV-scale extra dimensions, where the standard model gauge bosons and the third generation of quarks and leptons are put in D(=6,8,10,...) dimensions. In such a model, bulk gauge couplings rapidly grow in the ultraviolet region. In order to make the scenario viable, only the attractive force of the top condensate should exceed the critical coupling, while other channels such as the bottom and tau condensates should not. We then find that **the top condensate can be the MAC for D=8** ... We predict masses of the top (m_t) and the Higgs (m_H) ... based on the renormalization group for the top Yukawa and Higgs quartic couplings with the compositeness conditions at the scale where the bulk top condenses ... for ...[Kaluza-Klein type]... dimension... D=8 ...

m_t = 172-175 GeV and m_H=176-188 GeV ...".

As to composite Higgs and the Triviality boundary, Pierre Ramond says in his book Journeys Beyond the Standard Model (Perseus Books 1999) at pages 175-176: "... The Higgs quartic coupling has a complicated scale dependence. It evolves according to d lambda / d t = $(1 / 16 \text{ pi}^2)$ beta_lambda where the one loop contribution is given by beta_lambda = 12 lambda^2 - ... - 4 H ... The value of lambda at low energies is related [to] the physical value of the Higgs mass according to the tree level formula m_H = v sqrt(2 lambda) while the vacuum value is determined by the Fermi constant ... for a fixed vacuum value v, let us assume that the Higgs mass and therefore lambda is large. In that case, beta_lambda is dominated by the lambda^2 term, which drives the coupling towards its Landau pole at higher energies. Hence the higher the Higgs mass, the higher lambda is and the close[r] the Landau pole to experimentally accessible regions. This means that for a given (large) Higgs mass, we expect the standard model to enter a strong coupling regime at relatively low energies, losing in the process our ability to calculate. This does not necessarily mean that the theory is incomplete, only that we can no longer handle it ... it is natural to think that this effect is caused by new strong interactions, and that the Higgs actually is a composite ... The resulting bound on lambda is sometimes called the triviality bound. The reason for this unfortunate name (the theory is anything but trivial) stems from lattice studies where the coupling is assumed to be finite everywhere; in that case the coupling is driven to zero, yielding in fact a trivial theory. In the standard model lambda is certainly not zero. ...".

Middle Mass State Cross Section:

In the Cl(1,25) E8 model the D = 8 Kaluza-Klein is M4 x CP2 and the Middle-Mass Higgs structure is not restricted to Effective M4 Spacetime as is the case with the Low-Mass Higgs Ground State but extends to the full 4+4 = 8-dim structure of M4 x CP2 Kaluza-Klein.

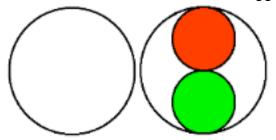


Therefore the Mid-Mass Higgs looks like a 3-particle system of Higgs + T + Tbar.

The T and Tbar form a Pion-like state. Since Tquark Mid-Mass State is 174 GeV the Middle-Mass T-Tbar that lives in the CP2 part of (4+4)-dim Kaluza-Klein has mass (174+174) x (135 / (312+312) = 75 GeV.

The Higgs that lives in the M4 part of (4+4)-dim Kaluza-Klein has, by itself, its Low-Mass Ground State Effective Mass of 125 GeV. So, the total Mid-Mass Higgs lives in full 8-dim Kaluza-Klein with mass 75+125 = 200 GeV.

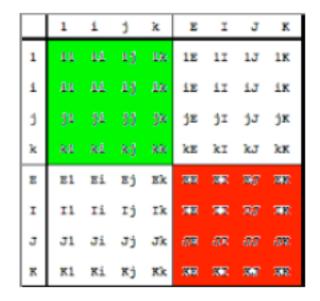
This is consistent with the Mid-Mass States of the Higgs and Tquark being on the Triviality Boundary of the Higgs - Tquark System and with the 8-dim Kaluza-Klein model in hep-ph/0311165 by Hashimoto, Tanabashi, and Yamawaki.As to the cross-section of the Middle-Mass Higgs



consider that the entire Ground State cross-section lives only in 4-dim M4 spacetime (left white circle)

while the Middle-Mass Higgs cross-section lives in full 4+4 = 8-dim Kaluza-Klein (right circle with red area only in CP2 ISS and white area partly in CP2 ISS with only green area effectively living in 4-dim M4 spacetime) so that

our 4-dim M4 Physical Spacetime experiments only see for the Middle-Mass Higgs a cross-section that is 25% of the full Ground State cross-section.



The 25% may also be visualized in terms of 8-dim coordinates {1,i,j,k,E,I,J,K}

in which $\{1,i,j,k\}$ represent M4 and $\{E,I,J,K\}$ represent CP2.

The Magenta Dot _____ at the end of the White Line is the high-mass state of a 220 GeV Truth Quark and a 240 GeV Higgs.

It is at the Critical Point of the Higgs-TruthQuark System

with respect to Vacuum Instability and Triviality.

It corresponds to the description in hep-ph/9603293 by Koichi Yamawakil:

"... the top quark condensate proposed by Miransky, Tanabashi and Yamawaki (MTY) and by Nambu independently ... entirely replaces the standard Higgs doublet by a composite one formed by a strongly coupled short range dynamics (four-fermion interaction) which triggers the top quark condensate. The Higgs boson emerges as a tbar-t bound state and hence is deeply connected with the top quark itself. ... the BHL [Bardeen-Hill-Lindner] formulation of the top quark condensate ... is based on the RG equation combined with the compositeness condition ... [it] start[s] with the SM Lagrangian ... BHL is crucially based on the perturbative picture ... [which]... breaks down at high energy near the compositeness scale $\land ...$ [10^19 GeV]... there must be a certain matching scale \land _Matching such that the perturbative picture (BHL) is valid for mu < \land _Matching, while only the nonperturbative picture (MTY) becomes consistent for mu > \land Matching ...

However, thanks to the presence of a quasi-infrared fixed point, BHL prediction is numerically quite stable against ambiguity at high energy region ...

Then we expect mt = mt(BHL) = ... = 1/(sqrt(2)) ybart v within 1-2%, where ybart is the quasi-infrared fixed point given by Beta(ybart) = 0 in ... the one-loop RG equation ... The composite Higgs loop changes ybart^2 by roughly the factor Nc/(Nc +3/2) = 2/3 compared with the MTY value, i.e., 250 GeV -> 250 x sqrt(2/3) = 204 GeV, while the electroweak gauge boson loop with opposite sign pulls it back a little bit to a higher value. The **BHL value is then given by mt = 218 +/- 3 GeV**, at $\Lambda = 10^{19}$ GeV. The Higgs boson was predicted as a tbar-t bound state with a ... mass ... calculated by BHL through the full RG equation ...

the result being ... MH / mt = 1.1 at Λ = 10^19 GeV ...".

Therefore $MH = 1.1 \times 218 = 240 \text{ GeV}$ which is roughly the Higgs VEV.

High Mass State Cross Section:

As with the Middle-Mass Higgs,

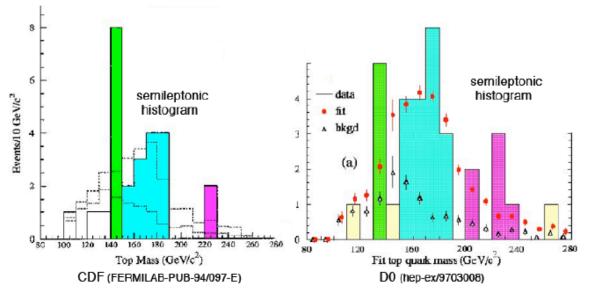
the High-Mass Higgs lives in all 4+4 = 8 Kaluza-Klein M4 x CP2 dimensions so its cross-section is also about 25% of the Higgs Ground State cross-section.

Why did Fermilab dismiss Low and High Mass States ?

The Truth Quark High Mass State peak in the 1994 CDF semileptonic histogram is low, only 2 events out of a total of 26, so they could be dismissed as insignificant, but the Truth Quark Low Mass State peak is not low (8 of 26 events) and should not be so easily dismissed by CDF. However, in 1994, CDF in FERMILAB-PUB-94/097-E did dismiss the Low Mass peak, saving merely

"... We assume the mass combinations in the 140 to 150 GeV/c² bin represent a statistical fluctuation since their width is narrower than expected for a top signal. ...". I strongly disagree with CDF's "statistical fluctuation" interpretation.

If it were merely a "statistical fluctuation" then it would have been highly improbable for the 1997 D0 semileptonic histogram to have shown a very similar Low Mass peak, but in fact a very similar Low Mass peak is what D0 did find in 1997:



For more detailed analysis of how Fermilab data over many years has supported the reality of three mass states of the Truth Quark, see viXra 1602.0319 . Fermilab's dismissal of the Low Mass Truth Quark peak around 130 GeV in its own data was not only a dismissal of my hep-ph/9301210 prediction but also a dismissal of other independent theoretical predictions of Truth Quark mass:

1982 - Inoue, Kakuto, Komatsu, and Takeshita in Aspects of Grand Unified Models with Softly Broken Suypersymmetry (Prog. Theor. Phys. 68 (1982) 927) relate supersymmetry to electro-weak symmetry breaking by radiative corrections and renormalization group equations, and find that the renormalization group equations have a fixed point related to a T-quark mass of about 125 GeV.

1983 - Alvarez-Gaume, Polchinski, and Wise in Nuclear Physics B221 (1983) 495-523 : "... The renormalization group equation ... tends to attract the top quark mass towards a fixed point of about 125 GeV ...". 1984 - Ibanez and Lopez in Nuclear Physics B233 (1984) 511-544 did supergravity calculations similar to Alvarez-Gaume, Polchinski, and Wise.

1993 - Chamseddine and Frohlich in hep-ph/9307209 : "... Connes ... non-commutative geometry [NCG] provides a geometrical interpretation of the Higgs field ... the only solutions ... occur in the narrow band ... Higgs mass 117.3 < mH < 142.6 GeV ... with ... corresponding top quark mass ... 146.2 < mt < 147.4 GeV ...". Later basic NCG calculation (see arXiv 1204.0328) indicated Tquark mass upper bound of sqrt(8/3) mW = 130 GeV .

The Renormalization Group and NCG predictions have been confirmed by the LHC 2016 run which showed not only the 125 GeV Higgs Mass State but also 3 Higgs Mass States corresponding to 3 Truth Quark Mass States including the Low Mass Truth Quark State dismissed by Fermilab.

Why would Fermilab dismiss the Low Mass Truth Quark peak in its own data, even though it had theoretical support from Renormalization Group and NCG, not to mention my isolated unconventional theory ?

To understand the hostility of Fermilab to a Low Mass Truth Quark State, you must look at the details of the process whereby Fermilab sought to discover the Truth Quark after CDF's 1988-89 run which produced a dilepton candidate event.

Kent Staley in "The Evidence for the Top Quark" (Cambridge 2004) said:

"... CDF searched for the top [quark] ... in ... the "dilepton" mode ...

CDF stopped taking data at the end of May 1989 ...

Kumi Kondo's Dynamical Likelihood Method ... would give a kinematical reconstruction of events and then calculate the likelihood of that reconstruction using the dynamics of the hypothesized decay process ... Kondo found that ... the lone dilepton candidate found during the 1988-9 run ... could be reconstructed with his method as the decay of a top-antitop pair, with a top mass of around 130 GeV/c2 ...

Goldstein, Sliwa, and Dalitz ... were trying to apply their method to the first CDF dilepton event, the same published e-mu event from the 1988-9 run that Kondo had analyzed ... In February 1992 ... Goldstein and Sliwa were invited to present their method ... at a meeting of the heavy flavors group (the precursor to the top group) ... Sliwa showed ... a bump ... at a top-quark mass of about 120 GeV/c2 ...

in May 1992 ... Goldstein, Sliwa, and Dalitz ... present[ed] ... analysis of data from ... 1988-9 ...[saying]... "The plots show very clearly a well separated enhancement around Mt = 135 GeV in the accumulated probability distributions, as expected by the Monte Carlo studies" ...

The top mass estimates from the Dalitz-Goldstein-Sliwa analysis ... consistently fell into the 130-140 GeV/c2 range ...

considerably lower than the later estimate of 174 GeV/c2

that appeared in CDF's paper claiming evidence for the top quark

•••

Then, a very strange thing happened: ...

New Scientist, dated June 27, 1992 ... announced ... "A claim that the top quark has been found is being suppressed by scientists at the Fermilab particle physics centre ... If Dalitz turns out to be correct ... the main credit for finding the particle will go to Dalitz, a scientist outside Fermilab ..." ... Dalitz, Goldstein, and Sliwa appeared in the article as a "rival group", the publication of whose paper CDF was "blocking", and the author reported Goldstein saying that he was "quite confident' that they have discovered the existence and the mass of the (Top) quark."

...

An article ... in the July 24 issue of Science ... recounted how the results of the Sliwa-Goldstein-Dalitz analysis were presented to CDF ...

Goldstein and Dalitz were subsequently excluded from CDF top group meetings ... CDF physicist... "Shochet says **CDF member Sliwa violated an unwritten code of ethics by sharing data with outsiders**."

•••

Sliwa denied that he had made substantive information about CDF's unpublished data available to Dalitz and Goldstein

•••

the unpleasant atmosphere generated by the controversy surrounding Sliwa's work hampered progress on the Dalitz-Goldstein-Sliwa method ...

Krys really never got the time of day after [the appearance of the articles in New Scientist and Science]...[He] took it very personally, and responded very personally

he was "spurned by the rest of the collaboration: because he was acting singly, and not in a larger collaboration" ...".

Tommaso Dorigo has written a book, "Anomaly"

(to be published by World on 5 Nov 2016),

that may give more details of the situation. He has blogged and commented on it over the past years (2006-2013), saying in part:

"... In **December 1988** a one-day workshop was organized in the Ramsey auditorium, the conference room at the basement floor of the Hirise, the main building of the Fermi National Accelerator Laboratory. The workshop was the first of a series of meetings that would take place in the course of the following few years, and it was specifically devoted to focused discussions on the top quark search, which was being performed independently by several groups of CDF physicists

...

one got the feeling that a well-defined strategy for the top search was missing. Indeed, back then it was not even clear to most CDF researchers that the main background to top production was constituted by events featuring a W boson together with hadronic jets produced by QCD radiation

•••

Finally, the time came for the talk by Kuni Kondo. Prof. Kondo was a Japanese physicist who led a sizable group of researchers from the University of Tsukuba. In his late fifties, he was lean, not tall, with black hair combed straight above an incipient baldness; he usually dressed in black or grey suits. He was a charming and very polite person, who spoke with a soft tone of voice and smiled a lot.

It looked like nothing could ever upset him.

Kondo had devised a very complex, deep method to discriminate top guark events from the background, based on an analysis approach he had dubbed "dynamical likelihood" which would become a sophisticated standard only a decade later, but which was taken with guite a bit of scepticism at the time; in private, guite a few of his American and Italian colleagues would even make silly jokes on it. The method consisted in constructing probability distributions for the observed kinematics of the events, which could then be used to derive the likelihood that the events were more signal-like or background-like.

It is ironic to think that nowadays all the most precise measurements of the mass of the top quark rely on the method called "matrix element", which is nothing but Kondo's original idea recast in the context of a measurement of the mass rather than the discrimination of a top signal. Kondo was way ahead of his time, and like most pioneers in science he did not have an easy life getting his work appreciated and accepted, in a situation dominated by a conservative mainstream.

It is by now four in the afternoon, and Kondo finally gives a full status report of his analysis. His presentation is thorough and yet almost unintelligible by a good half of his listeners; his analysis includes highly unorthodox and yet brilliant tricks, like taking a jet from one event and mixing it in with other jets in a different event to study the behaviour of some of his selection variables for background events. His colleagues listen in an atmosphere of disbelief mixed with awe. Despite the complexity of the material and the possibility to object on a hundred of details, no questions are asked.

As Kondo reaches the end of his talk, he concludes with a tone of voice just a millidecibel higher than the rest of his speech:

"And therefore", a pause, and then "I think we have discovered the top quark".

The audience remains silent.

The convener is a tall, lean guy with a sharp nose and a penetrating stare; he looks like an English gentleman from a XIXth century novel, especially thanks to his considerable aplomb. He is not impressed, and that much does show.

"Thank you very much Kuni. Is there any question ?", one, two, three, four,

"...No questions. Okay, thanks again Kuni. The next speaker is...".

In retrospect the convener's attitude and lack of consideration toward an esteemed colleague and a visitor from another country, who had brought to the experiment lots of resources and had contributed significantly to the detector construction, sounds at least rude and unjustified.

Still, back then CDF was not a place where people would exchange courtesies and compliments (it never was, in truth): there everybody had to work hard and the only way to earn the respect of colleagues was through the good physics output of one's analysis results. If your analysis methods were not considered publishable or your results were thought fallacious, you would be considered a potential threat to the good name of the experiment, and you would suffer little short than boycott.

But the way Kondo was treated was all flowers in comparison to what other physicists would experience, along the way to the top discovery

[1992] I had started working on CDF ... and I remember that one of the very first articles I read was the limit on top quark production where the famous dilepton ttbar candidate was mentioned. An event that is indeed most likely the first clear top-antitop decay detected in a particle physics experiment

Back then, Krisztof Sliwa analyzed the ttbar candidate by CDF in the dileptonic final state with an analysis called "neutrino weighting technique" which has later become a standard, and worked with Dalitz and Goldstein on a paper which was not authorized by the CDF collaboration

... CDF, as a collection of physicists, did feel betrayed by Chris Sliwa. I do not know how clear was the violation of internal rules of the experiment, but for sure that was the sentiment circulating those days in the corridors of the CDF trailers

...

there was this air of suspicion around in 1992

As if somebody had committed Heresy! ...".

Back in the 1990s, a very bad thing had happened:

Two issues had arisen:

1 - Physics Issue - Does the 130 GeV Truth Quark Low Mass State exist and did the Kondo and/or Sliwa-Goldstein-Dalitz Likelihood Method find it ?

2 - Bureaucratic Issue - Was Sliwa's sharing of CDF data with Goldstein and Dalitz a serious violation of an unwritten ethical code ?

Fermilab, as a large physics collaboration with power over jobs and funding, was in position to decide which of the issues should be pursued or suppressed.

It could have decided to pursue both issues, but it did not.

It decided to suppress the Physics Issue (and the Truth Quark Low Mass State) so that individual outsiders (and their ideas) would go away and only Fermilab consensus ideas would survive in the world of physics, and the Fermilab consensus was that the one and only Tquark Mass State, the 174 GeV Mass State, would be recognized in the world of physics.

It decided to pursue the Bureaucratic Issue because that allowed Fermilab to use its jobs-funding power to enforce its consensus view that the one and only Tquark Mass State was the 174 GeV Mass State.

So, instead of searching for Truth, Fermilab asserted its Power.

Regrettably, this is a common characteristic of Human Political Bureaucracies, as is exemplified by attacks on Snowdon and Assange as criminals for sharing Truthful Information with the public thus deflecting attention from the True Facts to details of Criminal Prosecution and instilling fear in others who might think about telling the Truth.

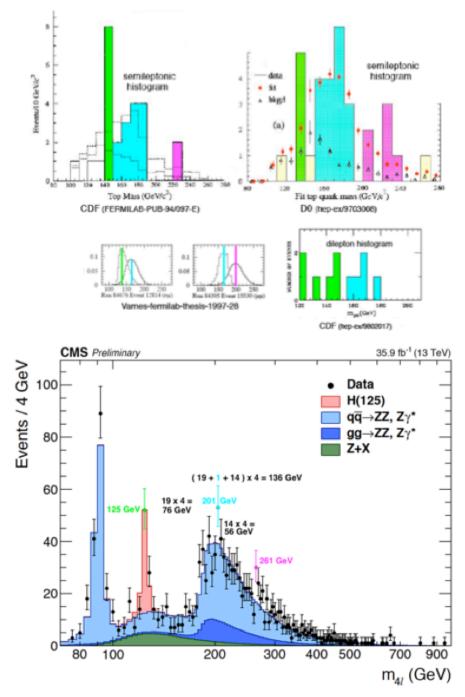
Now a quarter century later, a very good thing has happened:

In this case, suppression of the Physics Issue failed because:

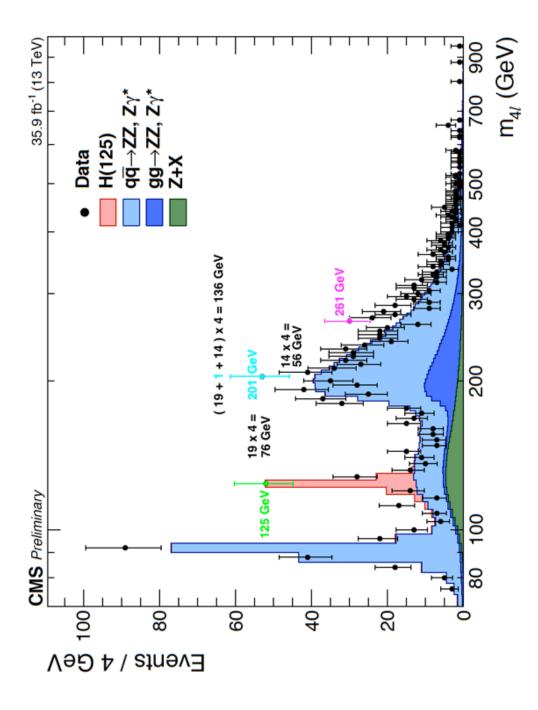
the Physics Issue has been raised by the LHC 2016 run data which shows evidence of 3 Higgs Mass States which correspond to 3 Truth Quark Mass States and

the 3-Mass-State-T-quark should now be known by its true name:

the Truth Quark.

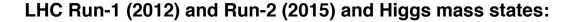


Graphic Overview of Experimental Results

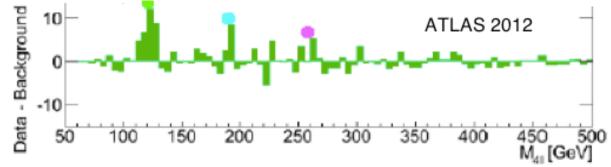


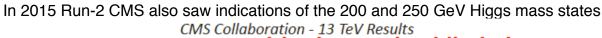
LHC Run-2 (2016) and Higgs mass states:

(histogram adapted from Figure 3 (left) of CMS PAS HIG-16-041)

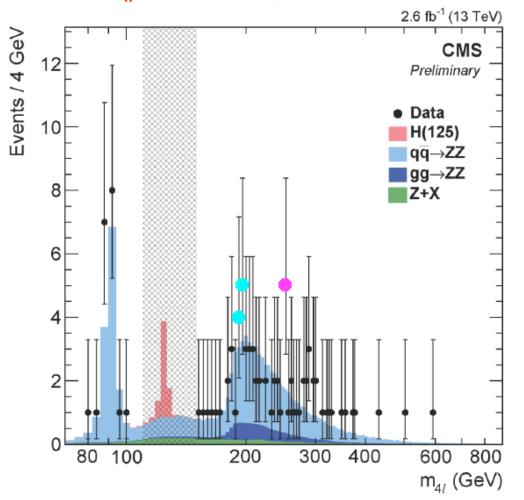


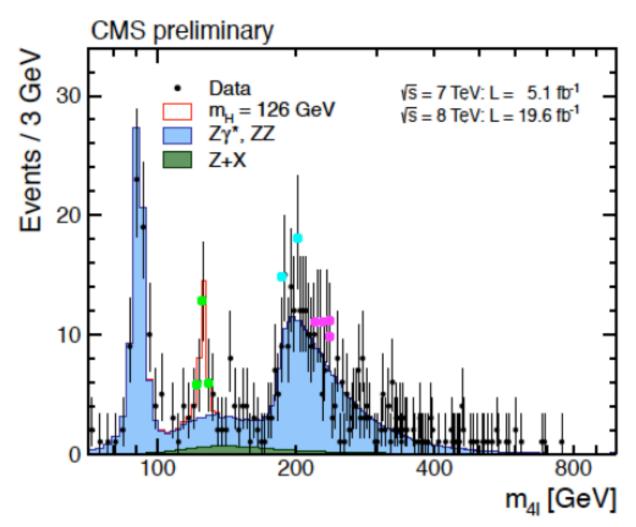
By the end of Run-1 in 2012 the LHC had seen clear evidence for a Higgs (green dot) with mass around 125 GeV and the expected Standard Model cross section. It also saw in the Higgs -> ZZ -> 4I channel two more peakss (cyan and magenta dots)



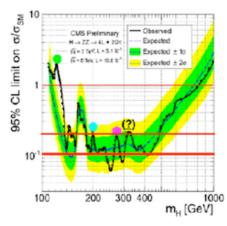








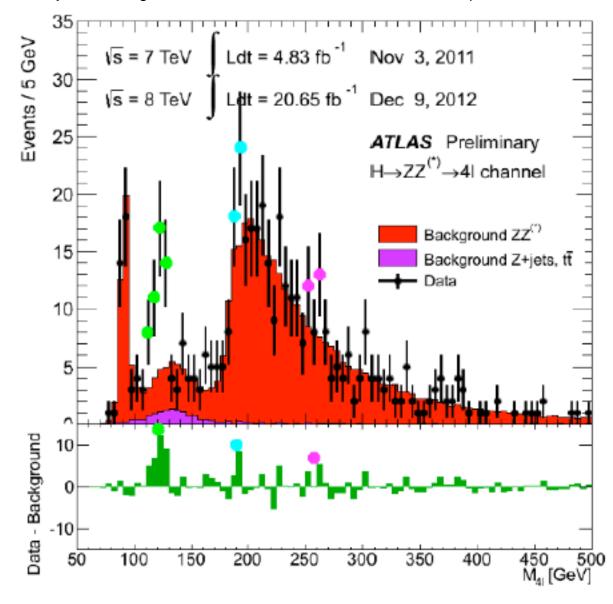
and with cross sections around 25% of SM expectation



CMS Run-1 also saw a (?) peak around 320 GeV that I expect to go away with 2016 Run-2 data. The two unmarked peaks around 160 and 180 GeV are probably due to WW and ZZ.

Further,

in Run-1 ATLAS had seen indications of Higgs mass states around 200 and 250 GeV

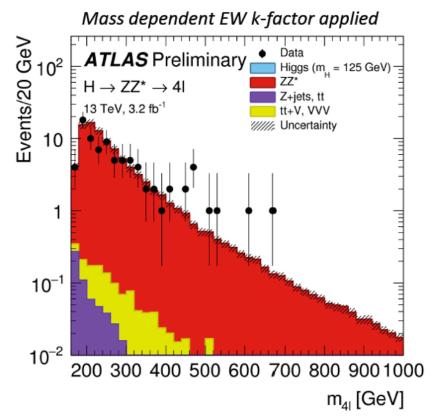


whose cyan and magenta dots coincide with the CMS 2015 Run-2 positions

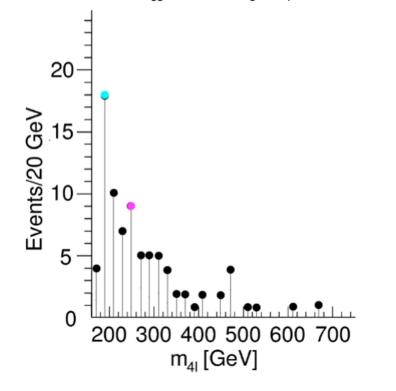
ATLAS Run-1 did not see the (?) CMS Run-1 peak around 320 GeV as ATLAS saw an excess bin adjacent to two deficient bins.

In 2015 Run-2 did ATLAS see indications of 200 and 250 GeV Higgs mass states ?

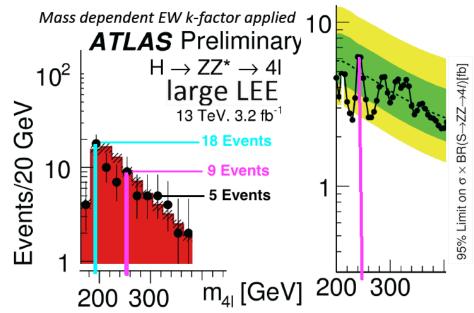
Here is what ATLAS reported (slide 22 by Marumi Kado) on 15 Dec 2015 LPCC Special Seminar:



Here is that ATLAS 2015 Higgs -> ZZ -> 4I histogram replotted with linear scale:



Here are some details (from slide 22 by Maarumi Kado for 15 Dec 2015 LPCC Special Seminar):



In my opinion the indications of 200 (cyan) and 250 (magenta) GeV Higgs mass states are there, but are obscured by:

1 - a large LEE effect that is NOT appropriate for the 200 and 250 GeV Higgs mass states that were predicted by my E8 Physics model and indicated by prior Run-1 data

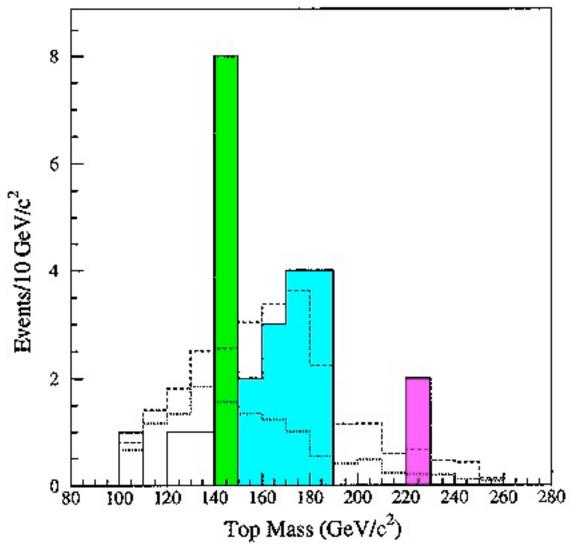
2 - the Brazil Band plot does NOT show the peak just below the 200 GeV line

2 - use of a log scale for the histogram of Events/20 GeV makes it hard to see the details of the Events around 200 and 250 GeV.

It seems clear to me that the linear plot indicates that the 200 GeV (cyan) peak and the 250 GeV (magenta) peak are serious candidates with over 5 Events that might well be confirmed by 2016 data as real Higgs mass states.

Three T-quark mass states

The 174 GeV Tquark mass state (cyan dot) is not controversial. It has been observed at Fermilab since 1994, when a semileptonic histogram from CDF (FERMILAB-PUB-94/097-E)

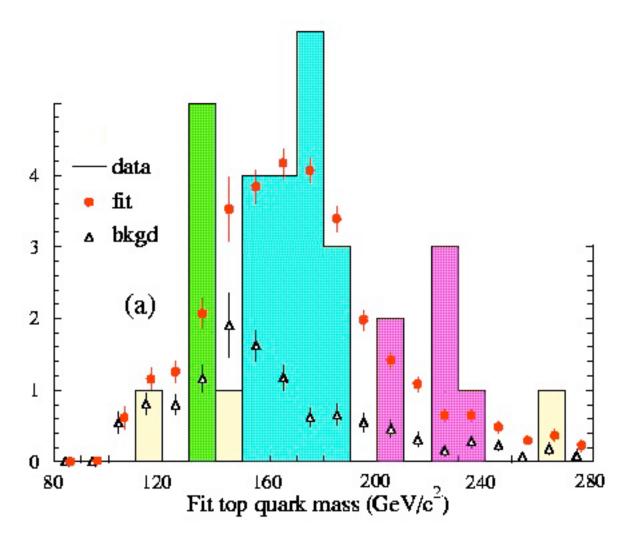


showed all three states of the T-quark.

In particular, the green bar represents a bin in the 140-150 GeV range containing Semileptonic events considered by me to represent the Truth Quark, but as to which CDF said "... We assume the mass combinations in the 140 to 150 GeV/c^2 bin represent a statistical fluctuation since their width is narrower than expected for a top signal. ...". I strongly disagree with CDF's "statistical fluctuation" interpretation, based on my interpretations of much Fermilab T-quark data.

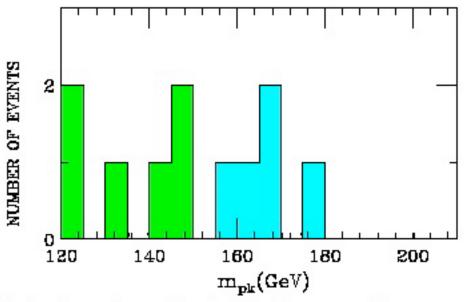
The same three Tquark mass states were seen in 1997 by D0 (hep-ex/9703008)

in this semileptonic histogram:



The fact that the low (green) state showed up in both independent detectors indicates a significance of 4 sigma.

My opinion is that the middle (cyan) state is wide because it is on the Triviality boundary where the composite nature of the Higgs as T-Tbar condensate becomes manifest and the low (cyan) state is narrow because it is in the usual non-trivial region where the T-quark acts more nearly as a single individual particle.

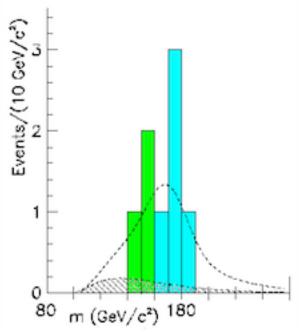


Further, in February 1998 a dilepton histogram of 11 events from CDF (hep-ex/9802017)

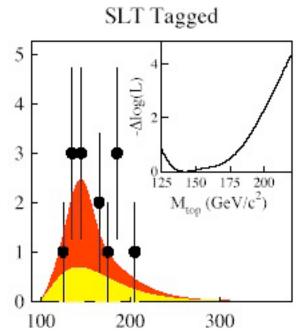
The distribution of m_{pk} values determined from 11 CDF dilepton events available empirically.

shows both the low (green) state and the middle (cyan) T-quark state but

in October 1998 CDF revised their analysis using 8 Dilepton CDF events (hep-ex/9810029)

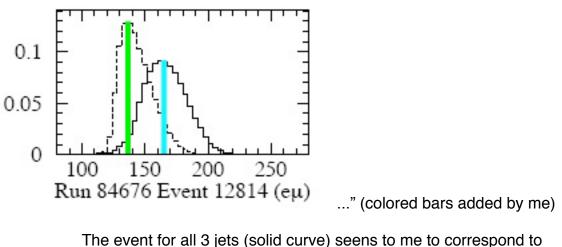


shows that CDF kept the 8 highest-mass dilepton events, and threw away the 3 lowestmass dilepton events that were indicated to be in the 120-135 GeV range, and shifted the mass scale upward by about 10 GeV, indicating to me tthat Fermilab was attempting to discredit the low-mass T-quark state by use of cuts etc on its T-quark data. In 1998 an analysis of 14 SLT tagged lepton + 4 jet events by CDF (hep-ex/9801014)



showed a T-quark mass of 142 GeV (+33,-14) that seems to me to be consistent with the low (green) state of the T-quark.

In his 1997 Ph.D. thesis Erich Ward Varnes (Varnes-fermilab-thesis-1997-28 at page 159) said: "... distributions for the dilepton candidates. For events with more than two jets, the dashed curves show the results of considering only the two highest ET jets in the reconstruction ...



The event for all 3 jets (solid curve) seens to me to correspond to decay of a middle (cyan) T-quark state with one of the 3 jets corresponding to decay from the Triviality boundary down to the low (green) T-quark state, whose immediately subsequent decay corresponds to the 2-jet (dashed curve) event at the low (green) energy level. As to the T-quark width for the 174 GeV mass state, which appears in the 1994 CDF and 1997 D0 semileptonic histograms to be about 40 GeV, which is 4 of the 10 GeV histogram bins,

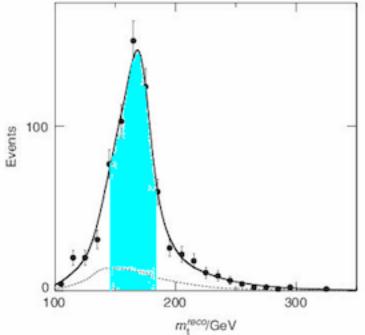
Mark Thomson, in "Modern Particle Physics" (Cambridge 2013) says:

"... Decay of the top quark ... The total decay rate is ...

$$\Gamma(t \to bW^{+}) = \frac{G_{\rm F}m_{\rm t}^{3}}{8\sqrt{2}\pi} \left(1 - \frac{m_{\rm W}^{2}}{m_{\rm t}^{2}}\right)^{2} \left(1 + \frac{2m_{\rm W}^{2}}{m_{\rm t}^{2}}\right),$$

... For ... mt = 173 GeV ... the lowest-order calculation of the total decay width of the top quark gives Γ t = 1.5 GeV ...

The total width of the top quark is measured to be Γ t = 2.0 +/- 0.6 GeV. The top width is determined much less precisely than the top quark mass because the width of the distribution ...[color added to show correspondence to CDF and D0 histograms]...



... is dominated by the experimental resolution. ...".

The T-quark total width Γ t = 2 GeV is much smaller than the 40 GeV width experimentally observed at Fermilab and would, except for experimental resolution, fit well within one single bin in the 1994 CDF and 1997 D0 semileptonic histograms.

As to the T-quark width for the 130 GeV mass state, which appears in the 1994 CDF and 1997 D0 semileptonic histograms to be less than the 10 GeV histogram bin width, using the total width formula from Mark Thomson's book and paraphrasing:

"... For mt = 130 GeV ... the lowest-order calculation

of the total decay width of the top quark gives Γ t = about 0.5 GeV ...".

I think that the CDF explanation for the low mass T-quark peak in a single 10 GeV bin

"... We assume the mass combinations in the ... bin represent a statistical fluctuation since their width is narrower than expected for a top signal. ...".

is highly unlikely since a similar low mass single 10 GeV bin T-quark mass peak was observed by the independent D0 detector.

The mt = 130 GeV width of 0.5 GeV is only 1/20 of the 10 GeV bin width of that peak. The 20:1 = 10: 0.5 observed width : actual width ratio for mt = 130 GeV is the same as the 20:1 = 40: 2.0 observed width : actual width ratio for mt = 173 GeV.

What differences between the mt = 130 GeV and mt = 173 GeV states might affect their relative experimental resolutions ?

The mt = 130 GeV peak is in the normal Stable region

in which the T-quark is represented by a Schwinger Source in M4 Physical Spacetime which Schwinger Source has Green's Function structure based on Kernel Functions of Bounded Symmetric Domains whose symmetry is that of the T-quark. Since it is a simple Schwinger Source it has simple W - b - 2 jet decay.

The mt = 173 GeV peak is on the boundary

of the Non-Perturbativity region where the composite nature of Higgs as T-quark Condensate becomes manifest, as does the 8-dim nature of Kaluza-Klein spacetime M4 x CP2 with M4 Physical Spacetime and CP2 Internal Symmetry Space where CP2 = SU(3) / SU(2)xU(1) has symmetries of the Standard Model Gauge Groups. Its decay scheme is more complicated, with 2 stages:

175 to 130 GeV, a process of the Higgs - T-quark condensate system of E8 Physics and simple W - b - 2 jet decay of the 130 GeV intermediate state.

The wider width of the 173 GeV decay peak is due to the Higgs - T-quark condensate process.

The 1997 UC Berkeley PhD thesis of Erich Ward Varnes gives details of some D0 events and analysis, based on the Standard Model view of one T-quark mass state: "... the leptonic decays of the t tbar events are divided into two broad categories: the lepton plus jets and dilepton channels.

The former has the advantage of a large branching ratio, accounting for about 30% of all t tbar decays, with the disadvantage that electroweak processes or detector misidentification of fina-state particle can mimic the t tbar signal relatively frequently. Conversely,

the dilepton channels have lower backgrounds, but account for only 5% of all decays. ...

The kinematic selection of dilepton events is summarized in Table 5.2 ...

	ee	$e\mu$	$\mu\mu$	
Leptons	$E_T > 20 \text{ GeV}$	$E_T(e) > 15 \text{ Gev}, p_T(\mu) > 15 \text{ GeV/c}$	$p_T(\mu) > 15 \text{ GeV/c}$	
	$ \eta < 2.5$	$ \eta(e) < 2.5$		
Jets	≥ 2 with $E_T > 20$ GeV and $ \eta < 2.5$			
$\not\!$	> 25 GeV	$\not\!$	N/A	
		$E_T^{\rm cal} > 10 { m ~GeV}$		
H_T^c	> 120 GeV	$> 120 { m ~GeV}$	> 100 GeV	

...

In the dilepton channels, one expects the final state to consist of two charged leptons, two neutrinos, and two b jets (see Fig. 6.1)

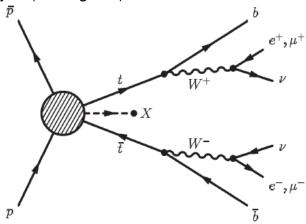


Figure 6.1: Schematic representation of $t\overline{t}$ production and decay in the dilepton channels.

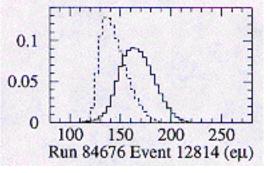
so that the final state is completely specified by knowledge of the energy four-vectors of these six particles ... there are ... kinematic constraints:

The invariant mass of each lepton and neutrino pair is equal to the W mass. The masses of the reconstructed t and that in the event are equal. •••

The result of reconstructing the top quark mass for a dilepton event is the distribution W(mt), which is evaluaed for 50 values of the top quark mass ... the intrinsic resolution of the dilepton mass reconstruction is much broader than the 4 GeV/c2 interval between assumed top quark masses ... the RMS of the typical W(mt) distribution ... typically lies between 35 and 40 GeV/c2 ...

•••

Figure 8.1: W(mt) distributions for the dilepton candidates. For events with more than two jets, the dashed curves show the results of considering only the two highest ET jets in the reconstruction ...

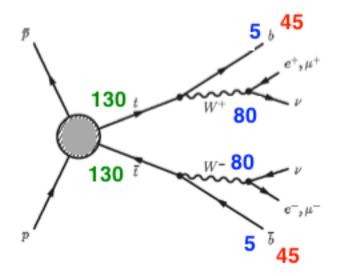


Run 8467	6 Event	12814			z verte	x: -6.17	7 cm
Object	E	E_x	E_y	E_z	E_T	η	ϕ
Electron	81.3	-75.4	-1.1	-30.2	74.5	-0.39	3.16
Muon	30.2	-25.2	10.6	-12.8	27.4	-0.45	2.75
E_T	-	62.0	5.2	-	62.3	_	0.08
Jet 1	93.8	38.0	-83.7	-15.6	91.9	-0.17	5.14
	(95.9)	(38.9)	(-85.6)	(-16.0)	(94.0)		
Jet 2	37.8	13.9	32.3	-11.2	35.2	-0.31	1.17
	(38.8)	(14.2)	(33.1)	(-11.4)	(36.0)		
Jet 3	31.4	-1.6	28.6	11.6	28.7	0.39	1.63
	(32.2)	(-1.6)	(29.3)	(11.9)	(29.4)		

...".

In E8 Physics (viXra 1508.0157) there are, as stated above, three T-quark mass states, so in order to keep the kinematic constraint

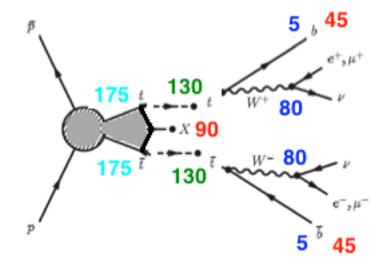
"The masses of the reconstructed t and tbar in the event are equal" the t and tbar must be in the same mass state, which is physically realistic because the t and tbar are created together in the same collider collision event. If the t and tbar are both in the 130 GeV mass state then the decay is simple with 2 jets:



and both jets are highly constrained as being related to the W - b decay process so it is reasonable to expect that the 130 GeV decay events would fall in the narrow width of a single 10 GeV histogram bin.

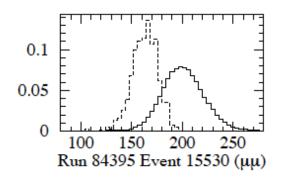
(In these two diagrams I have indicated energies only approximately for t and tbar mass states (cyan and green) and W and b-quark (blue) and jets (red). Actual kinematic data may vary from the idealized numbers on the diagrams, but they should give similar physics results.)

If the t and tbar are both in the 173 GeV mass state (as, for example, in Run 84676 Event 12814 (e mu) described above) the decay has two stages and 3 jets:



First, the 175 GeV t and tbar both decay to the 130 GeV state, emitting a jet. Then, the 130 GeV t and tbar decay by the simple 2-jet process.

The first jet is a process of the Higgs - T-quark condensate system of E8 Physics and is not a W -b decay process so it is not so highly constrained and it is reasonable to expect that the 175 GeV decay events would appear to have a larger (on the order of 40 GeV) width. As to t and tbar being the high T-quark mass state (around 225 GeV) there would be a third stage for decay from 225 GeV to 175 GeV with a fourth jet carrying around 100 GeV of decay energy. In the Varnes thesis there is one dilepton event



Run 8439	95 Event	15530			z vertex	: 5.9 cr	n
Object	E	E_x	E_y	E_z	E_T	η	ϕ
Muon 1	68.6	-63.9	12.7	-21.4	65.1	-0.32	2.94
Muon 2	34.9	-16.0	31.0	1.9	34.9	0.05	2.05
₿ _T	-	71.2	53.2	-	88.9	_	0.64
Jet 1	146.1	32.1	-98.2	-102.4	103.3	-0.88	5.03
	(153.5)	(33.8)	(-103.1)	(-107.6)	(108.5)		
Jet 2	35.1	-8.6	21.4	26.2	23.1	0.97	1.95
	(37.2)	(-9.1)	(22.7)	(27.7)	(24.5)		
Jet 3	47.1	-7.6	-16.8	43.0	18.4	1.58	4.29
	(52.3)	(-8.4)	(-18.6)	(47.8)	(20.5)		

that seems me to represent that third stage of decay from 225 GeV to 175 GeV. Since it is described as a 3-jet event and not a 4-jet event as I would have expected, my guess is that the third and fourth jets of my model were not distinguished by the experiment so that they appeared to be one third jet.

Appendix - Details of Force Strength and Boson Mass Calculations

Here are less approximate more detailed force strength calculations:

The force strength of a given force is

alphaforce = (1 / Mforce^2) (Vol(MISforce)) (Vol(Qforce) / Vol(Dforce)^(1 / mforce))

where:

alphaforce represents the force strength;

Mforce represents the effective mass;

MISforce represents the relevant part of the target Internal Symmetry Space;

Vol(MISforce) stands for volume of MISforce and is sometimes also denoted by Vol(M);

Qforce represents the link from the origin to the relevant target for the gauge boson;

Vol(Qforce) stands for volume of Qforce;

Dforce represents the complex bounded homogeneous domain of which Qforce is the Shilov boundary;

mforce is the dimensionality of Qforce, which is

4 for Gravity and the Color force,

2 for the Weak force (which therefore is considered to have two copies of QW for SpaceTime), 1 for Electromagnetism (which therefore is considered to have four copies of QE for SpaceTime)

Vol(Dforce)^(1 / mforce) stands for a dimensional normalization factor (to reconcile the dimensionality of the Internal Symmetry Space of the target vertex with the dimensionality of the link from the origin to the target vertex).

The Qforce, Hermitian symmetric space, and Dforce manifolds for the four forces are:

Spin(5)	Spin(7) / Spin(5)xU(1)	IV5	4	RP^1xS^4
SU(3)	SU(4) / SU(3)xU(1)	B^6(ball)	4	S^5
SU(2)	Spin(5) / SU(2)xU(1)	IV3	2	RP^1xS^2
U(1)	-	-	1	-

The geometric volumes needed for the calculations are mostly taken from the book Harmonic Analysis of Functions of Several Complex Variables in the Classical Domains (AMS 1963, Moskva 1959, Science Press Peking 1958) by L. K. Hua [unit radius scale].

Force	Μ	Vol(M)
gravity	S^4	8pi^2/3 - S^4 is 4-dimensional
color	CP^2	8pi^2/3 - CP^2 is 4-dimensional
weak	S^2 x S^2	2 x 4pi - S^2 is a 2-dim boundary of 3-dim ball 4-dim S^2 x S^2 = topological boundary of 6-dim 2-polyball Shilov Boundary of 6-dim 2-polyball = S^2 + S^2 = = 2-dim surface frame of 4-dim S^2 x S^
e-maq	T^4	4 x 2pi - S^1 is 1-dim boundary of 2-dim disk

e-mag 1⁴ 4 x 2pi - S¹ is 1-dim boundary of 2-dim disk 4-dim T⁴ = S¹ x S¹ x S¹ x S¹ = topological boundary of 8-dim 4-polydisk Shilov Boundary of 8-dim 4-polydisk = S¹ + S¹ + S¹ + S¹ = = 1-dim wire frame of 4-dim T⁴

Note (thanks to Carlos Castro for noticing this) also that the volume listed for CP2 is unconventional, but physically justified by noting that S4 and CP2 can be seen as having the same physical volume, with the only difference being structure at infinity.

Note that for U(1) electromagnetism, whose photon carries no charge, the factors Vol(Q) and Vol(D) do not apply and are set equal to 1, and from another point of view, the link manifold to the target vertex is trivial for the abelian neutral U(1) photons of Electromagnetism, so we take QE and DE to be equal to unity.

Force	Μ	Vol(M)	Q	Vol(Q)	D	Vol(D)
gravity	S^4	8pi^2/3	RP^1xS^4	8pi^3/3	IV5	pi^5/2^4 5!
color	CP^2	8pi^2/3	S^5	4pi^3	B^6(ball)	pi^3/6
Weak	S^2xS^2	2x4pi	RP^1xS^2	4pi^2	IV3	pi^3/24
e-mag	T^4	4x2pi	-	-	-	-

Note (thanks to Carlos Castro for noticing this) that the volume listed for S5 is for a squashed S5, a Shilov boundary of the complex domain corresponding to the symmetric space $SU(4) / SU(3) \times U(1)$.

Using the above numbers, the results of the calculations are the relative force strengths at the characteristic energy level of the generalized Bohr radius of each force:

Spin(5)	gravity	approx 10^19 GeV	V 1	GGmproton ² approx 5 x 10 ⁻³⁹
SU(3)	color	approx 245 MeV	0.6286	0.6286
SU(2)	weak	approx 100 GeV	0.2535	GWmproton ² approx 1.05 x 10 ⁻⁵
U(1)	e-mag	approx 4 KeV	1/137.03608	1/137.03608

The force strengths are given at the characteristic energy levels of their forces, because the force strengths run with changing energy levels. The effect is particularly pronounced with the color force. The color force strength was calculated using a simple perturbative QCD

renormalization group equation at various energies, with the following results:

Energy Level	Color Force Strength
245 MeV	0.6286
5.3 GeV	0.166
34 GeV	0.121
91 GeV	0.106

Taking other effects, such as Nonperturbative QCD, into account, should give a Color Force Strength of about 0.125 at about 91 GeV

Higgs, W+, W-, Z0:

As with forces strengths, the calculations produce ratios of masses, so that only one mass need be chosen to set the mass scale.

In the CI(1,25) E8 model,

the value of the fundamental mass scale vacuum expectation value $v = \langle PHI \rangle$ of the Higgs scalar field is set to be the sum of the physical masses of the weak bosons, W+, W-, and Z0, whose tree-level masses will then be shown by ratio calculations to be 80.326 GeV, 80.326 GeV, and 91.862 GeV, respectively, and therefore the electron mass will be 0.5110 MeV.

The relationship between the Higgs mass and v is given by the Ginzburg-Landau term from the Mayer Mechanism as (1/4) Tr ([PHI, PHI] - PHI)²

or, i

n the notation of quant-ph/9806009 by Guang-jiong Ni (1/4!) lambda PHI^4 - (1/2) sigma PHI^2 where the Higgs mass M_H = sqrt(2 sigma)

Ni says:

"... the invariant meaning of the constant lambda in the Lagrangian is not the coupling constant, the latter will change after quantization ... The invariant meaning of lambda is nothing but the ratio of two mass scales:

lambda = 3 (M_H / PHI)² which remains unchanged irrespective of the order ...".

Since $\langle PHI \rangle^2 = v^2$, and assuming that lambda = $(\cos(pi/6))^2 = 0.866^2$ (a value consistent with the Higgs-Tquark condensate model of Michio Hashimoto, Masaharu Tanabashi, and Koichi Yamawaki in their paper at hep-ph/0311165) we have

 $M_H^2 / v^2 = (\cos(pi/6))^2 / 3$

In the CI(1,25) E8 model, the fundamental mass scale vacuum expectation value v of the Higgs scalar field is the fundamental mass parameter that is to be set to define all other masses by the mass ratio formulas of the model and v is set to be 252.514 GeV so that

$$M_H = v \cos(pi / 6) / sqrt(1 / 3) = 126.257 \text{ GeV}$$

This is the value of the Low Mass State of the Higgs observed by the LHC.

MIddle and High Mass States come from a Higgs-Tquark Condensate System. The Middle and High Mass States may have been observed by the LHC at 20% of the Low Mass State cross section, and that may be confirmed by the LHC 2015-1016 run. A Non-Condensate Higgs is represented by a Higgs at a point in M4 that is connected to a Higgs representation in CP2 ISS by a line whose length represents the Higgs mass

```
Higgs Higgs in CP2 Internal Symmetry Space
```

and the value of lambda is $1 = 1^2$ so that the Higgs mass would be M_H = v /sqrt(3) = 145.789 GeV

However, in the Cl(1,25) E8 model, the Higgs has structure of a Tquark condensate

```
mass = 145
 ----Tbar
                      Effective Higgs in CP2 Internal Symmetry Space
Т
            /
 /
  /
         /mass = 145
                            | Higgs Effective Mass =
   \
                              = 145 \times \cos(pi/6) = 145 \times 0.866 = 126
    \setminus
        /
     \setminus | /
   Higgs
                        Higgs in M4 spacetime
```

in which the Higgs at a point in M4 is connected to a T and Tbar in CP2 ISS so that the vertices of the Higgs-T-Tbar system are connected by lines forming an equilateral triangle composed of 2 right triangles (one from the CP2 origin to the T and to the M4 Higgs and another from the CP2 origin to the Tbar and to the M4 Higgs). In the T-quark condensate picture lambda = 1^2 = lambda(T) + lambda(H) = (sin(pi / 6))² + (cos(pi / 6))² and lambda(H) = (cos(pi / 6))²

Therefore the Effective Higgs mass observed by LHC is:

Higgs Mass = 145.789 x cos(pi/6) = 126.257 GeV.

To get W-boson masses, denote the 3 SU(2) high-energy weak bosons (massless at energies higher than the electroweak unification) by W+, W-, and W0, corresponding to the massive physical weak bosons W+, W-, and Z0.

The triplet { W+, W-, W0 } couples directly with the T - Tbar quark-antiquark pair, so that the total mass of the triplet { W+, W-, W0 } at the electroweak unification is equal to the total mass of a T - Tbar pair, 259.031 GeV.

The triplet { W+, W-, Z0 } couples directly with the Higgs scalar, which carries the Higgs mechanism by which the W0 becomes the physical Z0, so that the total mass of the triplet { W+, W-, Z0 } is equal to the vacuum expectation value v of the Higgs scalar field, v = 252.514 GeV.

What are individual masses of members of the triplet { W+, W-, Z0 } ?

First, look at the triplet { W+, W-, W0 } which can be represented by the 3-sphere S^3. The Hopf fibration of S^3 as

S^1 --> S^3 --> S^2

gives a decomposition of the W bosons into the neutral W0 corresponding to S^{1} and the charged pair W+ and W- corresponding to S^{2} .

The mass ratio of the sum of the masses of W+ and W- to the mass of W0 should be the volume ratio of the S^2 in S^3 to the S^1 in S3. The unit sphere S^3 in R^4 is normalized by 1 / 2. The unit sphere S^2 in R^3 is normalized by 1 / sqrt(3). The unit sphere S^1 in R^2 is normalized by 1 / sqrt(2). The ratio of the sum of the W+ and W- masses to the W0 mass should then be $(2 / \text{sqrt3}) V(S^2) / (2 / \text{sqrt2}) V(S^1) = 1.632993$

Since the total mass of the triplet { W+, W-, W0 } is 259.031 GeV, the total mass of a T - Tbar pair, and the charged weak bosons have equal mass, we have

M_W+ = M_W- = 80.326 GeV and M_W0 = 98.379 GeV.

The charged W+/- neutrino-electron interchange must be symmetric with the electron-neutrino interchange, so that the tree-level absence of right-handed neutrino particles requires that

the charged W+/- SU(2) weak bosons act only on left-handed electrons.

Each gauge boson must act consistently on the entire Dirac fermion particle sector, so that the

charged W+/- SU(2) weak bosons act only on left-handed fermion particles of all types.

The neutral W0 weak boson does not interchange Weyl neutrinos with Dirac fermions, and so is not restricted to left-handed fermions, but also has a component that acts on both types of fermions, both left-handed and right-handed, conserving parity.

However, the neutral W0 weak bosons are related to the charged W+/- weak bosons by custodial SU(2) symmetry, so that the left-handed component of the neutral W0 must be equal to the left-handed (entire) component of the charged W+/-.

Since the mass of the W0 is greater than the mass of the W+/-, there remains for the W0 a component acting on both types of fermions.

Therefore the full W0 neutral weak boson interaction is proportional to $(M_W+/-^2 / M_W0^2)$ acting on left-handed fermions and $(1 - (M_W+/-^2 / M_W0^2))$ acting on both types of fermions.

If $(1 - (M_W+/-2 / M_W0^2))$ is defined to be sin(theta_w)^2 and denoted by K, and if the strength of the W+/- charged weak force (and of the custodial SU(2) symmetry) is denoted by T, then the W0 neutral weak interaction can be written as W0L = T + K and W0LR = K.

Since the W0 acts as W0L with respect to the parity violating SU(2) weak force and as W0LR with respect to the parity conserving U(1) electromagnetic force, the W0 mass mW0 has two components:

the parity violating SU(2) part mW0L that is equal to M_W+/-

and the parity conserving part M_W0LR that acts like a heavy photon.

As $M_W0 = 98.379 \text{ GeV} = M_W0L + M_W0LR$, and as $M_W0L = M_W+/- = 80.326 \text{ GeV}$, we have $M_W0LR = 18.053 \text{ GeV}$.

Denote by *alphaE = *e^2 the force strength of the weak parity conserving U(1) electromagnetic type force that acts through the U(1) subgroup of SU(2).

The electromagnetic force strength alphaE = $e^2 = 1 / 137.03608$ was calculated above using the volume V(S¹) of an S¹ in R², normalized by 1 / sqrt(2).

The *alphaE force is part of the SU(2) weak force whose strength alphaW = w^2 was calculated above using the volume V(S^2) of an S^2 \subset R^3, normalized by 1 / sqrt(3).

Also, the electromagnetic force strength $alphaE = e^2$ was calculated above using a 4-dimensional spacetime with global structure of the 4-torus T^4 made up of four S^1 1-spheres,

while the SU(2) weak force strength $alphaW = w^2$ was calculated above using two 2-spheres S² x S²,

each of which contains one 1-sphere of the *alphaE force.

Therefore

*alphaE = alphaE (sqrt(2) / sqrt(3))(2 / 4) = alphaE / sqrt(6), *e = e / (4th root of 6) = e / 1.565 ,

and

the mass mW0LR must be reduced to an effective value M_W0LReff = M_W0LR / 1.565 = 18.053/1.565 = 11.536 GeV for the *alphaE force to act like an electromagnetic force in the E8 model: *e M_W0LR = e (1/5.65) M_W0LR = e M_Z0, where the physical effective neutral weak boson is denoted by Z0. Therefore, the correct Cl(1,25) E8 model values for weak boson masses and the Weinberg angle theta_w are:

M_W+ = M_W- = 80.326 GeV;

M_Z0 = 80.326 + 11.536 = 91.862 GeV;

Sin(theta_w)^2 = 1 - $(M_W + / / M_Z 0)^2 = 1 - (6452.2663 / 8438.6270) = 0.235$.

Radiative corrections are not taken into account here, and may change these tree-level values somewhat.

Appendix - Details of Fermion Mass Calculations

In the Cl(1,25) E8 model, the first generation spinor fermions are seen as +half-spinor and -half-spinor spaces of Cl(1,7) = Cl(8). Due to Triality, Spin(8) can act on those 8-dimensional half-spinor spaces similarly to the way it acts on 8-dimensional vector spacetime.

Take the spinor fermion volume to be the Shilov boundary corresponding to the same symmetric space on which Spin(8) acts as a local gauge group that is used to construct 8-dimensional vector spacetime: the symmetric space Spin(10) / Spin(8)xU(1) corresponding to a bounded domain of type IV8 whose Shilov boundary is RP^1 x S^7

Since all first generation fermions see the spacetime over which the integral is taken in the same way (unlike what happens for the force strength calculation), the only geometric volume factor relevant for calculating first generation fermion mass ratios is in the spinor fermion volume term.

Cl(1,25) E8 model fermions correspond to Schwinger Source Kerr-Newman Black Holes,

so the quark mass in the CI(1,25) E8 model is a constituent mass.

Fermion masses are calculated as a product of four factors:

V(Qfermion) x N(Graviton) x N(octonion) x Sym

V(Qfermion) is the volume of the part of the half-spinor fermion particle manifold S^7 x RP^1 related to the fermion particle by photon, weak boson, or gluon interactions.

N(Graviton) is the number of types of Spin(0,5) graviton related to the fermion. The 10 gravitons correspond to the 10 infinitesimal generators of Spin(0,5) = Sp(2). 2 of them are in the Cartan subalgebra.

6 of them carry color charge, and therefore correspond to quarks.

The remaining 2 carry no color charge, but may carry electric charge and so may be considered as corresponding to electrons.

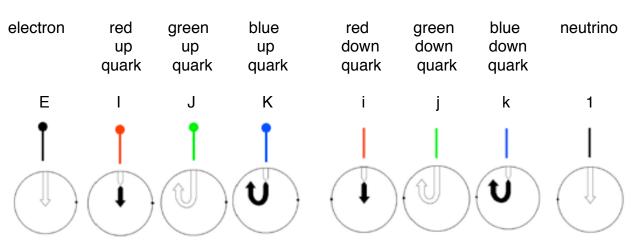
One graviton takes the electron into itself, and the other can only take the firstgeneration electron into the massless electron neutrino. Therefore only one graviton should correspond to the mass of the first-generation electron. The graviton number ratio of the down quark to the first-generation electron is therefore 6/1 = 6.

N(octonion) is an octonion number factor relating up-type quark masses to down-type quark masses in each generation.

Sym is an internal symmetry factor, relating 2nd and 3rd generation massive leptons to first generation fermions. It is not used in first-generation calculations.

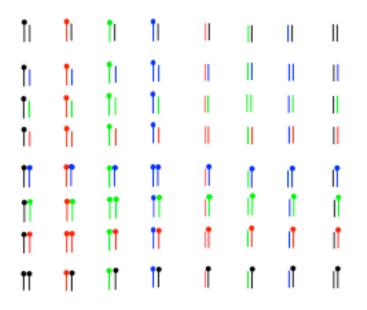
3 Generation Fermion Combinatorics

First Generation (8)



(geometric representation of Octonions is from arXiv 1010.2979)

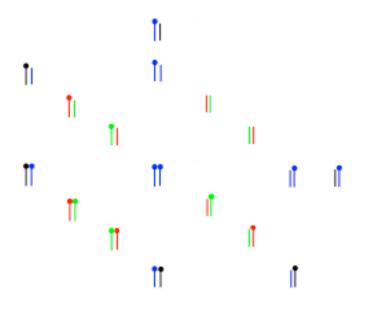
Second Generation (64)



Mu Neutrino (1) Rule: a Pair belongs to the Mu Neutrino if: All elements are Colorless (black) and all elements are Associative (that is, is 1 which is the only Colorless Associative element). Muon (3) Rule: a Pair belongs to the Muon if: All elements are Colorless (black) and at least one element is NonAssociative (that is, is E which is the only Colorless NonAssociative element).

Blue Strange Quark **(3)** Rule: a Pair belongs to the Blue Strange Quark if: There is at least one Blue element and the other element is Blue or Colorless (black) and all elements are Associative (that is, is either 1 or i or j or k).

Blue Charm Quark (17) Rules: a Pair belongs to the Blue Charm Quark if: 1 - There is at least one Blue element and the other element is Blue or Colorless (black) and at least one element is NonAssociative (that is, is either E or I or J or K) 2 - There is one Red element and one Green element (Red x Green = Blue).



(Red and Green Strange and Charm Quarks follow similar rules)

Third Generation (512)

Tau Neutrino (1) Rule: a Triple belongs to the Tau Neutrino if: All elements are Colorless (black) and all elements are Associative (that is, is 1 which is the only Colorless Associative element)

Tauon (7) Rule: a Triple belongs to the Tauon if: All elements are Colorless (black) and at least one element is NonAssociative (that is, is E which is the only Colorless NonAssociative element) Blue Beauty Quark (7)

Rule: a Triple belongs to the Blue Beauty Quark if:

There is at least one Blue element and all other elements are Blue or Colorless (black) and all elements are Associative (that is, is either 1 or i or j or k).

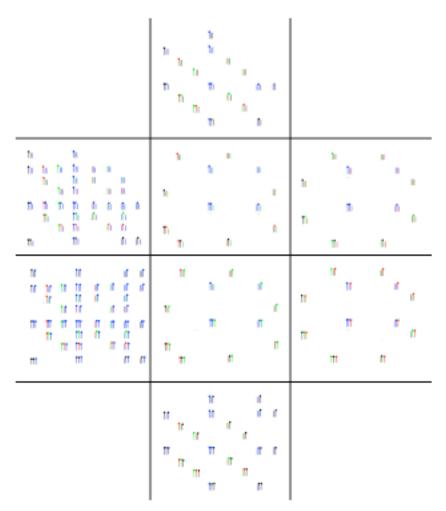
Blue Truth Quark (161)

Rules: a Triple belongs to the Blue Truth Quark if:

1 - There is at least one Blue element and all other elements are Blue or Colorless (black)

and at least one element is NonAssociative (that is, is either E or I or J or K) 2 - There is one Red element and one Green element and the other element is Colorless (Red x Green = Blue)

3 - The Triple has one element each that is Red, Green, or Blue, in which case the color of the Third element (for Third Generation) is determinative and must be Blue.



(Red and Green Beauty and Truth Quarks follow similar rules)

The first generation down quark constituent mass : electron mass ratio is:

The electron, E, can only be taken into the tree-level-massless neutrino, 1, by photon, weak boson, and gluon interactions.

The electron and neutrino, or their antiparticles, cannot be combined to produce any of the massive up or down quarks.

The neutrino, being massless at tree level, does not add anything to the mass formula for the electron.

Since the electron cannot be related to any other massive Dirac fermion, its volume V(Qelectron) is taken to be 1.

Next consider a red down quark i.

By gluon interactions, i can be taken into j and k, the blue and green down quarks. By also using weak boson interactions,

it can also be taken into I, J, and K, the red, blue, and green up quarks.

Given the up and down quarks, pions can be formed from quark-antiquark pairs, and the pions can decay to produce electrons and neutrinos.

Therefore the red down quark (similarly, any down quark)

is related to all parts of S^7 x RP^1,

the compact manifold corresponding to { 1, i, j, k, E, I, J, K }

and therefore

a down quark should have

a spinor manifold volume factor V(Qdown quark) of the volume of S^7 x RP^1.

The ratio of the down quark spinor manifold volume factor

to the electron spinor manifold volume factor is

 $V(Qdown quark) / V(Qelectron) = V(S^7x RP^1)/1 = pi^5 / 3.$

Since the first generation graviton factor is 6, $md (max - 6) V(SAT \times DBA1) = 2 piA5$

md / me = 6 V(S^7 x RP^1) = 2 pi^5 = 612.03937

As the up quarks correspond to I, J, and K, which are the octonion transforms under E of i, j, and k of the down quarks, the up quarks and down quarks have the same constituent mass

mu = md.

Antiparticles have the same mass as the corresponding particles. Since the model only gives ratios of masses, the mass scale is fixed so that the electron mass me = 0.5110 MeV.

Then, the constituent mass of the down quark is md = 312.75 MeV, and the constituent mass for the up quark is mu = 312.75 MeV.

These results when added up give a total mass of first generation fermion particles: Sigmaf1 = 1.877 GeV As the proton mass is taken to be the sum of the constituent masses of its constituent quarks

mproton = mu + mu + md = 938.25 MeV which is close to the experimental value of 938.27 MeV.

The third generation fermion particles correspond to triples of octonions. There are $8^3 = 512$ such triples.

The triple { 1,1,1 } corresponds to the tau-neutrino.

The other 7 triples involving only 1 and E correspond to the tauon:

{ E, E, E }
{ E, E, 1 }
{ E, 1, E }
{ 1, E, E }
{ 1, 1, E }
{ 1, E, 1 }
{ 1, E, 1 }

The symmetry of the 7 tauon triples is the same as the symmetry of the first generation tree-level-massive fermions, 3 down, quarks, the 3 up quarks, and the electron, so by the Sym factor the tauon mass should be the same as the sum of the masses of the first generation massive fermion particles.

Therefore the tauon mass is calculated at tree level as 1.877 GeV.

The calculated tauon mass of 1.88 GeV is a sum of first generation fermion masses, all of which are valid at the energy level of about 1 GeV.

However, as the tauon mass is about 2 GeV, the effective tauon mass should be renormalized from the energy level of 1 GeV at which the mass is 1.88 GeV to the energy level of 2 GeV. Such a renormalization should reduce the mass.

If the renormalization reduction were about 5 percent, the effective tauon mass at 2 GeV would be about 1.78 GeV. The 1996 Particle Data Group Review of Particle Physics gives a tauon mass of 1.777 GeV.

All triples corresponding to the tau and the tau-neutrino are colorless.

The beauty quark corresponds to 21 triples. They are triples of the same form as the 7 tauon triples involving 1 and E, but for 1 and I, 1 and J, and 1 and K, which correspond to the red, green, and blue beauty quarks, respectively.

The seven red beauty quark triples correspond to the seven tauon triples, except that the beauty quark interacts with 6 Spin(0,5) gravitons while the tauon interacts with only two.

The red beauty quark constituent mass should be the tauon mass times the third generation graviton factor 6/2 = 3, so the red beauty quark mass is mb = 5.63111 GeV.

The blue and green beauty quarks are similarly determined to also be 5.63111 GeV.

The calculated beauty quark mass of 5.63 GeV is a consitituent mass, that is, it corresponds to the conventional pole mass plus 312.8 MeV. Therefore, the calculated beauty quark mass of 5.63 GeV corresponds to a conventional pole mass of 5.32 GeV.

The 1996 Particle Data Group Review of Particle Physics gives a lattice gauge theory beauty quark pole mass as 5.0 GeV.

The pole mass can be converted to an MSbar mass if the color force strength constant alpha_s is known. The conventional value of alpha_s at about 5 GeV is about 0.22.

Using alpha_s (5 GeV) = 0.22, a pole mass of 5.0 GeV gives an MSbar 1-loop beauty quark mass of 4.6 GeV, and an MSbar 1,2-loop beauty quark mass of 4.3, evaluated at about 5 GeV.

If the MSbar mass is run from 5 GeV up to 90 GeV, the MSbar mass decreases by about 1.3 GeV, giving an expected MSbar mass of about 3.0 GeV at 90 GeV.

DELPHI at LEP has observed the Beauty Quark and found a 90 GeV MSbar beauty quark mass of about 2.67 GeV, with error bars +/- 0.25 (stat) +/- 0.34 (frag) +/- 0.27 (theo). The theoretical model calculated Beauty Quark mass of 5.63 GeV corresponds to a pole mass of 5.32 GeV, which is somewhat higher than the conventional value of 5.0 GeV.

However, the theoretical model calculated value of the color force strength constant alpha_s at about 5 GeV is about 0.166, while the conventional value of the color force strength constant alpha_s at about 5 GeV is about 0.216, and the theoretical model calculated value of the color force strength constant alpha_s at about 90 GeV is about 0.106, while the conventional value of the color force strength constant alpha_s at about 90 GeV is about 0.118.

The theoretical model calculations gives a Beauty Quark pole mass (5.3 GeV) that is about 6 percent higher than the conventional Beauty Quark pole mass (5.0 GeV), and a color force strength alpha_s at 5 GeV (0.166) such that 1 + alpha_s = 1.166 is about 4 percent lower than the conventional value of 1 + alpha_s = 1.216 at 5 GeV.

Triples of the type { 1, I, J } , { I, J, K }, etc., do not correspond to the beauty quark, but to the truth quark. The truth quark corresponds to those 512 - 1 - 7 - 21 = 483 triples, so the constituent mass of the red truth quark is 161 / 7 = 23 times the red beauty quark mass, and the red T-quark mass is mt = 129.5155 GeV

The blue and green truth quarks are similarly determined to also be 129.5155 GeV.

This is the value of the Low Mass State of the Truth calculated in the Cl(1,25) E8 model. The Middle Mass State of the Truth Quark has been observed by Fermilab since 1994. The Low and High Mass States of the Truth Quark have, in my opinion, also been observed by Fermilab (see Chapter 17 of this paper) but the Fermilab and CERN establishments disagree.

All other masses than the electron mass (which is the basis of the assumption of the value of the Higgs scalar field vacuum expectation value v = 252.514 GeV), including the Higgs scalar mass and Truth quark mass, are calculated (not assumed) masses in the Cl(1,25) E8 model. These results when added up give a total mass of third generation fermion particles:

Sigmaf3 = 1,629 GeV

The second generation fermion particles correspond to pairs of octonions. There are $8^2 = 64$ such pairs.

The pair { 1,1 } corresponds to the mu-neutrino.

The pairs { 1, E }, { E, 1 }, and { E, E } correspond to the muon.

For the Sym factor, compare the symmetries of the muon pairs to the symmetries of the first generation fermion particles: The pair { E, E } should correspond to the E electron. The other two muon pairs have a symmetry group S2, which is 1/3 the size of the color symmetry group S3 which gives the up and down quarks their mass of 312.75 MeV.

Therefore the mass of the muon should be the sum of the { E, E } electron mass and the { 1, E }, { E, 1 } symmetry mass, which is 1/3 of the up or down quark mass. Therefore, mmu = 104.76 MeV .

According to the 1998 Review of Particle Physics of the Particle Data Group, the experimental muon mass is about 105.66 MeV which may be consistent with radiative corrections for the calculated tree-level mmu = 104.76 MeV as Bailin and Love, in "Introduction to Gauge Field Theory", IOP (rev ed 1993), say: "... considering the order alpha radiative corrections to muon decay ... Numerical details are contained in Sirlin ... 1980 Phys. Rev. D 22 971 ... who concludes that the order alpha corrections have the effect of increasing the decay rate about 7% compared with the tree graph prediction ...". Since the decay rate is proportional to mmu^5 the corresponding effective increase in muon mass would be about 1.36%, which would bring 104.8 MeV up to about 106.2 MeV.

All pairs corresponding to the muon and the mu-neutrino are colorless.

The red, blue and green strange quark each corresponds to the 3 pairs involving 1 and i, j, or k.

The red strange quark is defined as the three pairs { 1, i }, { i, 1 }, { i, i } because i is the red down quark. Its mass should be the sum of two parts: the { i, i } red down quark mass, 312.75 MeV, and the product of the symmetry part of the muon mass, 104.25 MeV, times the graviton factor.

Unlike the first generation situation, massive second and third generation leptons can be taken, by both of the colorless gravitons that may carry electric charge, into massive particles.

Therefore the graviton factor for the second and third generations is 6/2 = 3.

So the symmetry part of the muon mass times the graviton factor 3 is 312.75 MeV, and the red strange quark constituent mass is ms = 312.75 MeV + 312.75 MeV = 625.5 MeV

The blue strange quarks correspond to the three pairs involving j, the green strange quarks correspond to the three pairs involving k, and their masses are similarly determined to also be 625.5 MeV. The charm guark corresponds to the remaining 64 - 1 - 3 - 9 = 51 pairs.

Therefore, the mass of the red charm quark should be the sum of two parts: the { i, i }, red up quark mass, 312.75 MeV; and the product of the symmetry part of the strange quark mass, 312.75 MeV, and the charm to strange octonion number factor 51 / 9, which product is 1,772.25 MeV.

Therefore the red charm quark constituent mass is mc = 312.75 MeV + 1,772.25 MeV = 2.085 GeV

The blue and green charm quarks are similarly determined to also be 2.085 GeV.

The calculated Charm Quark mass of 2.09 GeV is a consitituent mass, that is, it corresponds to the conventional pole mass plus 312.8 MeV.

Therefore, the calculated Charm Quark mass of 2.09 GeV corresponds to a conventional pole mass of 1.78 GeV.

The 1996 Particle Data Group Review of Particle Physics gives a range for the Charm Quark pole mass from 1.2 to 1.9 GeV.

The pole mass can be converted to an MSbar mass if the color force strength constant alpha_s is known.

The conventional value of alpha_s at about 2 GeV is about 0.39,

which is somewhat lower than the theoretical model value.

Using alpha_s (2 GeV) = 0.39, a pole mass of 1.9 GeV

gives an MSbar 1-loop mass of 1.6 GeV, evaluated at about 2 GeV.

These results when added up give a total mass of second generation fermion particles:

Sigmaf2 = 32.9 GeV

Appendix - Massless Realm Beyond EW Symmetry Breaking

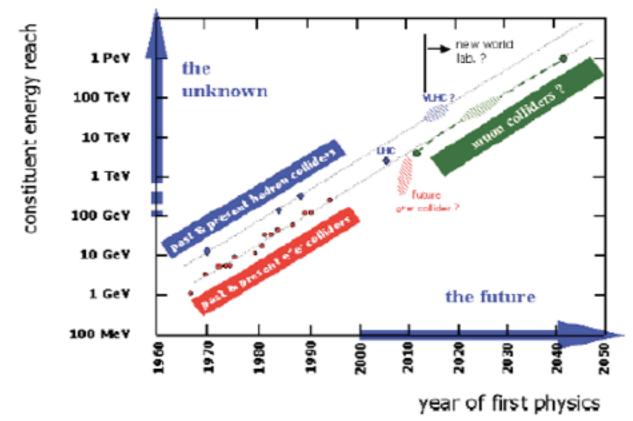
At Temperature / Energy above 3×10^{15} K = 300 GeV: the Higgs mechanism is not in effect so there is full ElectroWeak Symmetry and no particles have any mass from the Higgs. Questions arise:

1 - Can we build a collider that will explore the Massless Phase ?

2 - How did our Universe evolve in that early Massless Phase of its first 10⁽⁻¹¹⁾ seconds or so ?

3 - What do physical phenomena look like in the Massless Phase ?

1 - Can we build a collider that will explore the Massless Phase ? Yes: In hep-ex00050008 Bruce King has a chart and he gives a cost estimate of



about \$12 billion for a 1000 TeV (1 PeV) Linear Muon Collider with tunnel length about 1000 km. Marc Sher has noted that by now (late 2012 / early 2013) the cost estimate of \$12 billion should be doubled or more. My view is that a cost of \$100 billion is easily affordable by the USA as it is far less than the Trillions given annually since 2008 by the USA Fed/Treasury to Big Banks as Quantitative Easing to support their Derivatives Casino. Science will advance AND non-Bankster people will get paying jobs.

2 - How did our Universe evolve in that early Massless Phase of its first 10⁽⁻¹¹⁾ seconds or so ?

In the context of E8 Physics our Universe began as a Quantum Fluctuation from a Parent Universe whereby our Universe initially had Planck Scale Temperature / Energy 10^32 K = 1.22 x 10^19 GeV.

Its physics was then described by a Lagrangian with:

Gauge Boson term of 28-dimensional adjoint Spin(8) that eventually produces the 12-dim SU(3)xSU(2)xU(1) Standard Model along with 16-dim U(2,2) Conformal Gravity Ghosts.

Fermion term of 8-dimensional half-spinor Spin(8) corresponding to first-generation fermion particles and antipartices (electron, RGB Up quarks; neutrino, RGB down quarks);

Base Manifold of 8-dimensional Octonionic Spacetime.

With respect to 8-dimensional Spacetime

the dimensionality of the Gauge Boson term is $28 \times 1 = 28$ and

the dimensionality of the Fermion term is $8 \times 7/2 = 28$

(see Weinberg's 1986 Dirac Memorial Lecture at page 88 and note that 7/2 + 7/2 + 1 = 8) so

the E8 Physics Lagranigian is clearly Ultraviolet Finite at the Planck Scale due to Triality-based cancellations, an effective Subtle Supersymmetry.

Since the lower energy forms of E8 Physics are derived from the Planck Scale Lagrangian, they also benefit from the cancellations.

As Our Universe began to cool down below the Planck Scale Inflationary Expansion started due to Octonionic Quantum Non-Unitarity (see Adler's book "Quaternionic Quantum Mechanics ..." at pages 50-52 and 561).

Paola Zizzi describes the Octonionic Inflationary Era in terms of Clifford Algebras in gr-qc/0007006 and related papers. In short, the 64 doublings of Zizzi Inflation produce about 10^77 fermion particles.

At the End of Inflation Our Universe had Temperature / Energy 10^{27} K = 10^{14} GeV

A consequence of the end of Octonionic Inflation was the freezing out of a preferred Quaternionic Subspace so that 8-dim Octonionic Spacetime was converted into (4+4)-dim Kaluza-Klein spacetime M4 x CP2

where M4 is Minkowski Physical 4-dim spacetime and CP2 = SU(3) / SU(2)xU(1) is a Batakis 4-dim Internal Symmetry Space.

The geometry of that splitting of spacetime produces a Higgs mechanism. (see Meinhard Mayer and A. Trautman in "A Brief Introduction to the Geometry of Gauge Fields" and "The Geometry of Symmetry Breaking in Gauge Theories", Acta Physica Austriaca, Suppl. XXIII (1981))

Since each of the 10^77 fermions had energy of 10^14 GeV collisions among them would for each of the 10^77 fermions produce jets containing about 10^12 particles of energy 100 GeV or so so that the total number of such particles is about 10^89.

According to Weinberg's book "Cosmology":

"... above 10^13 K, nucleons would not yet have formed from their three constituent quarks, and there would have been roughly as many quarkantiquark pairs in thermal equilibrium as photons ...

before annihilation there must have been a slight excess ... of quarks over antiquarks, so that some quarks would survive to form nucleons when all the antiquarks had annihilated with quarks. There was also a slight excess of electrons over positrons, to maintain charge neutrality of the universe ...".

Therefore,

in the interval between the End of Inflation and ElectroWeak Symmetry Breaking most of the quarks in 10⁸⁹ fermions formed quark-antiquark pairs that produced as a condensate the Higgs that is needed for Mayer-Higgs. The quark-antiquark condensate Higgs then Breaks ElectroWeak Symmety at Temperature / Energy 3 x 10¹⁵ K = 300 GeV and gives mass to particles and at age 10⁻⁽¹¹⁾ seconds

ends the Massless Phase of the history of Our Universe.

3 - What do physical phenomena look like in the Massless Phase ?

The Weak Force Strength is $0.2535 \times (1 / MW^2) = 1.05 \times 10^{-5}$ where MW is a Weak Boson Mass factor that goes away in the Massless Realm where the Weak Force becomes a strong 0.25345.

As to Kobayashi-Maskawa Weak Force mixing in the Massless Realm, Kea (Marni Sheppeard) proposed that in the Massless Realm the mixing matrix might be democratic which to me means that in the Massless Realm you might say that there is just a democratic mixing matrix of the form 1/3 x

111

111

111

with no complex terms and no CP violation in the Massless Realm.

With no mass terms, the structure of particle interactions would be based on the Wave Picture instead of the Particle Picture. Instead of a particle with mass moving slower than light the picture is a massless particle moving at light speed with its energy defined by its frequency.

In that picture, for example:

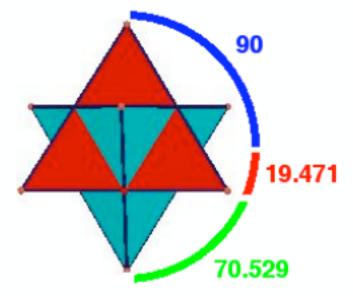
a Muon is distinguishable from an electron by higher frequency due to 2-fold 4+4 path of second generation fermions instead of simple 4 path of first generation fermions.

Quark wave paths have S7 x RP1 structure whose greater complexity produces higher frequency than Lepton wave paths.

Bound structures (Hadrons, Mesons, Nuclei, Atoms, etc) are based on standing wave frequencies instead of masses of particles, nuclei, etc.

Appendix - Kobayashi-Maskawa Parameters

In E8 Physics the KM Unitarity Triangle angles can be seen on the Stella Octangula



The Kobayashi-Maskawa parameters are determined in terms of the sum of the masses of the 30 first-generation fermion particles and antiparticles, denoted by

and the similar sums for second-generation and third-generation fermions, denoted by

Smf2 = 32.94504 GeV and Smf3 = 1,629.2675 GeV.

The resulting KM matrix is:

d		S	b
u	0.975	0.222 0.00249	-0.00388i
С	-0.222 -0.000161i	0.974 -0.0000365i	0.0423
t	0.00698 -0.00378i	-0.0418 -0.00086i	0.999

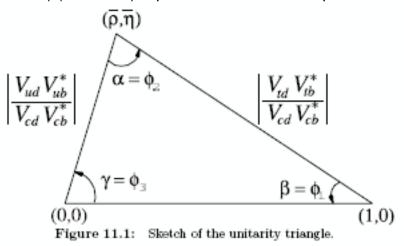
Below the energy level of ElectroWeak Symmetry Breaking the Higgs mechanism gives mass to particles.

According to a Review on the Kobayashi-Maskawa mixing matrix by Ceccucci, Ligeti, and Sakai in the 2010 Review of Particle Physics (note that I have changed their terminology of CKM matrix to the KM terminology that I prefer because I feel that it was Kobayashi and Maskawa, not Cabibbo, who saw that 3x3 was the proper matrix structure): "... the charged-current W± interactions couple to the ... quarks with couplings given by ...

Vud	Vus	Vub
Vcd	Vcs	Vcb
Vtd	Vts	Vtb

This Kobayashi-Maskawa (KM) matrix is a 3x3 unitary matrix. It can be parameterized by three mixing angles and the CP-violating KM phase ... The most commonly used unitarity triangle arises from Vud Vub* + Vcd Vcb* + Vtd Vtb* = 0, by dividing each side by the best-known one, Vcd Vcb*

 $\rho + i\eta = -(Vud Vub_*)/(Vcd Vcb_*)$ is phase-convention- independent ...



... sin $2\beta = 0.673 \pm 0.023$... $\alpha = 89.0 + 4.4 - 4.2$ degrees ... $\gamma = 73 + 22 - 25$ degrees ... The sum of the three angles of the unitarity triangle, $\alpha + \beta + \gamma = (183 + 22 - 25)$ degrees, is ... consistent with the SM expectation. ...

The area... of ...[the]... triangle...[is]... half of the Jarlskog invariant, J, which is a phase-convention-independent measure of CP violation, defined by Im Vij Vkl Vil* Vkj* = $J SUM(m,n) \epsilon_{ikm} \epsilon_{jln}$

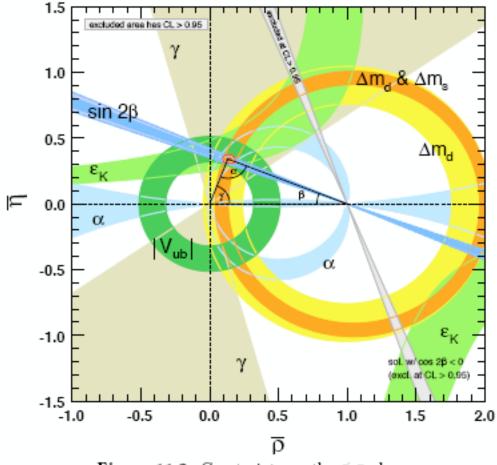


Figure 11.2: Constraints on the $\bar{\rho}, \eta$ plane. The shaded areas have 95% CL.

The fit results for the magnitudes of all nine KM elements are ...

0.97428 ± 0.00015	0.2253 ± 0.0007	0.00347 +0.00016 -0.00012		
0.2252 ± 0.0007	0.97345 +0.00015 - 0.00016	0.0410 +0.0011 – 0.0007		
0.00862 +0.00026 -0.00020	0.0403 +0.0011-0.0007	0.999152 +0.000030-0.000045		
and the Jarlskog invariant is $J = (2.91 + 0.19 - 0.11) \times 10 - 5$ ".				

Above the energy level of ElectroWeak Symmetry Breaking particles are massless.

Kea (Marni Sheppeard) proposed that in the Massless Realm the mixing matrix might be democratic. In Z. Phys. C - Particles and Fields 45, 39-41 (1989) Koide said: "... the mass matrix ... MD ... of the type ... 1/3 x m x

1 1 1 1 1 1 1 1 1

... has name... "democratic" family mixing ... the ... democratic ... mass matrix can be diagonalized by the transformation matrix A ...

1/sqrt(2) 1/sqrt(6) 1/sqrt(3)		1/sqrt(6)	-2/sqrt(6)
as A MD At =			
0 0 0	0 0 0	0 0 m	

Up in the Massless Realm you might just say that there is no mass matrix, just a democratic mixing matrix of the form 1/3 x

1 1 1 1 1 1 1 1 1

with no complex stuff and no CP violation in the Massless Realm.

When go down to our Massive Realm by ElectroWeak Symmetry Breaking then you might as a first approximation use m = 1so that all the mass first goes to the third generation as

0 0 0 0 0 0 0 0 1

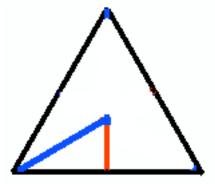
which is physically like the Higgs being a T-Tbar quark condensate.

Consider a 3-dim Euclidean space of generations:

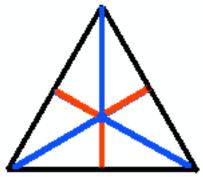
The case of mass only going to one generation can be represented as a line or 1-dimensional simplex

in which the blue mass-line covers the entire black simplex line.

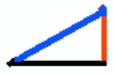
If mass only goes to one other generation that can be represented by a red line extending to a second dimension forming a small blue-red-black triangle



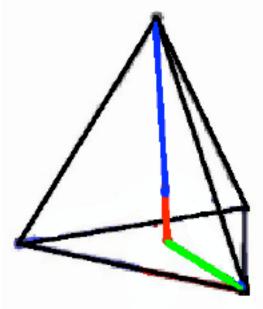
that can be extended by reflection to form six small triangles making up a large triangle



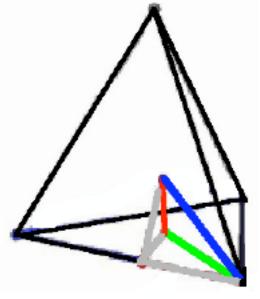
Each of the six component triangles has 30-60-90 angle structure:



If mass goes on further to all three generations that can be represented by a green line extending to a third dimension



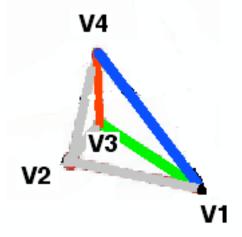
If you move the blue line from the top vertex to join the green vertex



you get a small blue-red-green-gray-gray-gray tetrahedron that can be extended by reflection to form 24 small tetrahedra making up a large tetrahedron.

Reflection among the 24 small tetrahedra corresponds to the 12+12 = 24 elements of the Binary Tetrahedral Group.

The basic blue-red-green triangle of the basic small tetrahedron



has the angle structure of the K-M Unitary Triangle.

Using data from R. W. Gray's "Encyclopedia Polyhedra: A Quantum Module" with lengths

V1.V2 = (1/2) EL = Half of the regular Tetrahedron's edge length. V1.V3 = (1 / sqrt(3)) EL ≈ 0.577 350 269 EL V1.V4 = 3 / (2 sqrt(6)) EL ≈ 0.612 372 436 EL V2.V3 = 1 / (2 sqrt(3)) EL ≈ 0.288 675 135 EL V2.V4 = 1 / (2 sqrt(2)) EL ≈ 0.353 553 391 EL V3.V4 = 1 / (2 sqrt(6)) EL ≈ 0.204 124 145 EL

the Unitarity Triangle angles are:

 β = V3.V1.V4 = arccos(2 sqrt(2) / 3) \approx 19.471 220 634 degrees so sin 2 β = 0.6285

 $\alpha = V1.V3.V4 = 90$ degrees

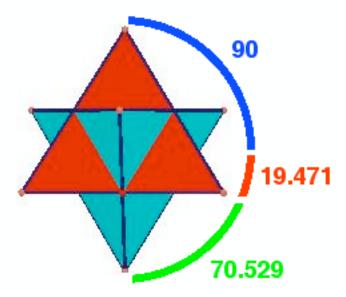
 $\gamma = V1.V4.V3 = \arcsin(2 \text{ sqrt}(2) / 3) \approx 70.528 779 366 \text{ degrees}$

which is substantially consistent with the 2010 Review of Particle Properties

sin $2\beta = 0.673 \pm 0.023$ so $\beta = 21.1495$ degrees $\alpha = 89.0 + 4.4 - 4.2$ degrees $\gamma = 73 + 22 - 25$ degrees

and so also consistent with the Standard Model expectation.

The constructed Unitarity Triangle angles can be seen on the Stella Octangula configuration of two dual tetrahedra (image from gauss.math.nthu.edu.tw):



In the CI(1,25) E8 model the Kobayashi-Maskawa parameters are determined in terms of

the sum of the masses of the 30 first-generation fermion particles and antiparticles, denoted by

Smf1 = 7.508 GeV,

and the similar sums for second-generation and third-generation fermions, denoted by Smf2 = 32.94504 GeV and Smf3 = 1,629.2675 GeV.

The reason for using sums of all fermion masses (rather than sums of quark masses only) is that all fermions are in the same spinor representation of Spin(8), and the Spin(8) representations are considered to be fundamental.

The following formulas use the above masses to calculate Kobayashi-Maskawa parameters:

phase angle d13 = gamma = 70.529 degrees

 $sin(theta12) = s12 = [me+3md+3mu]/sqrt([me^2+3md^2+3mu^2]+ + [mmu^2+3ms^2+3mc^2]) = 0.222198$

 $sin(theta13) = s13 = [me+3md+3mu]/sqrt([me^2+3md^2+3mu^2]+ + [mtau^2+3mb^2+3mt^2]) = 0.004608$

sin(*theta23 = [mmu+3ms+3mc]/sqrt([mtau^2+3mb^2+3mt^2]+ + [mmu^2+3ms^2+3mc^2])

sin(theta23) = s23 = sin(*theta23) sqrt(Sigmaf2 / Sigmaf1) = 0.04234886

The factor sqrt(Smf2 /Smf1) appears in s23 because an s23 transition is to the second generation and not all the way to the first generation, so that the end product of an s23 transition has a greater available energy than s12 or s13 transitions by a factor of Smf2 / Smf1.

Since the width of a transition is proportional to the square of the modulus of the relevant KM entry and the width of an s23 transition has greater available energy than the s12 or s13 transitions by a factor of Smf2 / Smf1 the effective magnitude of the s23 terms in the KM entries is increased by the factor sqrt(Smf2 /Smf1).

The Chau-Keung parameterization is used, as it allows the K-M matrix to be represented as the product of the following three 3x3 matrices:

1	0	0
0	cos(theta23)	sin(theta23)
0	-sin(theta23)	cos(theta23)
cos(theta13)	0	sin(theta13)exp(-i d13)
0	1	0
-sin(theta13)exp(i d13)	0	cos(theta13)
cos(theta12)	sin(theta12)	0
-sin(theta12)	cos(theta12)	0
0	0	1

The resulting Kobayashi-Maskawa parameters for W+ and W- charged weak boson processes, are:

	d	S	b
u	0.975	0.222	0.00249 -0.00388i
С	-0.222 -0.000161i	0.974 -0.0000365i	0.0423
t	0.00698 -0.00378i	-0.0418 -0.00086i	0.999

The matrix is labelled by either (u c t) input and (d s b) output, or, as above, (d s b) input and (u c t) output.

For Z0 neutral weak boson processes, which are suppressed by the GIM mechanism of cancellation of virtual subprocesses, the matrix is labelled by either (u c t) input and (u'c't') output, or, as below, (d s b) input and (d's'b') output:

	d	S	b
d'	0.975	0.222	0.00249 -0.00388i
s'	-0.222 -0.000161i	0.974 -0.0000365i	0.0423
b'	0.00698 -0.00378i	-0.0418 -0.00086i	0.999

Since neutrinos of all three generations are massless at tree level, the lepton sector has no tree-level K-M mixing.

In hep-ph/0208080, Yosef Nir says: "... Within the Standard Model,

the only source of CP violation is the Kobayashi-Maskawa (KM) phase ...

The study of CP violation is, at last, experiment driven. ...

The CKM matrix provides a consistent picture

of all the measured flavor and CP violating processes. ...

There is no signal of new flavor physics. ...

Very likely,

the KM mechanism is the dominant source of CP violation in flavor changing processes.

... The result is consistent with the SM predictions. ...".

Appendix - Neutrino Masses Beyond Tree Level

```
Consider the three generations of neutrinos:
nu e (electron neutrino); nu m (muon neutrino); nu t
and three neutrino mass states: nu 1 ; nu 2 : nu 3
and
the division of 8-dimensional spacetime into
4-dimensional physical Minkowski spacetime
plus
4-dimensional CP2 internal symmetry space.
The heaviest mass state nu 3 corresponds to a neutrino
whose propagation begins and ends in CP2 internal symmetry
space, lying entirely therein. According to the Cl(1,25) E8 model
the mass of nu 3 is zero at tree-level
but it picks up a first-order correction
propagating entirely through internal symmetry space by merging
with an electron through the weak and electromagnetic forces,
effectively acting not merely as a point
but
as a point plus an electron loop at beginning and ending points
so
the first-order corrected mass of nu 3 is given by
M nu 3 x (1/sqrt(2)) = M e x GW(mproton^2) x alpha E
where the factor (1/sqrt(2)) comes from the Ut3 component
of the neutrino mixing matrix
so that
M nu 3 = sqrt(2) x M e x GW(mproton<sup>2</sup>) x alpha E =
= 1.4 x 5 x 10^5 x 1.05 x 10^(-5) x (1/137) eV =
= 7.35 / 137 = 5.4 \times 10^{(-2)} \text{ eV}.
The neutrino-plus-electron loop can be anchored by weak force
```

action through any of the 6 first-generation quarks at each of the beginning and ending points, and that the anchor quark at the beginning point can be different from the anchor quark at the ending point, so that there are 6x6 = 36 different possible anchorings. The intermediate mass state nu_2 corresponds to a neutrino whose propagation begins or ends in CP2 internal symmetry space and ends or begins in M4 physical Minkowski spacetime, thus having only one point (either beginning or ending) lying in CP2 internal symmetry space where it can act not merely as a point but as a point plus an electron loop.

According to the Cl(1,25) E8 model the mass of nu_2 is zero at tree-level but it picks up a first-order correction at only one (but not both) of the beginning or ending points so that so that there are 6 different possible anchorings for nu_2 first-order corrections, as opposed to the 36 different possible anchorings for nu_3 first-order corrections, so that the first-order corrected mass of nu_2 is less than the first-order corrected mass of nu_3 by a factor of 6, so

```
the first-order corrected mass of nu_2 is

M_{nu_2} = M_{nu_3} / Vol(CP2) = 5.4 \times 10^{(-2)} / 6

= 9 x 10^(-3)eV.
```

The low mass state nu_1 corresponds to a neutrino whose propagation begins and ends in physical Minkowski spacetime. thus having only one anchoring to CP2 interna symmetry space. According to the Cl(1,25) E8 model the mass of nu_1 is zero at tree-level but it has only 1 possible anchoring to CP2 as opposed to the 36 different possible anchorings for nu_3 first-order corrections or the 6 different possible anchorings for nu_2 first-order corrections so that the first-order corrected mass of nu_1 is less than the first-order corrected mass of nu_2 by a factor of 6, so the first-order corrected mass of nu 1 is

 $M_{nu_1} = M_{nu_2} / Vol(CP2) = 9 \times 10^{(-3)} / 6$ = 1.5 x 10^(-3)eV. Therefore:

and

the mass-squared difference
$$D(M12^2) = M_nu_2^2 - M_nu_1^2 =$$

= (81 - 2) x 10^(-6) eV^2 =
= 7.9 x 10^(-5) eV^2

The 3x3 unitary neutrino mixing matrix neutrino mixing matrix U

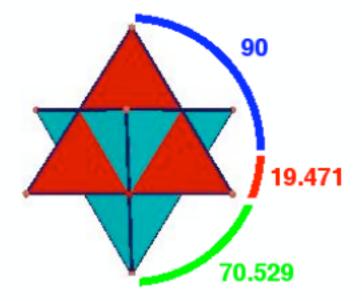
	nu_1	nu_2	nu_3
nu_e	Ue1	Ue2	Ue3
nu_m	Um1	Um2	Um3
nu_t	Ut1	Ut2	Ut3

can be parameterized (based on the 2010 Particle Data Book) by 3 angles and 1 Dirac CP violation phase

c12 c13	s12 c13	s13 e-id		
U = - s12 c23 - c12 s23 s13 eid	c12 c23 - s12 s23 s13 eid	s23 c13		
s12 s23 - c12 c23 s13 eid -	c12 s23 - s12 c23 s13 eid	c23 c13		
<pre>where cij = cos(theta_ij) , sij = sin(theta_ij)</pre>				

```
The angles are
theta 23 = pi/4 = 45 degrees
because
nu 3 has equal components of nu m and nu t so
that Um3 = Ut3 = 1/sqrt(2) or, in conventional
notation, mixing angle theta 23 = pi/4
so that cos(theta 23) = 0.707 = sqrt(2)/2 = sin(theta 23)
theta 13 = 9.594 degrees = asin(1/6)
and \cos(\text{theta } 13) = 0.986
because sin(theta 13) = 1/6 = 0.167 = |Ue3| = fraction of nu 3 that is nu e
theta 12 = pi/6 = 30 degrees
because
sin(theta 12) = 0.5 = 1/2 = Ue2 = fraction of nu 2 begin/end points
that are in the physical spacetime where massless nu e lives
so that \cos(\text{theta 12}) = 0.866 = \operatorname{sqrt}(3)/2
d = 70.529 degrees is the Dirac CP violation phase
ei(70.529) = cos(70.529) + i sin(70.529) = 0.333 + 0.943 i
This is because the neutrino mixing matrix has 3-generation structure
and so has the same phase structure as the KM quark mixing matrix
in which the Unitarity Triangle angles are:
\beta = V3.V1.V4 = arccos( 2 sqrt(2) / 3 ) \cong 19.471 220 634 degrees so sin 2\beta =
0.6285
\alpha = V1.V3.V4 = 90 degrees
\gamma = V1.V4.V3 = \arcsin(2 \text{ sqrt}(2) / 3) \approx 70.528 779 366 \text{ degrees}
```

The constructed Unitarity Triangle angles can be seen on the Stella Octangula configuration of two dual tetrahedra (image from gauss.math.nthu.edu.tw):



Then we have for the neutrino mixing matrix:

	nu_1	nu_2		nu_3
nu_e	0.866 x 0.986	0.50 x 0.	986	0.167 x e-id
nu_m	-0.5 x 0.707 -0.866 x 0.707 x 0.	0.866 x 0 167 x eid -0.5 x 0.7		0.707 x 0.986
nu_t	0.5 x 0.707 -0.866 x 0.707 x 0.	-0.866 x 0 167 x eid -0.5 x 0.7		0.707 x 0.986
	nu_1	nu_2		nu_3
nu_e	0.853	0.493		0.167 e-id
nu_m	-0.354 -0.102 eid	0.612 -0.059 eid		0.697
nu_t	0.354 -0.102 eid	-0.612 -0.059 eid		0.697
Since ei(70.529) = cos(70.529) + i sin(70.529) = 0.333 + 0.943 i and .333e-i(70.529) = cos(70.529) - i sin(70.529) = 0.333 - 0.943 i				
	nu_1	nu_2	nu_3	
nu_e	0.853	0.493	0.056 - 0.157 i	
nu_m	-0.354 -0.034 - 0.096 i	0.612 -0.020 - 0.056 i	0.697	
nu_t	0.354 -0.034 - 0.096 i	-0.612 -0.020 - 0.056 i	0.697	
for a result of				
	nu_1	nu_2	nu_3	

nu_e	0.853	0.493	0.056 - 0.157 i
nu_m	-0.388 - 0.096 i	0.592 - 0.056 i	0.697
nu_t	0.320 - 0.096 i	0.632 - 0.056 i	0.697

which is consistent with the approximate experimental values of mixing angles shown in the Michaelmas Term 2010 Particle Physics handout of Prof Mark Thomson if the matrix is modified by taking into account the March 2012 results from Daya Bay observing non-zero theta_13 = 9.54 degrees.

Appendix - Proton-Neutron Mass Difference

An up valence quark, constituent mass 313 Mev,

does not often swap places with a 2.09 Gev charm sea quark,

but

a 313 Mev down valence quark

can more often swap places with a 625 Mev strange sea quark.

Therefore the Quantum color force constituent mass of the down valence quark is heavier by about

(ms - md) (md/ms)² a(w) |Vdsl = 312 x 0.25 x 0.253 x 0.22 Mev = 4.3 Mev,

(where a(w) = 0.253 is the geometric part of the weak force strength and IVdsI = 0.22 is the magnitude of the K-M parameter mixing first generation down and second generation strange)

so that the Quantum color force constituent mass Qmd of the down quark is

Qmd = 312.75 + 4.3 = 317.05 MeV.

Similarly, the up quark Quantum color force mass increase is about

(mc - mu) (mu/mc)² a(w) IV(uc)I = 1777 x 0.022 x 0.253 x 0.22 Mev = 2.2 Mev,

(where |Vuc| = 0.22 is the magnitude

of the K-M parameter mixing first generation up and second generation charm)

so that the Quantum color force constituent mass Qmu of the up quark is

Qmu = 312.75 + 2.2 = 314.95 MeV.

Therefore, the Quantum color force Neutron-Proton mass difference is

mN - mP = Qmd - Qmu = 317.05 Mev - 314.95 Mev = 2.1 Mev.

Since the electromagnetic Neutron-Proton mass difference is roughly

$$mN - mP = -1 MeV$$

the total theoretical Neutron-Proton mass difference is

an estimate that is comparable to the experimental value of 1.3 Mev.

Appendix - Pion as Sine-Gordon Breather

The quark content of a charged pion is a quark - antiquark pair: either Up plus antiDown or Down plus antiUp. Experimentally, its mass is about 139.57 MeV.

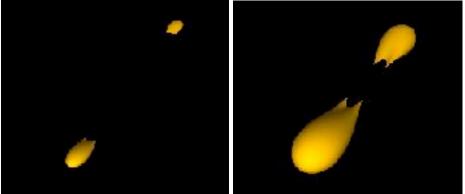
The quark is a Schwinger Source Kerr-Newman Black Hole with constituent mass M 312 MeV.

The antiquark is also a Schwinger Source Kerr-Newman Black Hole, with constituent mass M 312 MeV.

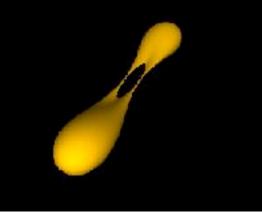
According to section 3.6 of Jeffrey Winicour's 2001 Living Review of the Development of Numerical Evolution Codes for General Relativity (see also a 2005 update): "... The black hole event horizon associated with ... slightly broken ... degeneracy [of

the axisymmetric configuration]... reveals new features not seen in the degenerate case of the head-on collision ... If the degeneracy is slightly broken, the individual black holes form with spherical topology but as they approach, tidal distortion produces two sharp pincers on each black hole just prior to merger. ...

Tidal distortion of approaching black holes ... Formation of sharp pincers just prior to merger ..



... toroidal stage just after merger ...



At merger, the two pincers join to form a single ... toroidal black hole.

The inner hole of the torus subsequently [begins to] close... up (superluminally) ... [If the closing proceeds to completion, it]... produce[s] first a peanut shaped black hole and finally a spherical black hole. ...".

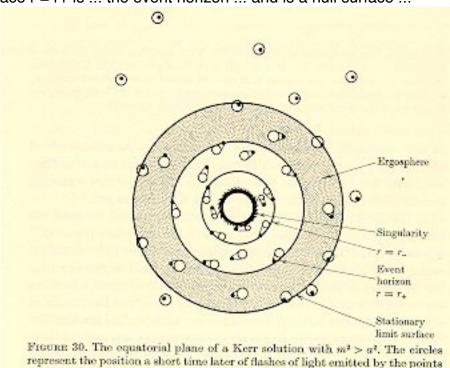
In the physical case of quark and antiquark forming a pion,

the toroidal black hole remains a torus.

The torus is an event horizon and therefore is not a 2-spacelike dimensional torus, but is a (1+1)-dimensional torus with a timelike dimension.

The effect is described in detail in Robert Wald's book General Relativity (Chicago 1984). It can be said to be due to extreme frame dragging, or to timelike translations becoming spacelike as though they had been Wick rotated in Complex SpaceTime.

As Hawking and Ellis say in The LargeScale Structure of Space-Time (Cambridge 1973):



"... The surface r = r+ is ... the event horizon ... and is a null surface ...

... On the surface r = r + ... the wavefront corresponding to a point on this surface lies entirely within the surface. ...".

represented by heavy dots.

A (1+1)-dimensional torus with a timelike dimension can carry a Sine-Gordon Breather. The soliton and antisoliton of a Sine-Gordon Breather correspond to the quark and antiquark that make up the pion, analagous to the Massive Thirring Model.

Sine-Gordon Breathers are described by Sidney Coleman in his Erica lecture paper Classical Lumps and their Quantum Descendants (1975), reprinted in his book Aspects of Symmetry (Cambridge 1985),

where he writes the Lagrangian for the Sine-Gordon equation as (Coleman's eq. 4.3):

 $L = (1 / B^2) ((1/2) (df)^2 + A (cos(f) - 1))$

Coleman says: "... We see that, in classical physics, B is an irrelevant parameter: if we can solve the sine-Gordon equation for any non-zero B, we can solve it for any other B.

The only effect of changing B is the trivial one of changing the energy and momentum assigned to a given solution of the equation. This is not true in quantum physics, because the relevant object for quantum physics is not L but [eq. 4.4]

 $L / hbar = (1 / (B^2 hbar)) ((1/2) (df)^2 + A (cos(f) - 1))$

An other way of saying the same thing is to say that in quantum physics we have one more dimensional constant of nature, Planck's constant, than in classical physics. ... the classical limit, vanishing hbar, is exactly the same as the small-coupling limit, vanishing B ... from now on I will ... set hbar equal to one. ...

... the sine-Gordon equation ...[has]... an exact periodic solution ...[eq. 4.59]... $f(x, t) = (4 / B) \arctan((n \sin(w t) / \cosh(n w x))$

where [eq. 4.60] $n = sqrt(A - w^2) / w$ and w ranges from 0 to A.

This solution has a simple physical interpretation ... a soliton far to the left ...[and]... an antisoliton far to the right. As sin(w t) increases, the soliton and antisoliton move farther apart from each other. When sin(w t) passes through one,

they turn around and begin to approach one another. As sin(w t) comes down to zero ... the soliton and antisoliton are on top of each other ...

when sin(w t) becomes negative .. the soliton and antisoliton have passed each other.

... Thus, Eq. (4.59) can be thought of as a soliton and an antisoliton oscillation about their common center-of-mass. For this reason, it is called 'the doublet [or Breather] solution'. ... the energy of the doublet ...[eq. 4.64]

$$E = 2 M sqrt(1 - (w^2 / A))$$

where [eq. 4.65] M = 8 sqrt(A) / B² is the soliton mass.

Note that the mass of the doublet is always less than twice the soliton mass, as we would expect from a soliton-antisoliton pair. ...

Dashen, Hasslacher, and Neveu ... Phys. Rev. D10, 4114; 4130; 4138 (1974). ...[found that]... there is only a single series of bound states, labeled by the integer N ... The energies ... are ... [eq. 4.82]

 $E_N = 2 M \sin(B'^2 N / 16)$

where N = 0, 1, 2 ... < 8 pi / $B^{\prime}2$, [eq. 4.83]

 $B'^{2} = B^{2} / (1 - (B^{2} / 8 pi))$ and M is the soliton mass.

M is not given by Eq. (4.65), but is the soliton mass corrected by the DHN formula, or, equivalently, by the first-order weak coupling expansion. ...

I have written the equation in this form .. to eliminate A,

and thus avoid worries about renormalization conventions.

Note that the DHN formula is identical to the Bohr-Sommerfeld formula.

except that B is replaced by B'. ...

Bohr and Sommerfeld['s] ... quantization formula says that if we have a one-parameter family of periodic motions, labeled by the period, T,

then an energy eigenstate occurs whenever [eq. 4.66]

[Integral from 0 to T](dt p qdot = 2 pi N,

where N is an integer. ... Eq.(4.66) is cruder than the WKB formula, but it is much more general;

it is always the leading approximation for any dynamical system ...

Dashen et al speculate that Eq. (4.82) is exact. ...

the sine-Gordon equation is equivalent ... to the massive Thirring model. This is surprising,

because the massive Thirring model is a canonical field theory

whose Hamiltonian is expressed in terms of fundamental Fermi fields only.

Even more surprising, when $B^2 = 4 pi$, that sine-Gordon equation is equivalent

to a free massive Dirac theory, in one spatial dimension. ...

Furthermore, we can identify the mass term in the Thirring model with the sine-Gordon interaction, [eq. 5.13]

 $M = -(A/B^2) N_m \cos(Bf)$

.. to do this consistently ... we must say [eq. 5.14]

....[where]... g is a free parameter, the coupling constant [for the Thirring model]... Note that if $B^2 = 4 pi$, g = 0,

and the sine-Gordon equation is the theory of a free massive Dirac field. ...

It is a bit surprising to see a fermion appearing as a coherent state of a Bose field. Certainly this could not happen in three dimensions,

where it would be forbidden by the spin-statistics theorem.

However, there is no spin-statistics theorem in one dimension,

for the excellent reason that there is no spin. ...

the lowest fermion-antifermion bound state of the massive Thirring model

is an obvious candidate for the fundamental meson of sine-Gordon theory. ...

equation (4.82) predicts that

all the doublet bound states disappear when B^2 exceeds 4 pi .

This is precisely the point where

the Thirring model interaction switches from attractive to repulsive. ... these two theories ... the massive Thirring model .. and ... the sine-Gordon equation ... define identical physics. ...

I have computed the predictions of ...[various]... approximation methods for the ration of the soliton mass to the meson mass for three values of B^2 : 4 pi (where the qualitative picture of the soliton as a lump totally breaks down), 2 pi, and pi . At 4 pi we know the exact answer ...

I happen to know the exact answer for 2 pi, so I have included this in the table. ...

Method	B^2 = pi	B^2 = 2 pi	B^2 = 4 pi
Zeroth-order weak couplise expansion eq2.13b	ng 2.55	1.27	0.64
Coherent-state variation	2.55	1.27	0.64
First-order weak coupling expansion	2.23	0.95	0.32
Bohr-Sommerfeld eq4.64	2.56	1.31	0.71
DHN formula eq4.82	2.25	1.00	0.50
Exact	?	1.00	0.50

...[eq. 2.13b]

$$E = 8 \operatorname{sqrt}(A) / B^2$$

...[is the]... energy of the lump ... of sine-Gordon theory ... frequently called 'soliton...' in the literature ... [Zeroth-order is the classical case, or classical limit.] Coherent-state variation always gives the same result as the ... Zeroth-order weak coupling expansion The ... First-order weak-coupling expansion ... explicit formula ... is (8 / B^2) - (1 / pi). ...".

Using the Cl(1,25) E8 model constituent mass of the Up and Down quarks and antiquarks, about 312.75 MeV, as the soliton and antisoliton masses, and setting $B^2 = pi$ and using the DHN formula, the mass of the charged pion is calculated to be (312.75 / 2.25) MeV = 139 MeV which is close to the experimental value of about 139.57 MeV.

Why is the value B² = pi the special value that gives the pion mass ? (or, using Coleman's eq. (5.14), the Thirring coupling constant g = 3 pi) Because B² = pi is where the First-order weak coupling expansion substantially coincides with the (probably exact) DHN formula. In other words, The physical guark - antiguark pion lives where the first-order weak coupling

expansion is exact.

Appendix - Planck Mass as Superposition Fermion Condensate

At a single spacetime vertex, a Planck-mass black hole is the Many-Worlds quantum sum of all possible virtual first-generation particle-antiparticle fermion pairs allowed by the Pauli exclusion principle to live on that vertex.

Once a Planck-mass black hole is formed, it is stable in the E8 model. Less mass would not be gravitationally bound at the vertex. More mass at the vertex would decay by Hawking radiation.

There are 8 fermion particles and 8 fermion antiparticles for a total of 64 particle-antiparticle pairs. Of the 64 particle-antiparticle pairs, 12 are bosonic pions.

A typical combination should have about 6 pions so it should have a mass of about .14x6 GeV = 0.84 GeV.

Just as the pion mass of .14 GeV is less than the sum of the masses of a quark and an antiquark, pairs of oppositely charged pions may form a bound state of less mass than the sum of two pion masses.

If such a bound state of oppositely charged pions has a mass as small as .1 GeV, and if the typical combination has one such pair and 4 other pions, then the typical combination could have a mass in the range of 0.66 GeV.

Summing over all 2^64 combinations,

the total mass of a one-vertex universe should give a Planck mass roughly around $0.66 \times 2^{64} = 1.217 \times 10^{19}$ GeV.

The value for the Planck mass given in by the 1998 Particle Data Group is 1.221 x 10^19 GeV.

Appendix - Lagrangian Terms

Gauge Gravity and Standard Model terms of Lagrangian have total weight 28 x 1 = 28 12 generators for SU(3) and U(2) Standard Model + + 16 generators for U(2,2) of Conformal Gravity =

= 28 D4 Gauge Bosons each with 8-dim Lagrangian weight = 1

Fermion Particle-AntiParticle term also has total weight 8 x (7/2) = 28 8 Fermion Particle/Antiparticle types each with 8-dim Lagrangian weight = 7/2

Since Boson Weight 28 = Fermion Weight 28 the Cl(1,25) E8 model has a Subtle SuperSymmetry and is UltraViolet Finite.

The 8 fermion particles each have dimension 7/2 because they are in the spinor fermion term of the Lagrangian. In his part of the book Elemetary Particles and the Laws of Physics: The 1986 Dirac Memorial Lectures Steven Weinberg described the Lagrangian in 4-dimensional spacetime as in the attached pdf excerpt



WeinbergLag....pdf (732 KB)

in which he shows that in 4-dim spacetime (the base manifold over which his Lagrangian is integrated) the fermion particles each have dimension 3/2 because the fermion term is the product of two fermions and a mass term which has dimension 1, so that 3/2 + 3/2 + 1 = 4 = spacetime dimension.

```
In my model with 8-dim Kaluza-Klein spacetime,
my Lagrangian must be integrated over 8 dimensions
so the fermion term (also product of two fermions and one mass)
must have dimension 7/2
for the Lagrangian dimensionality formula
7/2 + 7/2 + 1 = 8 = spacetime dimension
to hold true.
```

Here is how the top of the last page of the Weinberg excerpt should look for my 8-dimensional Kaluza-Klein spacetime:

All terms in the Lagrangian density must have units [mass]⁸, because length and time have units of inverse mass and the Lagrangian density integrated over spacetime must have no units. From the $m\psi\psi$ term, we see that the electron field must have units [mass]^{7/2}, because $\frac{7}{2} + \frac{7}{2} + 1 = 8$

$$\begin{aligned} \mathscr{L} &= -\bar{\psi} \left(\gamma^{\mu} \frac{\partial}{\partial x^{\mu}} + m \right) \psi \\ &- \frac{1}{4} \left(\frac{\partial A_{\nu}}{\partial x^{\mu}} - \frac{\partial A_{\mu}}{\partial x^{\nu}} \right)^{2} \\ &+ \mathrm{i} e A_{\mu} \bar{\psi} \gamma^{\mu} \psi \\ &- \mu \left(\frac{\partial A_{\nu}}{\partial x^{\mu}} - \frac{\partial A_{\mu}}{\partial x_{\nu}} \right) \bar{\psi} \sigma^{\mu\nu} \psi \\ &- G \bar{\psi} \psi \bar{\psi} \psi + \cdots . \end{aligned}$$
(1)

It may not mean very much to most of you; on the other hand it means a lot to some of you! Fortunately almost all of the details are irrelevant for the points that I want to make. Let me explain briefly what all the symbols mean. \mathcal{L} stands for Lagrangian density; roughly speaking you can think

of it as the density of energy. Energy is the quantity that determines how the state vector rotates with time, so this is the role that the Lagrangian density plays; it tells us how the system evolves. It's written as a sum of products of fields and their rates of change. ψ is the field of the electron (a function of the spacetime position x), and m is the mass of the electron. $\partial/\partial x^{\mu}$ means the rate of change of the field with position. γ^{μ} and $\sigma^{\mu\nu}$ are matrices about which I will say nothing, except that the γ^{μ} matrices are called Dirac matrices. A_{μ} is the field of the photon, called the electromagnetic field.

Looking in order at each term on the right-hand side of the equation, the first term involves the field twice, the next term involves the electron photon field twice because the bracket is squared, the third and fourth terms involve two electron fields and one photon field, the fifth term involves four electron so on. The symmetries of quantum fields. and electrodynamics give us well-defined rules for the construction of the terms in the Lagrangian, but there are an infinite number of terms allowed, with increasing numbers of fields, and also increasing numbers of derivative operators acting on them. Each independent called the term has an constant. coupling constant, that multiplies it. These are the quantities e, μ, G, \dots in (1). The coupling constant

gives the strength with which the term affects the dynamics. No coupling constants appear in the first two terms simply because I have chosen to absorb them into the definition of the two fields ψ and A_{μ} . If there were a constant in front of the first term, for example, I would just redefine ψ to absorb it. But for all the other terms, infinity minus two of them, there is a constant in front of each term. In principle all these constants are there, and they are all unknown. How in the world can you make any money out of a theory like this?

In fact, it's not that bad. Experimentally we know that the formula consisting of just the first three terms, with all higher terms neglected, is adequate to describe electrons and photons to a fantastic level of accuracy. This theory is known as quantum electrodynamics, or QED. it would be very easy to figure out what contribution an observable gets from its cloud of virtual photons and electron-positron pairs at very high energy E. Let's suppose an observable \mathcal{O} has dimensions [mass]^{- α}, where α is positive. (Of course, since the speed of light is one in these natural units, mass and energy are essentially the same quantity.) Now, at very high virtual-particle energy, E, much higher than any mass, or any energy of α particle in the initial or final state, there is nothing to fix a unit of energy. The contribution of high energy virtual particles to the observable \mathcal{O} must then be given an integral like

$$\mathcal{O} = \int^{\infty} \frac{\mathrm{d}E}{E^{\alpha+1}} \tag{3}$$

because this is the only quantity which has the right dimensions, the right units, to give the observable O. (The lower bound in the integral is some finite energy that marks the dividing line between what we call high and low energy.) This argument only works because there are no other quantities in the theory that have the units of mass or energy. All physicists use this sort of argument from time to time, especially when they can't think of anything else to do.

On the other hand, suppose that there are other

constants around that have units of mass raised to a negative power. Then if you have an expression involving a constant C_1 with units $[mass]^{-\beta_1}$, and another constant C_2 with units $[mass]^{-\beta_2}$ and so on, then instead of the simple answer obtained above we get a sum of terms of the form

$$\mathcal{O} = C_1 C_2 \cdots \int^{\infty} \frac{E^{\beta_1 + \beta_2 + \cdots}}{E^{\alpha + 1}} dE \qquad (4)$$

again because these are the only quantities that have the right units for the observable O. Expression (3) is perfectly well-defined, the integral converges (it doesn't add up to infinity), as long as the number α is greater than zero. However, if $\beta_1 + \beta_2 + \cdots$ is greater than α , then (4) will not be well-defined, because the numerator will have more powers of energy than the denominator and so the integral will diverge. The point is that no matter how many powers of energy you have in the denominator, i.e. no matter how large α is, (4) eventually will diverge when you get up to sufficiently high order in the coupling constants, C_1 , C_2 , etc., that have dimensions of negative powers of mass, because if you have enough of these constants, then eventually β_1 + \cdots is greater than α .

Looking at the Lagrangian density in (1), we can easily work out what the units of the constant e, μ , G, etc., are.

All terms in the Lagrangian density must have units [mass]⁴, because length and time have units of inverse mass and the Lagrangian density integrated over spacetime must have no units. From the $m\psi\psi$ term, we see that the electron field must have units [mass]^{3/2}, because $\frac{3}{2} + \frac{3}{2} + 1$ = 4. The derivative operator (the rate of change operator) has units of [mass]¹, and so the photon field also has units [mass]¹. Now we can work out what the units of the coupling constants are. As I said before, the electric charge turns out to be a pure number, to have no units. But then as you add more and more powers of fields, more and more derivatives, you are adding more and more quantities that have units of positive powers of mass, and since the Lagrangian density has to have fixed units of [mass]⁴, therefore the mass dimensions of the associated coupling constants must get lower and lower, until eventually you come to constants like μ and G which have negative units of mass. (Specifically, μ has the units of [mass]⁻¹, while G has the units $[mass]^{-2}$.) Such terms in (1) would completely spoil the agreement between theory and experiment for the magnetic moment of the electron, so experimentally we can say that they are not there to a fantastic order of precision, and for many years it seems that this could be explained by saying that such terms must be excluded because they would give infinite results, as in (4).

Appendix - E8 Fermionic AntiCommutators

Pierre Ramond has shown in hep-th/0112261 as shown that the exceptional Lie Algebra F4 can be described using anticommutators as well as commutators.

The periodicity property of Real Clifford Algebras shows that E8 Spinor Fermions can also be described using anticommutators as well as commutators

so that the E8 Physics model describes both Bosons and Fermions realistically.

Realistic Physics models must describe both

integer-spin Bosons whose statistics are described by commutators

(examples are Photons, W and Z bosons, Gluons, Gravitons, Higgs bosons) and

half-integer-spin Fermions whose statistics are described by anticommutators. (examples are 3 generations of Electrons, Neutrinos, Quarks and their antiparticles)

Lie Algebra elements are usually described by commutators of their elements so

if a Physics model attempts to describe both Bosons and Fermions as elements of a single unifiying Lie Algebra (for example, Garrett Lisi's E8 TOE) a common objection is:

> since the Lie Algebra is described by commutators, it can only describe Bosons and cannot describe Fermions therefore models (such as Garrett Lisi's) using E8 as a single unifying Lie Algebra violate the consistency of spin and statistics and are wrong.

However,

Pierre Ramond has shown in hep-th/0112261 as shown that the exceptional Lie Algebra F4 can be described using anticommutators as well as commutators.

The periodicity property of Real Clifford Algebras shows that E8 inherits from F4 a description using anticommutators as well as commutators so that it may be possible to construct a realistic Physics model that uses the exceptional Lie Algebra E8 to describe both Bosons and Fermions.

Here are relevant quotes from hep-th/0112261 by Pierre Ramond: "... exceptional algebras relate tensor and spinor representations of their orthogonal subgroups,

while Spin-Statistics requires them to be treated differently ... all representations of the exceptional group F4 are generated by three sets of oscillators transforming as 26. We label each copy of 26 oscillators as

 $Ak_0\;,\quad Ak_i\;,\;i=1,\;\ldots\;,\;9,\quad Bk_a\;,\;a=1,\;\ldots\;,\;16,\\ and their hermitian conjugates, and where \;k=1,\;2,\;3.$

•••

One can ... use a coordinate representation of the oscillators by introducing real coordinates

...[for A_i]... which transform as transverse space vectors,

...[for A_0]... which transform ... as scalars,

and ...[for B_a]... which transform ... as space spinors which satisfy Bose commutation rules

•••

Under SO(9), the Ak_i transform as 9, Bk_a transform as 16, and Ak_0 is a scalar. They satisfy the commutation relations of ordinary harmonic oscillators ... Note that the SO(9) spinor operators satisfy Bose-like commutation relations ... both A_0 and B_a ... obey Bose commutation relations

Curiously,

if both ... A_0 and B_a ... are anticommuting, the F4 algebra is still satisfied ...".

To see how the anticommuting property of the 16 B_a elements of F4 can be inherited by some of the elements of E8, consider that 52-dimensional F4 is made up of:

28-dimensional D4 Lie Algebra Spin(8) (in commutator part of F4)
8-dimensional D4 Vector Representation V8 (in commutator part of F4)
8-dimensional D4 +half-Spinor Representation S+8 (in anticommutator part of F4)
8-dimensional D4 -half-Spinor Representation S-8 (in anticommutator part of F4)

Since 28-dimensional D4 Spin(8) is the BiVector part BV28 of the Real Clifford Algebra Cl(8) with graded structure Cl(8) = 1 + V8 + BV28 + 56 + 70 + 56 + 28 + 8 + 1and with Spinor structure $Cl(8) = (S+8 + S-8) \times (8 + 8)$

F4 can be embedded in CI(8) (blue commutator part, red anticommutator part):

F4 = V8 + BV28 + S+8 + S-8

Note that V8 and S+8 and S-8 are related by the Triality Automorphism.

Also consider the 8-periodicity of Real Clifford Algebras, according to which for all N

 $CI(8N) = CI(8) \times ...(N \text{ times tensor product})... CI(8)$

so that in particular Cl(16) = Cl(8) x Cl(8) where Cl(16) graded structure is 1 + 16 + BV120 + 560 + ... + 16 + 1and Cl(16) Spinor structure is ((S+64 + S-64) + (64 + 64)) x (128 + 128) and Cl(16) contains 248-dimensional E8 as

E8 = BV120 + S+64 + S-64

where BV120 = 120-dimensional D8 Lie Algebra Spin(16) and S+64 + S-64 = 128-dimensional D8 half-Spinor Representation

Consider two copies of F4 embedded into two copies of Cl(8).

For commutator structure:

The tensor product of the two copies of Cl(8) can be seen as

which produces the Real Clifford Algebra Cl(16) with graded structure

1 + 16 + BV120 + 560 + 1820 + ... + 16 + 1

where the CI(16) BiVector BV120 is made up of 3 parts

BV120 = BV28x1 + 1xBV28 + V8xV8

that come from the V8 and BV28 commutator parts of the two copies of F4.

This gives the commutator part of E8 as BV120 inheriting commutator structure from the two copies of F4 embedded in two copies of Cl(8) whose tensor product produces Cl(16) containing E8.

For anticommutator structure:

The tensor product of the two copies of 256-dim Cl(8) can also be seen as

which produces the 2^16 = 65,536 = 256x256-dim Real Clifford Algebra Cl(16)

with 256-dimensional Spinor structure

$$= ((S+8 \times S+8) + (S-8 \times S-8)) + ((S+8 \times S-8) + (S-8 \times S+8))$$

that comes from the S+8 and S-8 anticommutator parts of the two copies of F4.

Since the (S+8 x S-8) and (S-8 x S+8) terms inherit mixed helicities from F4

only the $(S+8 \times S+8)$ and $(S-8 \times S-8)$ terms inherit consistent helicity from F4.

Therefore, define $S+64 = (S+8 \times S+8)$ and $S-64 = (S-8 \times S-8)$ so that (S+64 + S-64) = 128-dimensional D8 half-Spinor Representation

This gives the anticommutator part of E8 as S+64 + S-64 inheriting anticommutator structure from the two copies of F4 embedded in two copies of Cl(8) whose tensor product produces Cl(16) containing E8.

The result is that 248-dimensional E8 is made up of:

BV120 = 120-dimensional D8 Lie Algebra Spin(16) (commutator part of E8)

128-dimensional (S+64 + S-64) D8 half-Spinor (anticommutator part of E8)

Note that since the V8 and S+8 and S-8 components of F4 are related by Triality, and since the E8 component BV120 contains 64-dimensional V8xV8 and the 64-dimensional E8 component S+64 = S+8 x S+8 and the 64-dimensional E8 component S-64 = S-8 x S-8

E8 inherits from the two copies of F4 a Triality relation

V8xV8 = S+64 = S-64

The commutator - anticommutator structure of E8 allows construction of realistic Physics models that not only unify both Bosons and Fermions within E8 but

also contain Triality-based symmetries between Bosons and Fermions that can give the useful results of SuperSymmetry

without requiring conventional SuperPartner particles that are unobserved by LHC.

CONCLUSION:

Unified E8 Physics models can be constructed without violating spin-statistics.

Appendix - Details of Coleman-Mandula

The CI(1,25) E8 model has 8-dim Lorentz structure satisfying Coleman-Mandula because its fermionic fundamental spinor representations are built with respect to spinor representations for 8-dim Spin(1,7) spacetime.

The Quantum Theory of Fields

Volume III Supersymmetry Steven Weinberg University of Texas at Austin



Supersymmetry Algebras in Higher Dimensions

Ever since the ground-breaking work of Kaluza¹ and Klein,² theorists have from time to time tried to formulate a more nearly fundamental physical theory in spacetimes of higher than four dimensions. This approach was revived in superstring theories, which take their simplest form in 10 spacetime dimensions.³ More recently, it has been suggested that the various versions of string theory may be unified in a theory known as M*theory*, which in one limit is approximately described by supergravity in 11 spacetime dimensions.⁴ In this chapter we shall catalog the different types of supersymmetry algebra possible in higher dimensions, and use them to classify supermultiplets of particles.

32.1 General Supersymmetry Algebras

Our analysis of the general supersymmetry algebra in higher dimensions will follow the same logical outline as the work of Haag. Lopuszanski, and Sohnius⁵ on supersymmetry algebras in four spacetime dimensions, described in Section 25.2. The proof of the Coleman-Mandula theorem in the appendix of Chapter 24 makes it clear that the list of possible bosonic symmetry generators is essentially the same in d > 2 spacetime dimensions as in four spacetime dimensions: in an S-matrix theory of particles, there are only the momentum d-vector P^{μ} , a Lorentz generator $J^{\mu\nu} = -J^{\nu\mu}$ (with μ and ν here running over the values 1, 2, ..., d-1, 0), and various Lorentz scalar 'charges.' (In some theories there are topologically stable extended objects such as closed strings, membranes, etc., in addition to particles, which make possible other conserved quantities, to which we will return in Section 32.3.) The anticommutators of the fermionic symmetry generators with each other are bosonic symmetry generators, and therefore must be a linear combination of P^{μ} , $J^{\mu\nu}$, and various conserved scalars. This puts severe limits on the Lorentz transformation properties of the fermionic generators, and on the superalgebra to which they belong.

We will first prove that the general fermionic symmetry generator must transform according to the fundamental spinor representations of the Lorentz group, which are reviewed in the appendix to this chapter, and not in higher spinor representations, such those obtained by adding vector indices to a spinor. As we saw in Section 25.2, the proof for d = 4 by Haag, Lopuszanski, and Sohnius made use of the isomorphism of SO(4)to $SU(2) \times SU(2)$, which has no analog in higher dimensions. Here we will use an argument of Nahm,⁶ which is actually somewhat simpler and applies in any number of dimensions.

Since the Lorentz transform of any fermionic symmetry generator is another fermionic symmetry generator, the fermionic symmetry generators furnish a representation of the homogeneous Lorentz group O(d-1,d)(or, strictly speaking, of its covering group Spin(d-1,1)). Assuming that there are at most a finite number of fermionic symmetry generators, they must transform according to a finite-dimensional representation of the homogeneous Lorentz group. All of these representations can be obtained from the finite-dimensional unitary representations of the corresponding orthogonal group O(d) (actually Spin(d)) by setting $x^d = ix^0$. So let us first consider the transformation of the fermionic generators under O(d). For d even or odd, we can find d/2 or (d-1)/2 Lorentz generators J_{d1} , J_{23}, J_{45}, \ldots , which all commute with each other, and classify fermionic generators Q according to the values $\sigma_{d1}, \sigma_{23}, \ldots$ that they destroy:

$$[J_{d1}, Q] = -\sigma_{d1}Q, \qquad [J_{23}, Q] = -\sigma_{23}Q, \qquad [J_{45}, Q] = -\sigma_{45}Q, \dots$$
(32.1.1)

Since the finite-dimensional representations of O(d) are all unitary, the σs are all real.

Let us focus on one of these quantum numbers, $\sigma_{d1} \equiv w$ and refer to any fermionic or bosonic operator O as having weight w if

$$[J_{d1}, O] = -w O, \qquad (32.1.2)$$

or, in terms of the Minkowski component $J_{01} = iJ_{d1}$,

$$[J_{01}, O] = -iw O . (32.1.3)$$

The reason for concentrating on this particular quantum number is that it has the special property of being the same for an operator and its Hermitian adjoint. This is because J_{01} must be represented on Hilbert space (though not on field variables or symmetry generators) by a Hermitian operator, so that (remembering that w is real) the Hermitian adjoint of Eq. (32.1.3) is

$$-[J_{01}, 0^*] = +iw0^*, \qquad (32.1.4)$$

so O^* has the same weight as O.

Now consider the anticommutator $\{Q, Q^*\}$ of any fermionic symmetry generator Q with its Hermitian adjoint. According to the Coleman-Mandula theorem, it is at most a linear combination of P_{μ} , $J_{\mu\nu}$, and scalars. To calculate the weights of the components of P_{μ} , we recall the commutation relation (2.4.13)

$$i[P_{\mu}, J_{\rho\sigma}] = \eta_{\mu\rho}P_{\sigma} - \eta_{\mu\sigma}P_{
ho}$$
,

which shows that $P_0 \pm P_1$ has weight $w = \pm 1$, while the other components $P_2, P_3, \ldots, P_{d-1}$ all have weight zero. In the same way, the commutation relation (2.4.12) of the $J_{\mu\nu}$ with each other show that $J_{0i} \pm J_{1i}$ with $i = 2, 3, \dots d - 1$ have weight $w = \pm 1$, the J_{ij} with both i and j between 2 and d-1 have weight zero, J_{10} has weight zero, and of course all scalars have weight zero. We conclude then that all bosonic symmetry generators have weight ± 1 or 0 and the anticommutator $\{Q, Q^*\}$ must be a linear combination of operators with such weights. If Q has weight w then $\{Q, Q^*\}$ has weight 2w, and it is manifestly non-zero for any non-zero Q, so each fermionic generator can only have weight $\pm 1/2$. (Weight zero is excluded by the connection between spin and statistics — fermionic operators can only be constructed from odd numbers of operators with half-integer weights.) Going back to the Euclidean formalism, since the commutators of the particular O(d) generator J_{01} with all generators Q in a representation of O(d) are given by Eq. (32.1.2) with $w = \pm 1/2$, and there is nothing special about the 01 plane, O(d) invariance requires that the same is true for all O(d) generators J_{ij} , so that all the σ s in Eq. (32.1.1) are $\pm 1/2$. The only irreducible representations of the homogeneous Lorentz group with all σ s equal to $\pm 1/2$ are the fundamental spinor representations, so Q must belong to some direct sum of these representations.

We can also use this approach to show that the fermionic generators Q all commute with the *d*-momentum P_{μ} . For this purpose, note that the double commutator of a momentum operator $P_0 \pm P_1$ of weight ± 1 with any fermionic generator Q would have weight either $\pm 5/2$ if Q has weight $\pm 1/2$ or weight $\pm 3/2$ if Q has weight $\pm 1/2$, and since we have found that there are no fermionic symmetry generators of weight $\pm 3/2$ or $\pm 5/2$, these double commutators must all vanish:

$$[P_0 \pm P_1, [P_0 \pm P_1, Q]] = 0.$$

It follows then that

$$[P_0 \pm P_1, [P_0 \pm P_1, \{Q, Q^*\}]] = -2\{Q_{\pm}, Q_{\pm}^*\},\$$

where

$$Q_{\pm} \equiv [P_0 \pm P_1, Q] \; .$$

Now, $\{Q, Q^*\}$ is at most a linear combination of Js, Ps, and scalar

symmetry generators. The commutators of $P_0 \pm P_1$ with the Ps and scalar symmetry generators vanish, while the commutators of $P_0 \pm P_1$ with the Js are linear combinations of Ps, which commute with the other $P_0 \pm P_1$, so the double commutator $[P_0 \pm P_1, [P_0 \pm P_1, \{Q, Q^*\}]]$ must vanish and therefore $\{Q_{\pm}, Q_{\pm}^*\} = 0$, which implies that $Q_{\pm} = 0$. Since all members of the representation of the Lorentz group provided by the Qs thus commute with P_0 and P_1 , Lorentz invariance implies that all Qs commute with all Ps, as was to be shown.

There is an important corollary that since the Lorentz generators $J_{\mu\nu}$ do not commute with the momentum operators, they cannot appear on the right-hand side of the anticommutation relations. For the moment let us label the Qs as Q_n , where *n* runs over the labels for the different (not necessarily inequivalent) irreducible spinor representations among the Qs, now *including* their adjoints Q^* , and also over the index labelling members of these representations. The general anticommutation relation is then of the form

$$\{Q_n, Q_m\} = \Gamma^{\mu}_{nm} P_{\mu} + Z_{nm} , \qquad (32.1.5)$$

where the Γ_{nm}^{μ} are c-number coefficients and the Z_{nm} are conserved scalar symmetry generators, which commute with the P_{μ} and $J_{\mu\nu}$. We now want to show that the Z_{nm} are *central charges* of the supersymmetry algebra that is, that they commute with the Q_{ℓ} and each other as well as with the P_{μ} and $J_{\mu\nu}$ and all other symmetry generators.

To prove this for $d \ge 4$, note that for a given Z_{nm} to be non-zero, since it is a scalar all of the σ s in Eq. (32.1.1) must be opposite for Q_n and Q_m . Consider another fermionic symmetry generator Q_ℓ , for which the σ s of Eq. (32.1.1) are not all the same as those of either Q_n or Q_m . (For $d \ge 4$ there is always such a Q_ℓ in each set of Q_s forming an irreducible spinor representation of O(d).) We apply the super-Jacobi identity

$$[Q_{\ell}, \{Q_m, Q_n\}] + [Q_m, \{Q_n, Q_{\ell}\}] + [Q_n, \{Q_{\ell}, Q_m\}] = 0.$$
(32.1.6)

The anticommutators $\{Q_n, Q_\ell\}$ and $\{Q_\ell, Q_m\}$ are operators that have some σ s non-zero, so they can only be linear combinations of Ps rather than Zs, and so must commute with all Qs. This leaves just

$$0 = [Q_{\ell}, \{Q_m, Q_n\}] = [Q_{\ell}, Z_{mn}]. \qquad (32.1.7)$$

Thus in each set of Qs forming an irreducible spinor representation of O(d) there is at least one that commutes with the given Z_{mn} . But Z_{mn} is a Lorentz scalar, so it must then commute with all Qs. It follows then immediately from Eq. (32.1.5) that they also commute with each other.

The fermionic generators must form a representation (perhaps trivial) of the algebra \mathscr{A} consisting of all scalar bosonic symmetry generators. It follows then by precisely the same argument used in Section 25.2 that

the central charges Z_{mn} furnish an invariant Abelian subalgebra of \mathscr{A} . The Coleman-Mandula theorem tells us that \mathscr{A} must be a direct sum of a compact semi-simple Lie algebra, which by definition contains no invariant Abelian subalgebras, together with U(1) generators, so the Z_{mn} must be U(1) generators, which commute with all other bosonic symmetry generators, not just with each other.

To obtain more detailed information about the structure of the anticommutation relations (32.1.5), we must be more specific about the Lorentz transformation and reality properties of the fermionic symmetry generators Q_n . These are very different for spacetimes of even and odd dimensionality.

Odd Dimensionality

The appendix to this chapter shows that for odd spacetime dimensions d there is just one fundamental spinor representation of the Lorentz algebra, by matrices $\mathscr{J}_{\mu\nu}$ given in terms of Dirac matrices by Eq. (32.A.2), so we must label the fermionic generators as $Q_{\alpha r}$, where α is a $2^{(d-1)/2}$ -valued Dirac index, and r = 1, 2, ..., N labels different spinors in the case of N-extended supersymmetry. With this notation, the Lorentz transformation properties of the Qs imply that

$$[J_{\mu\nu}, Q_{\alpha r}] = -\sum_{\beta} (\mathscr{J}_{\mu\nu})_{\alpha\beta} Q_{\beta r}, \qquad (32.1.8)$$

so that the anticommutators of these generators have the transformation rule

$$[J_{\mu\nu}, \{Q_{\alpha r}, Q_{\beta s}\}] = -\sum_{\bar{\alpha}} (\mathscr{J}_{\mu\nu})_{\alpha\bar{\alpha}} \{Q_{\bar{\alpha} r}, Q_{\beta s}\} - \sum_{\bar{\beta}} (\mathscr{J}_{\mu\nu})_{\beta\bar{\beta}} \{Q_{\alpha r}, Q_{\bar{\beta} s}\}.$$

Recalling the Lorentz transformation rule (2.4.13) for the momentum operator P_{λ} , we see that the matrix Γ_{rs}^{λ} and the operator Z_{rs} in Eq. (32.1.5) (with Dirac indices now suppressed) must satisfy the conditions

$$\mathscr{J}_{\mu\nu}(\Gamma_{\lambda})_{rs} + (\Gamma_{\lambda})_{rs}\mathscr{J}^{\Gamma}_{\mu\nu} = -i(\Gamma_{\mu})_{rs}\eta_{\nu\lambda} + i(\Gamma_{\nu})_{rs}\eta_{\mu\lambda} , \qquad (32.1.9)$$

$$\mathscr{J}_{\mu\nu}Z_{rs} + Z_{rs}\mathscr{J}_{\mu\nu}^{T} = 0. \qquad (32.1.10)$$

But Eq. (32.A.38) gives $\mathscr{J}_{\mu\nu}^{T} = -\mathscr{C}^{-1} \mathscr{J}_{\mu\nu} \mathscr{C}$, so Eqs. (32.1.9) and (32.1.10) may be expressed as the requirement that $(\Gamma_{\mu})_{rs} \mathscr{C}^{-1}$ satisfies the same commutation relation (32.A.32) with $\mathscr{J}_{\mu\nu}$ as γ_{μ} , while $Z_{rs} \mathscr{C}^{-1}$ commutes with $\mathscr{J}_{\mu\nu}$. For odd *d* the matrices satisfying these conditions are unique up to multiplication with constants, so we can conclude that

$$\Gamma^{\lambda}_{\alpha r \ \beta s} = i \, g_{rs} \, (\gamma^{\lambda} \, \mathscr{C})_{\alpha \beta} \tag{32.1.11}$$

Appendix - Details of Mayer - Higgs

Excerpts from:

Meinhard Mayer and A. Trautman in "A Brief Introduction to the Geometry of Gauge Fields" and Meinhard Mayer in "The Geometry of Symmetry Breaking in Gauge Theories", Acta Physica Austriaca, Suppl. XXIII (1981))

and

Shoshichi Kobayashi and Katsumi Nomizu in "Foundations of Differential Geometry Vol. I", Interscience (1963)

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A BRIEF INTRODUCTION TO THE GEOMETRY OF GAUGE FIELDS M. E. Mayer and A. Trautman

THE GEOMETRY OF SYMMETRY BREAKING IN GAUGE THEORIES M. E. Mayer

GEOMETRIC ASPECTS OF QUANTIZED GAUGE THEORIES M. E. Mayer

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FOREWORD

The papers contained in this volume are lectures and seminars presented at the 20th "Universitätswochen für Kernphysik" in Schladming in February 1981. The goal of this school was to review some rapidly developing branches in mathematical physics. Thanks to the generous support provided by the Austrian Federal Ministry of Science and Research, the Styrian Government and other sponsors, it has been possible to keep up with the - by now already traditional - standards of this school. The lecture notes have been reexamined by the authors after the school and are now published in their final form, so that a larger number of physicists may profit from them. Because of necessary limitations in space all details connected with the meeting have been omitted and only brief outlines of the seminars were included. It is a pleasure to thank all the lecturers for their efforts, which made it possible to speed up the publication. Thanks are also due to Mrs. Krenn for the careful typing of the notes.

H.Mitter

L.Pittner

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A BRIEF INTRODUCTION TO THE GEOMETRY OF GAUGE FIELDS"

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1. INTRODUCTION

In view of the common background required for the understanding of the lectures of both authors, and in order to avoid unnecessary duplications, we have decided to present jointly this brief introduction to the language and properties of fiber bundles. By now the advantages of the fiber-bundle formulation of gauge field theories have led to a widespread acceptance of this language, and a number of reviews of the subject have appeared or are in course of publication. These, together with a number of standard textbooks are listed in the references to this

⁺Lectures given at the XX. Internationale Universitätswochen für Kernphysik, Schladming, Austria, February 17 - 26, 1981. introduction. Nevertheless, we felt that it would be convenient for the reader of these proceedings to have at his disposal a summary of the basic facts. We also tried to clarify a number of concepts and propose an acceptable terminology wherever a standard has not been established in the literature. This refers, in particular, to the terms gauge transformation , pure gauge transformation, and the related (infinite-dimensional) groups as well as to the concepts of extension, prolongation, restriction, and reduction of bundles, which are used with slightly varying meaning in different texts.

In the oral presentation most of the general background material was presented by Andrzej Trautman, and the material related to reduction and symmetry of connections was given in Meinhard Mayer's lectures. Little, if anything, in this introduction is original. The actual text has been written in California by the first author and slightly revised by the second during his stay in France after the Schladming meeting.

No detailed proofs are given here, but wherever possible illustrations and examples are used to make the concepts plausible to physicists. Many proofs are straightforward and can be carried out by introducting local coordinates and bases. However, we recommend to the reader who wants to become familiar with the spirit of modern, coordinate-free, differential geometry to try to stay away from bases and indices as much as possible.

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It is easy to see that the orbit space of P under the action of the subgroup H of G, P/H, can be identified with the associated bundle E. Denoting by γ the canonical projection of G onto G/H, we can set for $p \in P, \delta(p) =$ = $p \cdot \gamma(e)$, where e is the identity of G. The mapping $\delta: P + E$ is a projection for the new principal bundle (P, H, E, δ) over the larger base E = $P \times_G G/H$ which is canonically identified with the orbit space P/H (this is illustrated in Fig. 4, in the middle).

Let now σ : M + E denote a section of E and $\sigma^{\texttt{H}}$: (P, H, E, δ) = (Q, H, M, ρ) the pullback (induced bundle) of this map. It is obvicus (cf. Fig. 4, right) that this is now a principal bundle with structure group H over M, and its extension to G is isomorphic to the original bundle P. Two different sections σ_1 and σ_2 of E will define isomorphic restrictions iff they are mapped into each other by a pure gauge transformation (G-M-automorphism) of P. Otherwise different sections of E determine different (nonisomorphic) restrictions.

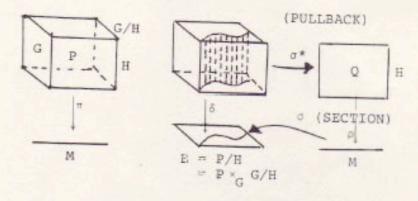


Fig. 4

6. INVARIANCE AND SYMMETRIES OF CONNECTIONS

In spite of the fact that conditions for the invariance of a connection have been discussed in the mathematical literature over twenty years ago, and Wang's theorem can be found in textbooks, physicists rediscovered them only in 1978-79. This section contains a brief survey of this topic, which has been discussed from a more physical point of view by Jackiw in last year's Schladming lectures.

The problem is quite simple when viewed globally, on the principal bundle; complications arise only when one tries to express the invariance conditions for the connection forms on local trivializations of P.

Before discussing connections we summarize the definitions of gauge transformations to be used. An isomorphism of a principal bundle onto itself is called an <u>automorphism</u> of the bundle. Such an automorphism consists of a pair of diffeomorphisms (u,v) of P and M such that $\pi ou = vo\pi$ (Eq. (3.1)), and $u(p \cdot g) = u(p) \cdot g$ for all $p \in P$, $g \in G$. An automorphism is called vertical if $v = Id_M$. If we denote the group of all automorphisms (an infinitedimensional group) by Aut P, the subgroup of all vertical automorphisms Aut_MP is a normal subgroup, the quotient being the group of all diffeomorphisms of M onto itself, i.e., we have the exact sequence of homomorphisms:

 $I \rightarrow Aut_M P \xrightarrow{i} Aut P \xrightarrow{j} Diff M \rightarrow I$, (6.1)

where i is the canonical injection and v = j(u). If $u \in Aut_M^P$, its action is in the fiber and therefore can be implemented by an element U(p) of G such that for any p in P and g in G

 $u(p) = p \cdot U(p), U(p \cdot g) = g^{-1}U(p)g$ (6.2)

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Thus, there is a natural isomorphism of $\operatorname{Aut}_{M}^{P}$ onto the multiplicative group of (smooth) maps U : P \rightarrow G, subject to the equivariance condition (6.2), or equivalently, to sections of the associated bundle P $\times_{\operatorname{AdG}}^{G}$ with fibers G, but the right action replaced by the adjoint action.

The group Aut P (as well as $\operatorname{Aut}_M P$) acts on (local) sections of P in the following manner: if $s : V \neq P$ (V an open subset of M), then its transform is $s' = u \circ s \circ v^{-1}$. If $u \in \operatorname{Aut}_M P$, the subset V of M is left invariant and the section is subject to what a physicist would call a gauge transformation:

 $s'(x) = s(x) \cdot U(s(x)), x \in V \subset M$. (6.3)

If one deals only with Yang-Mills fields over a flat spacetime (or a Euclidean, compact version thereof) one is thus entitled to identify Aut_MP with the group of gauge transformations (this is the definition adopted by Atiyah, Singer, and many other mathematicians). However, in theories involving gravity, or other structures on spacetime, it is convenient to introduce a further differentiation.

<u>Definition.</u> The <u>gauge group</u> of a theory in which the bundle has some <u>absolute elements</u>, such as the metric tensor of special relativity, or some other structure element of P or M, is the subgroup G of Aut P such that the diffeomorphism v and the projection preserve the absolute elements of M. The group of <u>pure gauge transformations</u> consists of the vertical automorphisms in G; this group will be denoted by $G_0 = G \cdot \operatorname{Aut}_M P$, it is a normal subgroup of G, and the quotient G/G_0 in the exact sequence

(6.4)

I+Go ig jo G /Go +I

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is the subgroup of Diff M leaving the absolute elements invariant (e.g., if M is Minkowski space, $\frac{6}{9}$ / $\frac{6}{9}$ o is the Poincaré group; this corresponds to the necessity of sometimes combining a gauge transformation with a change of Lorentz frame in some calculations).

Invariance of connections under automorphisms of the bundle P is simply expressed as the fact that the pullback of the connection form ω on P by the mapping $u \in Aut P, \omega' = u^{\varkappa}\omega$ is again a connection form on P. If u is a vertical automorphism (in particular, a pure gauge transformation), then

$$\omega' = Ad(U^{-1}(p))\omega + U^{-1}(p)dU(p) , \qquad (6.5)$$

where U(p) is the map defined in Eq.(6.2). We see that the form ω is subject to the usual gauge transformation of a gauge potential (albeit, on P rather than on M). The curvature form Ω' of the pullback $u^{it}\omega$ is given by the adjoint action of U(p) on the original curvature form:

$$\Omega' = Ad(U^{-1}(p))\Omega$$
 (6)

The equations (6.5), (6.6) can easily be pulled down to the forms A, F on the base space given by a locally trivializing section s. Here one can either pull w back to M by the transformed section, or pull w' back by the original section, obtaining the usual gauge transformation formulas for A and F:

$$A' = Ad(S^{-1})A + S^{-1}dS$$
, $F' = Ad(S^{-1})F$, (6.7)

where $S = U \circ s$.

Among the automorphisms of the principal bundle P with a connection ω and the associated bundles carrying the particle fields, symmetries are distinguished by the

.6)

fact that they preserve the connection ω and the absolute elements of the theory (e.g., they preserve the action, or they modify the Lagrangian density by a divergence). In particular, a <u>symmetry</u> of a gauge theory is a gauge transformation (in the wider sense defined above) which leaves the connection form ω invariant (in addition to the other absolute elements):

 $u^{H}\omega = \omega, u^{H}\Omega = \Omega ;$

(6.8)

since a nonabelian gauge theory is not completely determined by the curvature, it is not sufficient to require invariance only of the curvature form.

When this condition is pulled back by a local trivialization to the base space, it will usually be formulated as the requirement that the one-form A be unchanged up to a pure gauge transformation, or in other words, a gauge field is invariant under a symmetry, if the symmetry transformation can be compensated by a gauge transformation of the locally trivializing section (this is the formulation given by Bergmann and Flaherty, Trautman, Jackiw, and other authors).

To write the invariance condition (6.8) for the physical fields A, F, we consider first a one-parameter group $u_t : R \rightarrow Aut P$ of automorphisms of P. Let Y denote the corresponding vector field on P, and X the projection of Y onto M:

 $X = \pi_{H}Y$.

(6.9)

The vector field X generates a one-parameter group $v_t = j(u_t)$ of transformations on M. Let ω be a u_t -invariant connection on P,

 $u_{\pm}^{H}\omega = \omega, \quad u_{\pm}^{H}\Omega = \Omega$

(6.10)

For an arbitrary point p in P the groups ut, vt define curves in P, M, respectively:

$$p_t = u_t(p_0)$$
, $x_t = v_t(\pi p_0) = \pi(p_t)$. (6.11)

The connection defines a horizontal lift of x_t which we denote by h_t . Then it is obvious that $p_t = h_t g_t$ for a suitable element g_t of G, and g_t is a one-parameter Lie subgroup of G, generated by the Lie algebra element $T = \omega_{p_0}(Y)$. The invariance of the connection and its curvature on P can be expressed infinitesimally as the vanishing of their Lie derivatives with respect to Y:

$$L_{Y}\omega = 0$$
, $L_{Y}\Omega = 0$. (6.12)

(Recall that for forms the Lie derivative is defined by $L_{Y} = d \circ Y \rfloor + Y \rfloor \circ d$, where denotes the interior product of Y with the differential form following the sign.)

The expressions (6.12) for the invariance of connections are identical to the usual conditions for the invariance of fields encountered in physics, but hidden behind the simple form is the gauge freedom inherent in the theory, particularly if one works in terms of the pullbacks A, F, to the base space. If we denote the value of the one-form ω_p (at the point p in P) on the vector field Y at p by $Z = \omega_p(Y)$, we obtain an equivariant map of P into the Lie algebra $Z : P + G, Z \circ R_g = Ad(g^{-1}) \circ Z$. Its covariant exterior differential

 $DZ = dZ + [\omega, Z]$

(6.13)

is a horizontal one-form (with values in G) of type Ad, and the definition of the Lie derivative and Eq.(6.14) yield the detailed form of the invariance condition:

$$L_{Y}\omega = Y \lrcorner \Omega + DZ = 0, \ L_{Y}\Omega = D(Y \lrcorner \Omega) + [\Omega, Z] = 0 \quad (6.14)$$

(Trautman, 1979). If we use a local section s to pull back the connection and curvature to the gauge potential A, and the field strength F on M, the vector field Y is to be replaced by the generator X of the transformations in M, and the Lie-algebra-valued function on P, Z, defines a function on M, $\phi = Z$ o s : M + G. Then the invariance conditions for A and F under the symmetry induced on M by the vector field X (such a vector field always has a horizontal lift under the given connection; adding an arbitrary vertical vector field of the type of Z to it, will give a field on P) can be written in the form

 $X J F + D\Phi = 0 \tag{6.15}$

(6.16)

where $D\Phi = d\Phi + [A, \Phi]$, and

 $D(X JF) + [F, \Phi] = O.$

In terms of the potential one-form A the invariance condition can be rewritten as $L_X^A = DW(X)$, where W(X) differs from 0 by the zero-form -X J A. The right-hand side of the last equation has the infinitesimal form of a gauge transformation, and under a change of chart (gauge transformation) with transition functions g_{ij} the function W is subject to the transformation

$$W_{j} = Ad(g_{ij}^{-1}) W_{i} + g_{ij}^{-1} X J dg_{ij}$$
 (6.17)

If X₁ and X₂ denote two vector fields on M inducing symmetries of the connection A, then consistency requires that

$$2F(X_1, X_2) = \Phi([X_1, X_2]) - [\Phi(X_1), \Phi(X_2)] , \qquad (6.18)$$

where the left-hand side denotes the value of the two-form

F on the two vector fields X₁, X₂, and the right-hand side expresses the dependence of the G-valued O-form on the vector field X₁ (and implicitly, on the trivializing section s). The infinitesimal forms of the invariance conditions have been independently discovered by Forgacs and Manton, Harnad, Shnider and Vinet, and Jackiw (cf. the bibliography to Mayer's contribution for references), and the usefulness of Eqs.(6.15), (6.18) (with a difference in sign) has been discussed in Jackiw's 1980 Schladming lectures.

To end this section we give, for the convenience of the reader, a brief statement of Wang's theorems on invariant connections, in a notation which is close to the one used by Kobayashi and Nomizu, where the detailed proofs can be found.

Consider, as before, a principal bundle P(M,G), with a connection w which is invariant with respect to a group of automorphisms K of P(M,G), assumed to be a connected Lie group with fiber-transitive action, i.e., for any two fibers there is an element of K which maps one into the other, hence K acts transitively on the base space M. We denote by u a reference point in P, chosen once and for all, and by x_0 its projection in M, $x_0 = \pi(u_0)$. Furthermore we denote by J the isotropy subgroup of K at x, i.e., the subgroup of all transformations in K which leave x invariant (it is clear that M can then be viewed as the homogeneous space K/J). We denote the Lie algebras of the groups G, K, J by g, k, j , respectively and, when it exists, the subspace of k complementary to j by m: k = = $j \div m$ (direct sum). Then we define a linear mapping Λ : k + g by $\Lambda(X) = \omega_{U_{\Omega}}(X)$, where $X \in k$ and \hat{X} is the vector field on P induced by X, which has the properties (i) $\Lambda(X) = \lambda_{H}(X)$ for $X \in j$; here λ_{H} is the homomorphism $\lambda_{ii}: j \rightarrow g$ defined as the differential of the homomorphism

 $\lambda : J \neq G$, which assigns an element $g \in G$ taking the point u_0 into the same point as the left action of $j \in J : ju_0 = u_0g : g = \lambda(j);$

(ii) for $j \in J$ and $X \in k$, $\Lambda(Ad(j)(X)) = Ad(\lambda(j))(\Lambda(X))$, where Ad(j) is the adjoint action of J on k and Ad($\lambda(j)$) is that of G on g. The geometric meaning of these homomorphisms should be clear from our discussion of the lifting of the horizontal projection of any one-parameter group of automorphisms given by Eq.(6.11) and the discussion following it. Note that u_0 denotes our previous p_0 (and not the value of the automorphism at t = 0), and the vertical action $\lambda(j)$ is the same as the previous g_t .

It is easy to verify, by using the definition of curvature (the structure equation), that the curvature form Ω satisfies the condition (from which Eq.(6.18) follows by pullback to M):

 $2\Omega_{u}(\hat{X},\hat{Y}) = [\Lambda(X),\Lambda(Y)] - \Lambda([X,Y]), \text{ for } X, Y \in k . \quad (6.19)$

What Wang's theorem asserts is the existence of a bijection between the set of K-invariant connections in P and the set of linear mappings Λ : k + g satisfying the conditions listed above, bijection which is given by

 $\Lambda(X) = \omega_{u_0}(X), \text{ for } X \in k . \tag{6.20}$

The proof is straightforward and can be found, e.g., in Kobayashi and Nomizu (p.107, with the same notations as here).

It also follows immediately that a K-invariant connection is flat (i.e., has vanishing curvature) iff Λ : k + g is a Lie algebra homomorphism (since then the right-hand side of Eq.(23) vanishes, and hence so does the left-hand side).

Moreover, if in addition the Lie subalgebra j admits a complementary subspace m in k such that $\operatorname{Ad}(J)(m) = (m)$, then there is a bijection between the set of K-invariant connections in P and the set of linear mappings $\Lambda_m : m \circ g$, such that for $X \in m$, $j \in J$ we have $\Lambda_m(\operatorname{Ad}(j)(X)) = \operatorname{Ad}(\lambda(j))$ $(\Lambda_m(X))$, with the bijection given in terms of the Λ defined above by $\Lambda(X) = \lambda(X)$ if $X \notin j$, and $\Lambda(X) = \Lambda_m(X)$ if $X \notin m$. The curvature form of the K-invariant connection defined by the linear mapping Λ_m satisfies the following condition:

$$2\Omega_{\mathbf{u}_{O}}(\mathbf{X},\mathbf{Y}) = [\Lambda_{\mathbf{m}}(\mathbf{X}),\Lambda_{\mathbf{m}}(\mathbf{Y})] - \Lambda_{\mathbf{m}}([\mathbf{X},\mathbf{Y}]_{\mathbf{m}}) - \lambda([\mathbf{X},\mathbf{Y}]_{\mathbf{y}}),$$

where the subscripts on the brackets denote components in the corresponding subspaces of the algebra κ where the bracket is originally defined. If $\Lambda_m = 0$ then the corresponding invariant connection is called the <u>canonical in-</u> <u>variant connection</u> with respect to the decomposition $\kappa = j + m$. Physically, this corresponds to choosing the gauge functions Z and the connection A in eqs.(6.13) -(6.18) so that the components of ϕ in the subspace m, corresponding to the given decomposition, should vanish.

It is to be noted that the existence of a complementary subspace m invariant under the adjoint action of J is equivalent to the reductivity of the homogeneous space K/J = M, a rather restrictive condition on the base space M.

Finally, it should be noted that the Lie algebra of the holonomy group of a K-invariant connection at u_0 is defined by a sum of iterated brackets of $\Lambda(k)$ with the subspace m_0 of g spanned by the right-hand side of eq. (6.19) (for details we refer the reader again to Kobayashi-Nomizu, p.110-111). Acta Physica Austriaca, Suppl. XXIII, 477-490 (1981) © by Springer-Verlag 1981

THE GEOMETRY OF SYMMETRY BREAKING IN GAUGE THEORIES"

by

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ABSTRACT

This together with Sections 3 and 6 of the joint contribution with A. Trautman (this volume, pp. 433 to be referred to as Mayer-Trautman) constitutes a summary of the first two lectures. Much of the material is available elsewhere [1], so only results and some open questions are discussed. The subject matter of the second two lectures is treated in the following contribution (pp. 491).

1. INTRODUCTION

The motivation of these lectures is a search for an alternative to the traditional Brout-Englert-Higgs-Kibble (BEHK) method of symmetry breaking in gauge theories, based on the geometry of principal bundles with connections. In the BEHK approach the action of the classical theory of a Dirac or Weyl field interacting with a Klein-Yang-Mills field A, F is

⁺Lectures given at the XX. Internationale Universitätswochen für Kernphysik, Schladming, Austria, Pebruary 17-26, 1981.

$$S_{DYM} = \frac{1}{4} \int_{M} \text{Tr} F \wedge {}^{x}F + \int_{M} {}^{x} \{\psi \beta \psi\} , \qquad (1.1)$$

where M denotes the spacetime base manifold of the bundles, F is the Yang-Mills field strength two-form on M (the pulldown of the curvature two-form to M, cf. Mayer-Trautman, Eq.(4.12)), " is the Hodge-dual on M, ψ denotes a Dirac or Weyl spinor which transforms under a representation of the structure group G (a local representation of a section in a tensor product of a spin bundle and a vector bundle associated to the gauge principal bundle P by that representation). Ø denotes the "gauge-covariant Dirac-Weyl operator" (in coordinates, with e a basis for the representation of the Lie algebra G, in which I denotes the unit matrix, and γ^{μ} the usual Dirac matrices) $p = I \not a + A^{a}_{\mu} \gamma^{\mu} e_{a}$. In order to produce the symmetry breaking, leading to a restriction of the original bundle P to a subbundle Q(M,H), the BEHK model introduces "by hand" a scalar field ϕ which represents a section of an associated bundle (or a smooth function on P with values in some representation space V of G, cf. Mayer-Trautman, Eq.(2.5)), which is supposed to be an extremal of the Ginzburg-Landau action:

 $S_{GL} = \int D\phi \wedge \pi D + \nabla[\phi], \nabla[\phi] = -\mu \|\phi\|^2 + \lambda \|\phi\|^4 , \qquad (1.2)$

where the norms in the Ginzburg-Landau functional V are to be understood as the result of integration over M of the hermitian norm in V. For positive λ,μ the functional V has nontrivial critical points ϕ_0 and the stabilizer subgroup of these is H, the symmetry group of the "vacuum" to which the bundle is then restricted. Reducing the connection form A and the curvature form F to the corresponding Lie algebra H, one can choose a gauge in which the terms involving the nonvanishing ϕ_0^2 in (1.2) appear like "mass terms" for the components of A in the complement M = G - H of the Lie algebra of H in that of G, thus leading to a loss of con-

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formal invariance for the appropriate Yang-Mills equations. The surviving Higgs fields and the fermions are also aquiring "masses" by this mechanism. For details of this and other aspects of traditional symmetry breaking the reader is referred to the review by O'Raifeartaigh [2] where further references can be found.

A closer look at the BEHK mechanism (and this will partially be true of the geometric models discussed in this lecture too) shows that the presence of the Ginzburg-Landau potential is not really at the heart of the matter. The scalar field and the quartic interaction were chosen because they lead to a renormalizable quantum theory and are the simplest combination which does the job. In effect, the reason why they do the job is revealed by a careful analysis of group actions on manifolds, particularly of pairs of groups such as G and H, and their homogeneous spaces G/H. Such an analysis was carried out in other contexts of symmetry breaking by Michel and Radicati [3] over a decade ago, and a good summary can be found in Ref.[2]. It turns out that if one is given G and H, there are relatively few invariants which lead to the desired physical results, among them the Ginzburg-Landau action.

The same remarks apply, mutatis mutandis, to the orbit structure of the associated bundles E(M,P,G/H,p) discussed below in symmetry breaking models. In fact, the symmetry breaking sections should appear from a detailed analysis, in the spirit of Michel and Radicati, of the orbits and strata of group actions in these bundles. There does not seem to exist in the literature an explicit discussion of this topic, and it was hoped that such a discussion could be included here. However, time pressure forced me to defer this to a future publication.

Until recently, Higgs fields were considered almost sacrosanct, but the view that they really exist (and the

appropriate particles should indeed manifest themselves experimentally) is becoming less widely held. Many of us who were not satisfied by the artificial introduction of the Higgs fields have been searching for alternatives to the introduction of the Higgs bosons, yielding the same results which made this model so appealing and successful in the electroweak unification, and in all grand unified gauge theories. I will not discuss theories in which the Higgs scalars are treated as bound states of more elementary fermions, or metric theories of the Kaluza-Klein type (for an interesting recent attempt to obtain the putative SU(3)×SU(2)×U(1) symmetry of strong and electroweak interactions, I refer the reader to a recent paper by Witten [4]) but will describe briefly two "geometric" approaches to the problem which can be described in the language of bundle restrictions (cf. Mayer-Trautman, Secs. 3 and 6).

The second is based on the introduction of hidden dimensions followed by a "dimensional reduction" [7,8,9] and makes use of symmetries of connections and curvatures discussed in Sec. 6 of Mayer-Trautman, and should be considered a direct application of the methods discussed there.

3. HIDDEN DIMENSIONS AND SYMMETRY BREAKING

Another approach to symmetry breaking (more correctly, a whole class of approaches) is based on the introduction of "hidden dimensions" into the principal bundle on which a gauge theory is based, with the result that certain components of the connection take over the role of the Higgs bosons and produce the required violation of conformal invariance of the Yang-Mills equations. There are essentially two ways of introducing hidden dimensions into a principal bundle, which I will call the Kaluza-Klein, and Weyl methods, respectively. In a Kaluza-Klein approach one starts from a Riemannian or pseudo-Riemannian manifold of dimension 4 + k, writes down the Einstein-Hilbert action (linear in the curvature) for the metric in this space, and treats the non-block-diagonal terms as a Yang-Mills connection. The appropriate terms in the action then yield, among others, terms which are quadratic

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in the Yang-Mills curvature and can thus be interpreted as a Yang-Mills action. The general theory of such models has been discussed in many places; cf., e.g., Trautman's lecture in this volume, the forthcoming book by Bleecker [12], and Witten's recent atempt [4] to obtain an $SU(3) \times SU(2) \times U(1)$ gauge theory from an eleven-dimensional Kaluza-Klein model.

The Weyl approach, also known as "dimensional reduction" or "fiberflipping", has been particularly popular among supersymmetrists (I will not discuss supersymmetric gauge models here), and has been successfully used by Manton [8] in a model which derives many of the features of the standard electroweak unification from a G2-principal bundle by this method.

The general theory of such symmetry breaking can be formulated as follows. We start out from a principal bundle P(M,G) over four-dimensional M, with hidden symmetry group G as the structure group. The symmetry group of the vacuum H, a closed subgroup of G, is assumed known. A given symmetry breaking is then described, as already discussed, by a section of the associated bundle E(M,P,G/H,p). We now take E as the base space of a new bundle R(E,G) with structure group G (not H, as was the case for the restriction Q(M,H)) obtained as the pullback of P under the projection p of the associated bundle E: $R = p^{\mu}P$. (Pictorially, one can think of R as the bundle obtained from P by "reattaching, or flipping" part of the fiber, G/H, so that it appears both in the base space and in the fiber.)

The result is a larger principal bundle, where the "hidden dimensions" of the manifold G/H appear both in the base space E and in the fiber G. The group G acts both on the base space and the bundle space, and therefore the results obtained in Sec. 6 of the Mayer-Trautman article in this volume apply. The connection on P is pulled back into a connection on R, and both this connection and its curvature acquire extra components, since they are now defined on a larger base space. Let us denote by script letters the pullbacks to E of the connection and curvature on R in a local trivialization determined by a section s:UC E + R:

 $A = s^{H}p^{H}\omega$, $F = s^{H}p^{H}\Omega$

(3.1)

where ω and Ω are the connection and curvature on P, and s"p" denote their pullback to R pulled down to E by s (this symbolic notation can be interpreted easily in terms of local bases, which we leave as an exercise for the reader). If G/H is k-dimensional, then A is a G-valued K=4 one-form on the 4 + k-dimensional manifold E, and F is a G-valued two-form. Thus A can be thought of as a set of 78 4 + k matrices, and F as a set of (4 + k)(3 + k)/2 28 15 matrices. Moreover, one can choose in the Lie algebra G a basis adapted to the splitting G = H + M, dim G = n, n=28 dim H = m, dim M = n - m = k. Clearly, the physical surviving components of A and F, which we will denote by A and F, respectively, are a one-form and two form on M with values in H, and the remaining components will be subjected to symmetry and gauge transformations, thus reducing the Yang-Mills action on E to a Yang-Mills-Ginzburg-Landau action on M!

Consider the Yang-Mills action on R (numerical factors are omitted)

 $S_{\rm YM} = \int Tr (F \wedge \#F)$,

(3.2)

where the trace is the Killing-Cartan trace on G, and the Hodge-dual is taken on the oriented Riemannian manifold E. (This presupposes a fiber metric on G/H, which is the same as the h of the preceding section; it should be recalled that F is a two-form, hence "F is a (2 + k)-form, and the integrand is a (4 + k)-form, as it should be.) The connection

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and its curvature are clearly invariant under the action of G on the base space E, hence we can apply Eqs.(6.15) and (6.18) of Mayer-Trautman (p.433 this volume). We can obviously split the curvature F into components along M 4^{-3} (spacetime) and those along directions tangent to G/H. 4^{-3} We denote the former components by F₁₁ and the latter by F₂₂, whereas the mixed components (one along M, the other along G/H) will be denoted by F₁₂; the Hodge-dual can be reexpressed in terms of the corresponding contravariant components. Then the integrand of (3.2) becomes

$$\operatorname{Tr}\left(F_{11}F^{11} + 2F_{12}F^{12} + F_{22}F^{22}\right) \quad . \tag{3.3}$$

Exploiting the invariance of the connection with respect to transformations in the ?-directions, i.e., assuming the vector fields X, Y in Eqs.(6.15) and (6.18) in Mayer-Trautman to be along G/H, the components $F_{1?}$ can be expressed as the $D_1 \Phi(?)$, where $\Phi(?)$ is the Lie-algebravalued O-form corresponding to the invariance of A with respect to the vector field ?, in the G/H direction of E. Thus, the middle term in Eq.(3.3) becomes, symbolically,

Tr [D, 0(?) D 0 (?) ,

(3.4)

where the summation is over the repeated symbols !, ?. The first term in (3.3), after integration over the homogeneous spaces G/H and reduction to the Lie-algebra H, becomes the Yang-Mills action for the reduced Yang-Mills theory on Q. Finally, in order to handle the third term, which involves the contraction $F_{??}$ of F with two vector fields lying along G/H, we make use of the equation (6.18) in Mayer-Trautman, which becomes:

 $2F_{22} = [\phi(2), \phi(2)] - \phi([2, 2]) , \qquad (3.5)$

with the obvious meaning for the bracket of two?. Thus, the third term in Eq.(3.3) reduces to what is essentially

a Ginzburg-Landau polynomial in the components of 4:

$$TrF_{??}F^{??} = \frac{1}{4}Tr([\phi,\phi]-\phi)^2, \qquad (3.6)$$

where the square means contraction in the appropriate vector field directions with the metric h on G/H. As was pointed out by Professor O'Raifeartaigh, it is necessary to analyze the expression (3.6) more carefully, since the presence of the brackets may in some cases lead to instability problems. However, special cases which were considered show that Eq. (3.6) has indeed the properties required of a Ginzburg-Landau-Higgs potential, and moreover the relative signs of the quartic and quadratic terms are correct, and only one overall normalization constant (rather than the two which are usual in the expression (1.2)) is needed.

There remains, of course, the problem of how to introduce spinors into a model of this type, and how to couple the spinors to the new fields ϕ which have been introduced. There are two obvious ways in which spinors can be handled in this context, neither of which leads to satisfactory results in physical contexts. The first is to treat the spinors as tensor products of four dimensional spinors with objects behaving trivially on G/H. The second is to introduce spinors on E (i.e., objects transforming under the group Spin (4 + k)), and then carry out the reduction. k=4 Spin (8)

FOUNDATIONS OF DIFFERENTIAL GEOMETRY

VOLUME I

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we have $\dot{u}_t = \varphi_t(X_{u_0})$ and hence $\omega(\dot{u}_t) = \omega(X_{u_0}) = A$, since the connection form ω is invariant by φ_t . Thus we obtain $a_t^{-1}\dot{a}_t = A$. QED.

Let K be a Lie group acting on a principal fibre bundle P(M, G) as a group of automorphisms. Let u_0 be an arbitrary point of P which we choose as a reference point. Every element of K induces a transformation of M in a natural manner. The set J of all elements of K which fix the point $x_0 = \pi(u_0)$ of M forms a closed subgroup of K, called the isotropy subgroup of K at x_0 . We define a homomorphism $\lambda: J \to G$ as follows. For each $j \in J$, ju_0 is a point in the same fibre as u_0 and hence is of the form $ju_0 = u_0 a$ with some $a \in G$. We define $\lambda(j) = a$. If $j, j' \in J$, then $u_0\lambda(jj') = (jj')u_0 = j(u_0\lambda(j')) = (ju_0)\lambda(j')$

$$= (u_0\lambda(j))\lambda(j') = u_0(\lambda(j)\lambda(j')).$$

Hence, $\lambda(jj') = \lambda(j)\lambda(j')$, which shows that $\lambda: J \to G$ is a homomorphism. It is also easy to check that λ is differentiable. The induced Lie algebra homomorphism $j \to g$ will be also denoted by the same λ . Note that λ depends on the choice of u_0 ; the reference point u_0 is chosen once for all and is fixed throughout this section.

PROPOSITION 11.3. Let K be a group of automorphisms of P(M, G)and Γ a connection in P invariant by K. We define a linear mapping $\Lambda: \mathfrak{t} \to \mathfrak{g}$ by $\Lambda(X) = \omega_{\mu}(\tilde{X}), \quad X \in \mathfrak{t},$

where \tilde{X} is the vector field on P induced by X. Then

- (1) $\Lambda(X) = \lambda(X)$ for $X \in j$;
- (2) $\Lambda(\mathrm{ad}(j)(X)) = \mathrm{ad}(\lambda(j))(\Lambda(X))$ for $j \in J$ and $X \in \mathfrak{l}$,

where ad (j) is the adjoint representation of J in \mathfrak{t} and ad $(\lambda(j))$ is that of G in g.

Note that the geometric meaning of $\Lambda(X)$ is given by Proposition 11.2.

Proof. (1) We apply Proposition 11.2 to the 1-parameter subgroup φ_t of K generated by X. If $X \epsilon_i$, then the curve $x_t = \pi(\varphi_t(u_0))$ reduces to a single point $x_0 = \pi(u_0)$. Hence we have $\varphi_t(u_0) = u_0 \lambda(\varphi_t)$. Comparing the tangent vectors of the orbits $\varphi_t(u_0)$ and $u_0 \lambda(\varphi_t)$ at u_0 , we obtain $\Lambda(X) = \lambda(X)$. (2) Let $X \in \mathfrak{f}$ and $j \in J$. We set $Y = \mathrm{ad}(j)(X)$. Then Y generates the 1-parameter subgroup $j\varphi_t j^{-1}$ which maps u_0 into $j\varphi_t j^{-1}(u_0) = j\varphi_t(u_0\lambda(j^{-1})) = j(R_{\lambda(j^{-1})}\varphi_t u_0)$. It follows that $\tilde{Y}_{u_0} = j(R_{\lambda(j^{-1})}\tilde{X}_{u_0})$. Since the connection form ω is invariant by j, we have

PROPOSITION 11.4. With the notation of Proposition 11.3, the curvature form Ω of Γ satisfies the following condition:

$$2\Omega_{u_{\epsilon}}(\tilde{X}, \tilde{Y}) = [\Lambda(X), \Lambda(Y)] - \Lambda([X, Y]) \quad for X, Y \in \mathfrak{k}.$$

Proof. From the structure equation (Theorem 5.2) and Proposition 3.11 of Chapter I, we obtain

$$\begin{aligned} 2\Omega(\tilde{X}, \, \tilde{Y}) &= 2d\omega(\tilde{X}, \, \tilde{Y}) \,+\, [\omega(\tilde{X}), \, \omega(\tilde{Y})] \\ &= \tilde{X}(\omega(\tilde{Y})) \,-\, \tilde{Y}(\omega(\tilde{X})) \,-\, \omega([\tilde{X}, \, \tilde{Y}]) \,+\, [\omega(\tilde{X}), \, \omega(\tilde{Y})]. \end{aligned}$$

Since ω is invariant by K, we have by (c) of Proposition 3.2 of Chapter I (cf. also Proposition 3.5 of Chapter I)

$$\begin{split} \tilde{X}(\omega(\tilde{Y})) &- \omega([\tilde{X}, \tilde{Y}]) = (L_{\tilde{X}}\omega)(\tilde{Y}) = 0, \\ \tilde{Y}(\omega(\tilde{X})) &- \omega([\tilde{Y}, \tilde{X}]) = (L_{\tilde{Y}}\omega)(\tilde{X}) = 0. \end{split}$$

On the other hand, $X \to \hat{X}$ being a Lie algebra homomorphism, we have

$$\omega_{u_0}([\bar{X}, \bar{Y}]) = \Lambda([X, Y]).$$

Thus we obtain

$$2\Omega_{u_0}(\tilde{X}, \tilde{Y}) = [\omega_{u_0}(\tilde{X}), \omega_{u_0}(\tilde{Y})] - \Lambda([X, Y])$$

= $[\Lambda(X), \Lambda(Y)] - \Lambda([X, Y]).$
QED.

We say that K acts fibre-transitively on P if, for any two fibres of P, there is an element of K which maps one fibre into the other, that is, if the action of K on the base M is transitive. If J is the isotropy subgroup of K at $x_0 = \pi(u_0)$ as above, then M is the homogeneous space K/J.

The following result is due to Wang [1].

THEOREM 11.5. If a connected Lie group K is a fibre-transitive automorphism group of a bundle P(M, G) and if J is the isotropy subgroup of

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K at $x_0 = \pi(u_0)$, then there is a 1:1 correspondence between the set of Kinvariant connections in P and the set of linear mappings $\Lambda: \mathfrak{t} \to \mathfrak{g}$ which satisfies the two conditions in Proposition 11.3; the correspondence is given by

$$\Lambda(X) = \omega_{u_0}(\hat{X}) \qquad for \ X \in \mathfrak{k},$$

where X is the vector field on P induced by X.

Proof. In view of Proposition 11.3, it is sufficient to show that, for every $\Lambda: \mathfrak{t} \to \mathfrak{g}$ satisfying (1) and (2) of Proposition 11.3, there is a K-invariant connection form ω on P such that $\Lambda(X) = \omega_{u_0}(\tilde{X})$ for $X \in \mathfrak{t}$. Let $X^* \in T_u(P)$. Since K is fibre-transitive, we can write

$$u_0 = kua = k \circ R_a u$$
$$k \circ R_a X^* = \tilde{X}_{u_0} + A^*_{u_0},$$

where $k \in K$, $a \in G$, $X \in k$ and A^* is the fundamental vector field corresponding to $A \in g$. We then set

$$\omega(X^*) = \operatorname{ad} (a)(\Lambda(X) + A).$$

We first prove that $\omega(X^*)$ is independent of the choice of X and A. Let

 $\tilde{X}_{u_0} + A^*_{u_0} = \tilde{Y}_{u_0} + B^*_{u_0}$, where $Y \in \mathfrak{t}$ and $B \in \mathfrak{g}$,

so that $\tilde{X}_{u_0} - \tilde{Y}_{u_0} = B^*_{u_0} - A^*_{u_0}$. From the definition of $\lambda: j \to g$, it follows that $\lambda(X - Y) = B - A$. By condition (1) of Proposition 11.3, we have $\lambda(X - Y) = \Lambda(X - Y) = \Lambda(X) - \Lambda(Y)$. Hence, $\Lambda(X) + A = \Lambda(Y) + B$.

We next prove that $\omega(X^*)$ is independent of the choice of k and a. Let

$$u_0 = kua = k_1 ua_1$$
 $(k_1 \in K \text{ and } a_1 \in G),$

so that $k_1k^{-1}u_0 = u_0a_1^{-1}a$ and $k_1k^{-1} \in J$. We set $j = k_1k^{-1}$. Then $\lambda(j) = a_1^{-1}a$. We have

$$\begin{aligned} k_1 \circ R_{a_1} X^* &= jk \circ R_{a\lambda(j^{-1})} X^* \\ &= j \circ R_{\lambda(j^{-1})} (k \circ R_a X^*) = j \circ R_{\lambda(j^{-1})} (\tilde{X}_{u_0} + A^*_{u_0}). \end{aligned}$$

By Proposition 1.7 of Chapter I, we have

$$j \circ R_{\lambda(j^{-1})}(\tilde{X}_{u_0}) = j(\tilde{X}_{u_0\lambda(j^{-1})}) = \tilde{Z}_{u_0}, \quad \text{where } Z = \mathrm{ad}\;(j)(X).$$

By Proposition 5.1 of Chapter I, we have

 $j \circ R_{\lambda(j^{-1})}(A_{u_0}^*) = R_{\lambda(j^{-1})}(jA_{u_0}^*) = R_{\lambda(j^{-1})}A_{ju_0}^* = R_{\lambda(j^{-1})}A_{u_0\lambda(j)}^* = C_{u_0}^*,$ where $C = \text{ad} (\lambda(j))(A)$. Hence we have

$$k_1 \circ R_{a_1} X^* = \tilde{Z}_{u_0} + C_{u_0}^*,$$

ad $(a_1)(\Lambda(Z) + C) = \operatorname{ad} (a_1)(\Lambda(\operatorname{ad} (j)(X)) + \operatorname{ad} (\lambda(j))A)$
 $= \operatorname{ad} (a_1)[\operatorname{ad} (\lambda(j))(\Lambda(X) + A)]$
 $= \operatorname{ad} (a)(\Lambda(X) + A).$

This proves our assertion that $\omega(X^*)$ depends only on X^* .

We now prove that ω is a connection form. Let $X^* \in T_u(P)$ and $u_0 = kua$ as above. Let b be an arbitrary element of G. We set

 $Y^* = R_b X^* \epsilon T_v(P), \quad \text{where } v = ub,$

so that $u_0 = kub(b^{-1}a) = kv(b^{-1}a)$. We then have

$$k \circ R_{b^{-1}a}Y^* = k \circ R_{b^{-1}a}R_bX^* = k \circ R_aX^* = (\hat{X}_{u_0} + A_{u_0}^*)$$

and hence

$$\omega(R_bX^*) = \omega(Y^*) = \mathrm{ad} \ (b^{-1}a)(\Lambda(X) + A) = \mathrm{ad} \ (b^{-1})(\omega(X^*)),$$

which shows that ω satisfies condition (b') of Proposition 1.1. Now, let A be any element of g and let $u_0 = kua$. Then

$$k \circ R_a(A_u^*) = R_a \circ k(A_u^*) = R_a(A_{ku}^*) = B_{u_a}^*$$
, where $B = ad(a^{-1})(A)$.

Hence we have

$$\omega(A_u^*) = \mathrm{ad} \ (a)(B) = A,$$

which shows that ω satisfies condition (a') of Proposition 1.1.

To prove that ω is differentiable, let u_1 be an arbitrary point of P and let $u_0 = k_1 u_1 a_1$. Consider the fibre bundle K(M, J), where M = K/J. Let $\sigma: U \to K$ be a local cross section of this bundle defined in a neighborhood U of $\pi(u_1)$ such that $\sigma(\pi(u_1)) = k_1$. For each $u \in \pi^{-1}(U)$, we define $k \in K$ and $a \in G$ by

$$k = \sigma(\pi(u))$$
 and $u_0 = kua$.

Then both k and a depend differentiably on u. We decompose the vector space f into a direct sum of subspaces: f = j + m. For an

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arbitrary $X^* \in T_u(P)$, we set

 $k \circ R_a(X^*) = \tilde{X}_{u_0} + A^*_{u_0}, \quad \text{where } X \in \mathfrak{m}.$

Then both X and A are uniquely determined and depend differentiably on X^{*}. Thus $\omega(X^*) = \operatorname{ad} (a)(\Lambda(X) + A)$ depends differentiably on X^{*}.

Finally, we prove that ω is invariant by K. Let $X^* \in T_u(P)$ and $u_0 = kua$. Let k_1 be an arbitrary element of K. Then $k_1X^* \in T_{k_1u}(P)$ and $u_0 = kk_1^{-1}(k_1u)a$. Hence,

$$kk_1^{-1} \circ R_a(k_1X^*) = k \circ R_a(X^*).$$

From the construction of ω , we see immediately that $\omega(k_1X^*) = \omega(X^*)$. QED.

In the case where K is fibre-transitive on P, the curvature form Ω , which is a tensorial form of type ad G (cf. §5) and is invariant by K, is completely determined by the values $\Omega_{u_0}(\tilde{X}, \tilde{Y}), X, Y \in \mathfrak{k}$. Proposition 11.4 expresses $\Omega_{u_0}(\tilde{X}, \tilde{Y})$ in terms of Λ . As a consequence of Proposition 11.4 and Theorem 11.5, we obtain

COROLLARY 11.6. The K-invariant connection in P defined by Λ is flat if and only if $\Lambda: \mathfrak{t} \to \mathfrak{g}$ is a Lie algebra homomorphism.

Proof. A connection is flat if and only if its curvature form vanishes identically (Theorem 9.1). QED.

THEOREM 11.7. Assume in Theorem 11.5 that \mathfrak{t} admits a subspace \mathfrak{m} such that $\mathfrak{t} = \mathfrak{j} + \mathfrak{m}$ (direct sum) and $\mathfrak{ad}(J)(\mathfrak{m}) = \mathfrak{m}$, where $\mathfrak{ad}(J)$ is the adjoint representation of J in \mathfrak{t} . Then

(1) There is a 1:1 correspondence between the set of K-invariant connections in P and the set of linear mappings Λ_m : $m \rightarrow g$ such that

 $\Lambda_{\mathfrak{m}}(\mathrm{ad}\;(j)(X)) = \mathrm{ad}\;(\lambda(j))(\Lambda_{\mathfrak{m}}(X)) \quad \text{for } X \in \mathfrak{m} \quad and \quad j \in J;$ the correspondence is given via Theorem 11.5 by

$$\Lambda(X) = \begin{cases} \lambda(X) & \text{if } X \epsilon j, \\ \Lambda_{\mathfrak{m}}(X) & \text{if } X \epsilon \mathfrak{m}. \end{cases}$$

(2) The curvature form Ω of the K-invariant connection defined by Λ_m satisfies the following condition:

$$2\Omega_{u_0}(\tilde{X}, \tilde{Y}) = [\Lambda_{\mathfrak{m}}(X), \Lambda_{\mathfrak{m}}(Y)] - \Lambda_{\mathfrak{m}}([X, Y]_{\mathfrak{m}}) - \lambda([X, Y]_{\mathfrak{l}})$$
for X, Y ϵ m,

Appendix - Higgs as Primitive Idempotent

By identifying the Higgs with Primitive Idempotents of the CI(8) real Clifford algebra, the Higgs is not seen as a simple-minded fundamental scalar particle, but rather the Higgs is seen as a quantum process that creates a fermionic condensate with which it interacts to make the fermions appear massive. The Primitive Idempotent Higgs is part of my E8 Physics model in terms of which the Primitive Idempotent Higgs is seen to do all the nice things that the fundamental scalar particle Higgs needs to do, and to be effectively a Higgs-Tquark system with 3 mass states.

The conventional Standard Model has structure: spacetime is a base manifold; particles are representations of gauge groups gauge bosons are in the adjoint representation fermions are in other representations (analagous to spinor) Higgs boson is in scalar representation.

E8 Physics (see vixra 1108.0027 and tony5m17h.net) has structure (from 248-dim E8 = 120-dim adjoint D8 + 128-dim half-spinor D8): spacetime is in the adjoint D8 part of E8 (64 of 120 D8 adjoints) gauge bosons are in the adjoint D8 part of E8 (56 of the 120 D8 adjoints) fermions are in the half-spinor D8 part of E8 (64+64 of the 128 D8 half-spinors.

There is no room for a fundamental Higgs in the E8 of E8 Physics.

However,

Cl(8)

for E8 Physics to include the observed results of the Standard Model it must have something that acts like the Standard Model Higgs even though it will NOT be a fundamental particle.

To see how the E8 Physics Higgs works, embed E8 into the 256-dimensional real Clifford algebra Cl(8):

16 = 1	+ 6	+ 1
	+ 8	
	16 = 1	

E8 Root Vectors 240 = 8 + 28 + 56 + 56 + 56 + 28 + 8

The Cl(8) Primitive Idempotent is 16-dimensional and can be decomposed into two 8-dimensional half-spinor parts each of which is related by Triality to 8-dimensional spacetime and has Octonionic structure. In that decomposition: the 1+6+1 = (1+3)+(3+1) is related to two copies of a 4-dimensional Associative Quaternionic subspace of the Octonionic structure

256 = 1 + 8 + 28 + 56 + 70 + 56 + 28 + 8 + 1

and

the 8 = 4+4 is related to two copies of a 4-dimensional Co-Associative subspace of the Octonionic structure (see the book "Spinors and Calibrations" by F. Reese Harvey)

The 8 = 4+4 Co-Associative part of the Cl(8) Primitive Idempotent when combined with the 240 E8 Root Vectors forms the full 248-dimensional E8.

It represents a Cartan subalgebra of the E8 Lie algebra.

The (1+3)+(3+1) Associative part of the Cl(8) Primitive Idempotent is the Higgs of E8 Physics.

The half-spinors generated by the E8 Higgs part of the CI(8) Primitive Idempotent represent:

neutrino; red, green, blue down quarks; red, green, blue up quarks; electron so

the E8 Higgs effectively creates/annihilates the fundamental fermions and the E8 Higgs is effectively a condensate of fundamental fermions.

In E8 Physics the high-energy 8-dimensional Octonionic spacetime reduces, by freezing out a preferred 4-dim Associative Quaternionic subspace, to a 4+4 -dimensional Batakis Kaluza-Klein of the form M4 x CP2 with 4-dim M4 physical spacetime.

Since the (1+3)+(3+1) part of the Cl(8) Primitive Idempotent includes the Cl(8) grade-0 scalar 1

and 3+3 = 6 of the Cl(8) grade-4 which act as pseudoscalars for 4-dim spacetime and the Cl(8) grade-8 pseudoscalar 1

the E8 Higgs transforms with respect to 4-dim spacetime as a scalar (or pseudoscalar) and in that respect is similar to Standard Model Higgs.

Not only does the E8 Higgs fermion condensate transform with respect to 4-dim physical spacetime like the Standard Model Higgs but

the geometry of the reduction from 8-dim Octonionic spacetime to 4+4 -dimensional Batakis Kaluza-Klein, by the Mayer mechanism, gives E8 Higgs the ElectroWeak Symmetry-Breaking Ginzburg-Landau structure.

Since the second and third fermion generations emerge dynamically from the reduction from 8-dim to 4+4 -dim Kaluza-Klein, they are also created/annihilated by the Primitive Idempotent E8 Higgs and are present in the fermion condensate. Since the Truth Quark is so much more massive that the other fermions,

the E8 Higgs is effectively a Truth Quark condensate. When Triviality and Vacuum Stability are taken into account,

the E8 Higgs and Truth Quark system has 3 mass states.

Appendix - Joy Christian Correlations

Bell's Theorem

on Quantum Correlations is based on the Hopf Fibration RP1 -> S1 -> S0 = $\{-1,+1\}$.

Joy Christian has shown that it is more realistic

to base Quantum Correlations on the Hopf Fibrations

S1 -> S3 -> S2 = CP1 and S3 -> S7 -> S4 = QP1 and S7 -> S15 -> S8 = OP1 where R, C, Q, and O are Real, Complex, Quaternion, and Octonion Division Algebras.

In his book "Disproof of Bell's Theorem" (BrownWalker Press, 2nd ed, 2014) Joy Christian said:

"... Every quantum mechanical correlation can be understood as

a classical, local-realistic correlation among a set of points of a parallelized 7-sphere

physical space ... respects the symmetries and topologies of a parallelized 7-sphere ...

because 7-sphere ...[is]... homeomorphic to the ...[Octonion]... division algebra ... it is the property of division that[is]... responsible for ... local causality in the world

•••

To understand this reasoning better, recall that, just as a parallelized 3-sphere is a 2-sphere worth of 1-spheres but with a twist in the manifold S3 (=/= S2xS1),

a parallelized 7-sphere is a 4-sphere worth of 3-spheres

but with a twist in the manifold S7 (=/= S4xS3)

... just as S3 is

a nontrivial fiber bundle over S2 with Clifford parallels S1 as its linked fibers, S7 is also

a nontrivial fiber bundle ... over S4 ... with ... spheres S3 as its linked fibers.

it is the twist in the bundle S3 that forces one

to forgo the commutativity of complex numbers (corresponding to the circles S1) in favor of the non-commutativity of quaternions.

In other words, a 3-sphere is not parallelizable by the commuting complex numbers but only by the non-commuting quaternions. And it is this noncommutativity that gives rise to the non-vanishing of the torsion in our physical space.

In a similar vein, the twist in the bundle S7 (=/= S4xS3) forces one to forgo the associativity of quaternions (corresponding to the fibers) in favor of the non-associativity of octonions.

In other words, a 7-sphere is not parallelizable by the associative quaternions but only by the non-associative octonions.

... it can be parallelized ... because its tangent bundle happens to be trivial: Once parallelized by a set of unit octonions,

both the 7-sphere and each of its 3-spherical fibers remain closed under multiplication. This, in turn, means that the factorizability or locality condition of Bell is ... satisfied within a parallelized 7-sphere. The lack of associativity of octonions, however, entails that, unlike the unit 3-sphere [which is homeomorphic to the ... group SU(2)], a 7-sphere is not a group manifold ... the torsion within the 7-sphere ... varies from one point to another of the manifold. It is this variability of the parallelizing torsion within that is ultimately responsible for the diversity and non-linearity of the quantum correlations we observe in nature ...".

The 7-sphere S7 is the unit sphere in 8-dim space. S7 is not a Lie algebra, but is a Malcev algebra and is naturally embedded in the D4 Lie algebra Spin(8) which is topologically composed of (but =/= the simple product S7 x S7 x G2) 2 copies of S7 and 14-dim Lie Algebra G2 of the Octonion Automorphism Group.

28-dim D4 Lie algebra Spin(8) can be represented by 8x8 antisymmetric real matrices It is a subalgebra of 63-dim A7 Lie Algebra SL(8,R) of all 8x8 real matrices with det = 1.

Unimodular SL(8,R) is the non-compact Lie algebra corresponding to SU(8).

SL(8,R) effectively describes the 8-dim SpaceTime of E8 Physics

as a generalized checkerboard of SpaceTime HyperVolume Elements.

Anderson and Finkelstein in Am . J. Phys. 39 (1971) 901-904 said:

"... Unimodular relativity ... expresses the existence of a fundamental element of spacetime hypervolume at every point. ...".

From the Real Clifford Algebra Cl(16) and 8-Periodicity

64-dim R+SL(8,R) appears from factoring Cl(16) = tensor product Cl(8)xCl(8)

as the tensor product of the 8-dim vector spaces 8v of each of the Cl(8) factors so that 64-dim R+SL(8,R) = $8v \times 8v$

If you regard the two CI(8) as Fourier duals then

one 8v describes 8-dim Spacetime Position and the other 8v describes its Momentum.

David Brown, in May 2012 comments on scottaaronson.com blog, said:

"... Where did Bell go wrong? Bell used quantum SU(1) states

whereas Christian correctly uses quantum SU(8) states ...[from]...

Christian's parallelized 7-sphere model. ...

Every quantum mechanical Christian SU(8) correlation can be understood

as a realistic, non-local Christian SU(8) correlations among a set of points

of a parallelized 7-sphere ... More importantly, if Christian's theory of local realism is true then SU(8) should be the gauge group for physical reality ...".

SU(8) is the compact version of SL(8,R), so it seems to me that it is David Brown's idea, possibly motivated by SU(8) and SL(8,R) in E7 of D = 4 N = 8 supergravity models, that **Joy Christian's S7 Quantum Correlations have fundamental SL(8,R) structure**.

Rutwig Campoamor-Stursberg in Acta Physica Polonica B 41 (2010) 53-77, "Contractions of Exceptional Lie Algebras and SemiDirect Products", showed that SL(8,R) appears in the E8 Maximal Contraction = semi-direct product H92 x SL(8,R) where

H92 is (8+28+56 +1+ 56+28+8)-dim Heisenberg Creation/Annihilation Algebra

so that H92 x SL(8,R) has 7-graded structure:

grade -3 = Creation of 1 fermion (tree-level massless neutrino) with 8 SpaceTime Components for a total of 8 fermion component creators (related to SpaceTime by Triality)

grade -2 =Creation of 8+3+1 = 12 Bosons for Standard Model and 16 Conformal U(2,2) Bosons for MacDowell-Mansouri Gravity for a total of 28 Boson creators

grade -1 = Creation of 7 massive Dirac fermion each with 8 SpaceTime Components for a total of 56 fermion component creators

grade 0 = 1 + SL(8) = 1+63 = 64-dim representing 8-dim SpaceTime of HyperVolume Elements

grade 1 = Annihilation of 7 massive Dirac fermions each with 8 SpaceTime Components for a total of 56 fermion component annihilators

grade 2 = Annihilation of 8+3+1 = 12 Bosons for Standard Model and 16 Conformal U(2,2) Bosons for MacDowell-Mansouri Gravity for a total of 28 Boson annihilators

grade 3 = Annilation of 1 fermion (tree-level massless neutrino) with 8 SpaceTime Components for a total of 8 fermion component annihilators (related to SpaceTime by Triality)

Here is how Physics Structures expand from Joy Christian's S7 to E8 Physics:

7-dim S7 - Lie Algebra -> 28-dim Spin(8)

28-dim Spin(8) - Full 8x8 Matrix -> 63-dim SL(8,R)

63-dim SL(8,R) - Creation/Annihilation -> 248-dim H92xSL(8,R)

248-dim H92xSL(8,R) - Expansion -> 248-dim E8

The E8 expansion of H92 x SL(8,R) has physical interpretation leading to a Local Classical Lagrangian with Base Manifold Spacetime, Gravity + Standard Model Gauge Boson terms, and Fermion terms for 8-dim spacetime and First-Generation Fermions (with 4+4 dim Kaluza-Klein and Second and Third Fermion Generations emerging with Octonionic Symmetry being broken to Quaternionic) :

248-dim E8 = 120-dim D8 + 128-dim half-spinors of D8

In Symmetric Space terms:

E8 / D8 = (64+64)-dim (OxO)P2 Octo-Octonionic Projective Plane 64 = 8 components of 8 fermion particles 64 = 8 components of 8 fermion antiparticles

D8 / D4xD4 = 64-dim = 8 position coordinates x 8 momentum coordinates

one D4 = 28 = 12 Standard Model Ghosts + 16 Conformal Gravity Gauge Bosons (4 of the 16 are not in the 240 E8 root vectors, but are in its 8-dim Cartan subalgebra)

other D4 = 28 = 16 ConformalGravity Ghosts + 12 Standard Model Gauge Bosons (4 of the 12 are not in the 240 E8 root vectors, but are in its 8-dim Cartan subalgebra)

My E8 Physics model (viXra 1405.0030 vG) was initially inspired back in the 1980s by D = 4, N = 8 supergravity models.

Yoshiaki Tanii in his book "Introduction to Supergravity" (Springer 2014) said: "... Poincare supergravity constructed in the highest spacetime dimension is D = 11, N = 1 theory ... the low energy effective theory of M theory ... D = 11 supergravity has AdS4 x S7 spacetime ... This ... corresponds to the AdS4 solution of D = 4, N = 8 gauged supergravity ... D = 4, N = 8 gauged supergravity is ... related to a compactification of D = 11 supergravity ... by a seven-dimensional sphere S7 ... N = 8 supergravity ... the maximal supergravity ...[has]... multiplets ... 1 8 28 56 70 56 28 8 1 ... D = 4, N = 8 Supergravity ... has global E7(+7) and local SU(8) symmetries. ...".

Supergravity itself did not quite work for me. In hindsight,

D = 4, N = 8 maximal global symmetry is only E7 with maximal compact SU(8)

(noncompact version of SU(8) is SL(8,R) which is only part of the maximal contraction of E8) and the supergravity with maximal global symmetry E8 with maximal compact D8

is D = 3, N = 8 whose spacetime is only 3-dimensional. (Samtleben, arXiv 0808.4076).

The S7 led me to work with Spin(8) which is the bivector Lie algebra of the Real Clifford Algebra Cl(8) with graded structure 1 8 28 56 70 56 28 8 1 When Spin(8) seemed too small, I went to F4 which contained Spin(8) for Gauge Bosons, Spin(9) / Spin(8) for 8-dim SpaceTime, and F4 / Spin(9) for 8 fermion particles + 8 fermion antiparticles. When F4 failed to have desired complex structure, I went to E6. When E6 failed to have all the necessary fermion components and gauge boson ghosts, I went to E8 and found the E8 Physics model that as of now seems to be realistic.

How does Bell-Christian-Brown SL(8,R) Quantum Theory fit with the Bohm Quantum Potential of E8 Physics (<u>http://vixra.org/pdf/1405.0030vG.pdf</u>)?

Comparison of Bohm's Quantum Potential hidden variable "lambdas" with Bell's "lambdas" and Joy Christian's (arxiv 0904.4259)"lambdas": Peter Holland, in his book "The Quantum Theory of Motion, an Account of the de Broglie - Bohm Causal Interpretation of Quantum Mechanics" (Cambridge 1993) said:

"... 11.5.1 Bell's Inequality ... In discussing the EPR spin experiment Bell supposed that the results of the two spin measurements are determined completely by a set of hidden variables lambda and made two assumptions which he claimed should be satisfied by a local hidden-variables theory: (i) The result A of measuring sigma1 . a on particle 1 is determined solely by a and lambda, and the result B of measuring sigma2 . b on particle 2 is determined solely by b and lambda , where a and b are unit vectors with a . b = cos(delta).

Thus A = A(a, lambda) = +/- 1 and B = B(b, lambda) = +/- 1

Possibilities such as A = A(a, b, lambda) and B = B(a, b, lambda) are excluded.

(ii) The normalized probability distribution of the hidden variables depends only on lambda : rho = rho(lambda).

Possibilities such as rho = rho(lambda , a , b) are excluded.

•••

We now consider to what extent assumptions (i) and (ii) are valid in the causal [Bohm Potential] interpretation ... The hidden variables are then the particle positions x1, x2 (the internal orientation spin vectors s1, s2 along the trajectories are determined by the positions and the wavefunction ...) ... the eventual results ... for each of sz1 and sz2 is determined by the intial positions of both particles and by delta, i.e., A = A(x1, x2, a.b),

B = B(x1, x2, a.b) Thus assumption (i) is not valid ...

Neither is assumption (ii) satisfied. ...

In reproducing ... the quantum mechanical correlation function ...

Ppsi(a, b) = ... = - cos(delta) ... the causal [Bohm Potential] interpretation disobeys both of Bell's basic assumptions. ...".

So, Bell's "lambdas" obey (i) and (ii) and so obey Bell's inequality and

Bohm's "lambdas" violate (i) and (ii) and so violate Bell's Inequality but obey the quantum experimentally observed correlation function.

Joy Christian (see arxiv 0904.4259) explicitly violates (i) by replacing A = A(a, lambda) = +/- 1 and B = B(b, lambda) = +/- 1 with A = A(a, lambda) in S2 and B = B(b, lambda) in S2.

However, Joy does not violate (ii). Joy says: "... once the state lambda is specified and the two particles have separated, measurements of A can depend only on lambda and a, but not b, and likewise measurements of B can depend only on lambda and b, but not a ...[compare the (ii)-violation by Bohm's lamdbas as stated above]... Assuming ... that the distribution rho(lambda) is normalized on the space \land , .we finally arrive at the inequalities ... exactly what is predicted by quantum mechanics ... we have been able to derive these results without specifying what the complete state lambda is or the distribution rho(lambda) is, and without employing any averaging procedure ... the correlations [for the examples of 0904.4259] ... are simply the local, realistic, and deterministic correlations among certain points of ... S3 and S7 ... This implies that the violations of Bell inequalities ... have nothing to do with quantum mechanics per se ...".

So, even though Joy's lambdas do not violate (ii), when Joy "... derive[s] ... the exact quantum mechanical expectation value ... - a . b " Joy's result is consistent with that of Bohm's "lambdas".

Joy's "lambdas" are classical and local (in Joy's sense).

Bohm's "lambdas" are quantum and, since Joy does not change Bell's (ii), nonlocal (in Joy's sense).

Joy's "lambdas" and Bohm's "lambdas" are consistent with each other with respect to their calculated quantum expectation values.

Could Joy's "lambdas" be considered as a Classical Limit of Bohm's "lambdas" ?

Consider again Peter Holland's book in which he says:

"... 6.9 Remarks on the path integral approach ... Feynman['s] ... route to quantum mechanics ... rests on the trajectory concept and so may be expected to have some connection with the causal [Bohm Potential] formulation. ... Feynman provides a technique for computing ... the transition amplitude (Green function or propagator) ... from the classical Lagrangian ... One considers all the paths ... and associates with each an amplitude ... These tracks are ... called 'classical paths' ... one sums (integrates) over all the paths ... the solution .. is given by ... Huygens' principle ... of all the paths ... one of them will be the actual trajectory pursued by the quantum particle according to the [Bohm Potential] guidance formula ... We shall refer to ... it ... as the 'quantum path' ... For an infinitesimal time interval ... the propagator is just the classical wavefunction ... a finite path may be decomposed into many such infinitesimal steps, the net propagator being obtained by successive applications of Huygens' construction ... We may view the Feynman procedure as a method of obtaining the quantum action from the set of all classical actions. ...".

If Joy Christian's classical "lambdas" are identified with Feynman path Lagrangian / Green function propagators, and if their Huygens' sums can be seen to produce the Bohm "lambdas",

then Joy's work will show a nice smooth classical limit (as opposed to Bell's discordant classical limit) for the Bohm Quantum Potential.

If the Bohm Quantum Potential can then be used as a basis for a construction of a realistic AQFT (Algebraic Quantum Field Theory)

then maybe Joy Christian's work will help show a useful connection (and philosphical reconciliation) between

the Classical Lagrangian physics so useful in detailed understanding of the Standard Model

and

of AQFT along the lines of

generalization of the Hyperfinite II1 von Neumann factor algebra.

Appendix - Details of Conformal Gravity and ratio DE : DM : OM

MacDowell-Mansouri Gravity is described by Rabindra Mohapatra in section 14.6 of his book "Unification and Supersymmetry":

§14.6. Local Conformal Symmetry and Gravity

Before we study supergravity, with the new algebraic approach developed, we would like to discuss how gravitational theory can emerge from the gauging of conformal symmetry. For this purpose we briefly present the general notation for constructing gauge covariant fields. The general procedure is to start with the Lie algebra of generators X_A of a group

$$[X_A, X_B] = f_{AB}^C X_C, \tag{14.6.1}$$

where f_{AB}^{C} are structure constants of the group. We can then introduce a gauge field connection h_{ρ}^{A} as follows:

$$h_{\mu} \equiv h_{\mu}^{A} X_{A}. \qquad (14.6.2)$$

Let us denote the parameter associated with X_A by ε^A . The gauge transformations on the fields h_{ρ}^A are given as follows:

$$\delta h_{\mu}^{A} = \partial_{\mu} \varepsilon^{A} + h_{\mu}^{B} \varepsilon^{C} f_{CB}^{A} \equiv (D_{\mu} \varepsilon)^{A}. \qquad (14.6.3)$$

We can then define a covariant curvature

$$R^A_{\mu\nu} = \partial_\nu h^A_\mu - \partial_\mu h^A_\nu + h^B_\nu h^C_\mu f^A_\mu. \qquad (14.6.4)$$

Under a gauge transformation

$$\delta_{gauge} R^A_{\mu\nu} = R^B_{\mu\nu} \varepsilon^C f^A_{CB}. \qquad (14.6.5)$$

We can then write the general gauge invariant action as follows:

$$I = \int d^4x \ Q^{\mu\nu\rho\sigma}_{AB} R^A_{\mu\nu} R^B_{\rho\sigma}, \qquad (14.6.6)$$

Let us now apply this formalism to conformal gravity. In this case

$$h_{\mu} = P_{\mu}e_{\mu}^{m} + M_{\mu\mu}\omega_{\mu}^{m} + K_{\mu}f_{\mu}^{m} + Db_{\mu}.$$
 (14.6.7)

The various R_s, are

$$\mathcal{K}_{\mu\nu}(P) = \partial_{\nu}e_{\mu}^{m} - \partial_{\mu}e_{\nu}^{m} + \omega_{\mu}^{m\nu}e_{\nu}^{n} - \omega_{\nu}^{m\nu}e_{\mu}^{m} - b_{\mu}e_{\nu}^{m} + b_{\nu}e_{\mu}^{n}, \qquad (14.6.8)$$

$$R_{\mu\nu}(M) = \partial_{\nu}\omega_{\mu}^{mn} - \partial_{\mu}\omega_{\nu}^{mn} - \omega_{\nu}^{mp}\omega_{\mu,p}^{n} - \omega_{\mu}^{mp}\omega_{\nu,p}^{n} - 4(e_{\mu}^{m}f_{\nu}^{n} - e_{\nu}^{n}f_{\mu}^{n}), \quad (14.6.9)$$

$$R_{\mu\nu}(K) = \partial_{\mu}f_{\mu}^{m} - \partial_{\mu}f_{\nu}^{m} - b_{\mu}f_{\nu}^{m} + b_{\nu}f_{\mu}^{m} + \omega_{\mu}^{mn}f_{\nu}^{n} - \omega_{\nu}^{mn}f_{\nu}^{n}$$
(14.6.10)

$$R_{\mu\nu}(D) = \partial_{\nu}b_{\mu} - \partial_{\mu}b_{\nu} + 2e_{\mu}^{m}f_{\nu}^{m} - 2e_{\nu}^{m}f_{\mu}^{m}.$$
(14.6.11)

The gauge invariant Lagrangian for the gravitational field can now be written down, using eqn. (14.6.6), as

$$S = \int d^4x \ \epsilon_{maxs} \epsilon^{\mu\nu\rho\sigma} R^{\mu\alpha}_{\rho\sigma}(M) R^{\nu\sigma}_{\rho\sigma}(M). \tag{14.6.12}$$

We also impose the constraint that

 $R_{\mu\nu}(P) = 0, \tag{14.6.13}$

which expresses ω_{μ}^{m} as a function of (e, b). The reason for imposing this constraint has to do with the fact that P_m transformations must be eventually identified with coordinate transformation. To see this point more explicitly let us consider the vierbein e_{μ}^{m} . Under coordinate transformations

$$\delta_{GC}(\xi^{\gamma})e_{\alpha}^{m} = \partial_{\mu}\xi^{\lambda}e_{\lambda}^{m} + \xi^{\lambda}\partial_{\lambda}e_{\alpha}^{m}. \qquad (14.6.14)$$

Using eqn. (14.6.8) we can rewrite

$$\delta_{\alpha\beta}(\xi^{\nu})e_{\alpha}^{m} = \delta_{P}(\xi e^{\nu})e_{\alpha}^{m} + \delta_{M}(\xi \omega^{mn})e_{\alpha}^{m} + \delta_{D}(\xi b)e_{\alpha}^{m} + \xi^{\nu}R_{\alpha\nu}^{m}(P),$$

where

$$\delta_{\rho}(\xi^{n})e_{\mu}^{m} = \partial_{\mu}\xi^{m} + \xi^{n}\omega_{\mu}^{mn} + \xi^{m}b_{\mu}.$$
 (14.6.15)

If $R^{\mu\nu}(P) = 0$, the general coordinate transformation becomes related to a set of gauge transformations via eqn. (14.6.15).

At this point we also wish to point out how we can define the covariant derivative. In the case of internal symmetries $D_{\mu} = \partial_{\mu} - iX_A h_{\mu}^A$; now since momentum is treated as an internal symmetry we have to give a rule. This follows from eqn. (14.6.15) by writing a redefined translation generator \tilde{P} such that

$$\delta_{\overline{\rho}}(\xi) = \delta_{\overline{\rho}C}(\xi'') - \sum_{A'} \delta_{A'}(\xi^m h_m^A),$$
 (14.6.16)

where A' goes over all gauge transformations excluding translation. The rule is

$$\delta_{\bar{p}}(\xi^{m})\phi = \xi^{m}D_{m}^{C}\phi.$$
 (14.6.17)

We also wish to point out that for fields which carry spin or conformal charge, only the intrinsic parts contribute to D_m^C and the orbital parts do not play any rule.

Coming back to the constraints we can then vary the action with respect to f_a^m to get an expression for it, i.e.,

$$e_r^n f_{am} = -\frac{1}{4} [e_m^A e_m R_{ab}^{am} - \frac{1}{6} g_{av} R], \qquad (14.6.18)$$

where \int_{a}^{m} has been set to zero in R written in the right-hand side.

This eliminates (from the theory the degrees of freedom) ω_s^{nn} and f_s^n and we are left with e_s^n and b_s . Furthermore, these constraints will change the transformation laws for the dependent fields so that the constraints do not change.

Let us now look at the matter coupling to see how the familiar gravity theory emerges from this version. Consider a scalar field ϕ . It has conformal weight $\lambda = 1$. So we can write a convariant derivative for it, eqn. (14.6.17)

$$D_{\mu}^{C}\phi = \partial_{\mu}\phi - \phi b_{\mu}. \qquad (14.6.19)$$

We note that the conformal charge of ϕ can be assumed to be zero since $K_m = x^2 \partial$ and is the dimension of inverse mass. In order to calculate $\Box^c \phi$ we

start with the expression for d'Alambertian in general relativity

$$\frac{1}{e}\hat{\sigma}_{\mu}(g^{\mu\nu}eD^{C}_{\mu}\phi). \qquad (14.6.20)$$

The only transformations we have to compensate for are the conformal transformations and the scale transformations. Since

$$\delta b_{\mu} = -2\xi_{k}^{\mu}e_{m\mu}, \qquad \delta(\phi b_{\mu}) = \phi\delta b_{\mu} = -2\phi f_{\mu}^{m}e_{m}^{\mu} = +\frac{2}{12}\phi R, \qquad (14.6.21)$$

where, in the last step, we have used the constraint equation (14.6.18). Putting all these together we find

$$\Box^{c}\phi = \frac{1}{e}\partial_{r}(g^{\mu\nu}eD^{c}_{\mu}\phi) + b_{\mu}D^{c}_{\mu}\phi + \frac{2}{12}\phi R.$$
(14.6.22)

Thus, the Lagrangian for conformal gravity coupled to matter fields can be written as

$$S = \int e \, d^4 x \, \frac{1}{2} \phi \Box^c \phi. \tag{14.6.23}$$

Now we can use conformal transformation to gauge $b_{\mu} = 0$ and local scale transformation to set $\phi = \kappa^{-1}$ leading to the usual Hilbert action for gravity. To summarize, we start with a Lagrangian invariant under full local conformal symmetry and fix conformal and scale gauge to obtain the usual action for gravity. We will adopt the same procedure for supergravity. An important technical point to remember is that, \Box^{c} , the conformal d'Alambertian contains R, which for constant ϕ , leads to gravity. We may call ϕ the auxiliary field.

After the scale and conformal gauges have been fixed, the conformal Lagrangian becomes a de Sitter Lagrangian.

Einstein-Hilbert gravity can be derived from the de Sitter Lagrangian,

as was first shown by MacDowell and Mansouri (Phys. Rev. Lett. 38 (1977) 739).

(Frank Wilczek, in hep-th/9801184 says that the MacDowell-Mansouri "... approach

to casting gravity as a gauge theory was initiated by MacDowell and Mansouri ...

S. MacDowell and F. Mansouri, Phys. Rev. Lett. 38 739 (1977) ... ,

and independently Chamseddine and West ... A. Chamseddine and P. West Nucl. Phys. B 129, 39 (1977); also quite relevant is A. Chamseddine, Ann. Phys. 113, 219 (1978). ...".)

The minimal group required to produce Gravity,

and therefore the group that is used in calculating Force Strengths, is the [anti] de Sitter group, as is described by Freund in chapter 21 of his book Supersymmetry (Cambridge 1986) (chapter 21 is a Non-Supersymmetry chapter leading up to a Supergravity description in the following chapter 22): "... Einstein gravity as a gauge theory ... we expect a set of gauge fields w^ab_u for the Lorentz group and a further set e[^]a_u for the translations, ... Everybody knows though, that Einstein's theory contains but one spin two field, originally chosen by Einstein as g_uv = e^a_u e^b_v n_ab (n ab = Minkowski metric). What happened to the w^ab_u? The field equations obtained from the Hilbert-Einstein action by varying the w^ab_u are algebraic in the w^ab_u ... permitting us to express the w^ab_u in terms of the e[^]a u ... The w do not propagate ... We start from the four-dimensional de-Sitter algebra \dots so(3,2). Technically this is the anti-de-Sitter algebra ... We envision space-time as a four-dimensional manifold M. At each point of M we have a copy of SO(3,2) (a fibre ...) ... and we introduce the gauge potentials (the connection) $h^A_mu(x)$ A = 1,..., 10, mu = 1,...,4. Here x are local coordinates on M. From these potentials h^A mu we calculate the field-strengths (curvature components) [let @ denote partial derivative] R^A munu = @ mu h^A nu - @ nu h^A mu + f^A BC h^B mu h^C nu ...[where]... the structure constants f^C_AB ...[are for]... the anti-de-Sitter algebra We now wish to write down the action S as an integral over the four-manifold M ... $S(Q) = INTEGRAL_M R^A \wedge R^B Q_AB$ where Q AB are constants ... to be chosen ... we require ... the invariance of S(Q) under local Lorentz transformations ... the invariance of S(Q) under space inversions[AFTER A LOT OF ALGEBRA NOT SHOWN IN THIS QUOTE]... we shall see ... [that]... the action becomes invariant under all local [anti]de-Sitter transformations ...[and]... we recognize ... t he familiar Hilbert-Einstein action with cosmological term in vierbein notation ... Variation of the vierbein leads to the Einstein equations with cosmological term. Variation of the spin-connection ... in turn ... yield the torsionless Christoffel connection ... the torsion components ... now vanish. So at this level full sp(4) invariance has been checked. ... Were it not for the assumed space-inversion invariance ... we could have had a parity violating gravity. ... Unlike Einstein's theory ... [MacDowell-Mansouri] does not require Riemannian invertibility of the metric. ... the solution has torsion ... produced by an interference between parity violating and parity conserving amplitudes. Parity violation and torsion go hand-in-hand. Independently of any more realistic parity violating solution of the gravity equations this raises the cosmological guestion whether

the universe as a whole is in a space-inversion symmetric configuration. ...".

According to gr-gc/9809061 by R. Aldrovandi and J. G. Peireira: "... If the fundamental spacetime symmetry of the laws of Physics is that given by the de Sitter instead of the Poincare group, the P-symmetry of the weak cosmological-constant limit and the Q-symmetry of the strong cosmological constant limit can be considered as limiting cases of the fundamental symmetry. N ... [is the space]... whose geometry is gravitationally related to an infinite cosmological constant ... [and]... is a 4-dimensional cone-space in which ds = 0, and whose group of motion is Q. Analogously to the Minkowski case, N is also a homogeneous space, but now under the kinematical group Q, that is, N = Q/L[where L is the Lorentz Group of Rotations and Boosts]. In other words, the point-set of N is the point-set of the special conformal transformations. Furthermore, the manifold of Q is a principal bundle P(Q/L,L), with Q/L = N as base space and L as the typical fiber. The kinematical group Q, like the Poincare group, has the Lorentz group L as the subgroup accounting for both the isotropy and the equivalence of inertial frames in this space. However, the special conformal transformations introduce a new kind of homogeneity. Instead of ordinary translations, all the points of N are equivalent through special conformal transformations. ...

... Minkowski and the cone-space can be considered as dual to each other, in the sense that their geometries are determined respectively by a vanishing and an infinite cosmological constants. The same can be said of their kinematical group of motions: P is associated to a vanishing cosmological constant and Q to an infinite cosmological constant.

The dual transformation connecting these two geometries is the spacetime inversion $x^u \rightarrow x^u / sigma^2$. Under such a transformation, the Poincare group P is transformed into the group Q, and the Minkowski space M becomes the conespace N. The points at infinity of M are concentrated in the vertex of the conespace N, and those on the light-cone of M becomes the infinity of N. It is concepts of space isotropy and equivalence between inertial frames in the conespace N are those of special relativity. The difference lies in the concept of uniformity as it is the special conformal transformations, and not ordinary translations, which act transitively on N. ..." Gravity and the Cosmological Constant come from the MacDowell-Mansouri Mechanism and the 15-dimensional Spin(2,4) = SU(2,2) Conformal Group, which is made up of:

3 Rotations 3 Boosts 4 Translations 4 Special Conformal transformations 1 Dilatation

The **Cosmological Constant / Dark Energy** comes from the **10 Rotation, Boost, and Special Conformal generators** of the Conformal Group Spin(2,4) = SU(2,2), so the fractional part of our Universe of the Cosmological Constant should be **about 10 / 15 = 67% for tree level**.

Black Holes, including **Dark Matter Primordial Black Holes**, are curvature singularities in our 4-dimensional physical spacetime, and since Einstein-Hilbert curvature comes from the **4 Translations** of the 15-dimensional Conformal Group Spin(2,4) = SU(2,2) through the MacDowell-Mansouri Mechanism (in which the generators corresponding to the 3 Rotations and 3 Boosts do not propagate), the fractional part of our Universe of Dark Matter Primordial Black Holes should be **about 4 / 15 = 27% at tree level**.

Since **Ordinary Matter** gets mass from the Higgs mechanism which is related to the **1 Scale Dilatation** of the 15-dimensional Conformal Group Spin(2,4) = SU(2,2), the fractional part of our universe of Ordinary Matter should be **about 1 / 15 = 6% at tree level**.

However,

as Our Universe evolves the Dark Energy, Dark Matter, and Ordinary Matter densities evolve at different rates,

so that the differences in evolution must be taken into account from the initial End of Inflation to the Present Time.

Without taking into account any evolutionary changes with time, our Flat Expanding Universe should have roughly:

67% Cosmological Constant 27% Dark Matter - possilbly primordial stable Planck mass black holes 6% Ordinary Matter As Dennis Marks pointed out to me,

since density rho is proportional to $(1+z)^{3}(1+w)$ for red-shift factor z and a constant equation of state w:

w = -1 for \land and the average overall density of \land Dark Energy remains constant with time and the expansion of our Universe; and

w = 0 for nonrelativistic matter so that the overall average density of Ordinary Matter declines as $1 / R^3$ as our Universe expands;

and

w = 0 for primordial black hole dark matter - stable Planck mass black holes - so that Dark Matter also has density that declines as 1 / R^3 as our Universe expands; so that the ratio of their overall average densities must vary with time, or scale factor R of our Universe, as it expands.

Therefore,

the above calculated ratio 0.67 : 0.27 : 0.06 is valid

only for a particular time, or scale factor, of our Universe.

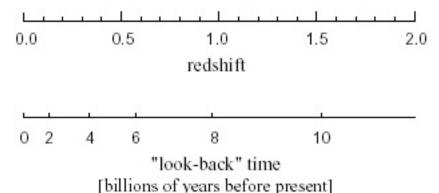
When is that time ? Further, what is the value of the ratio now ?

Since WMAP observes Ordinary Matter at 4% NOW, the time when Ordinary Matter was 6% would be

at redshift z such that

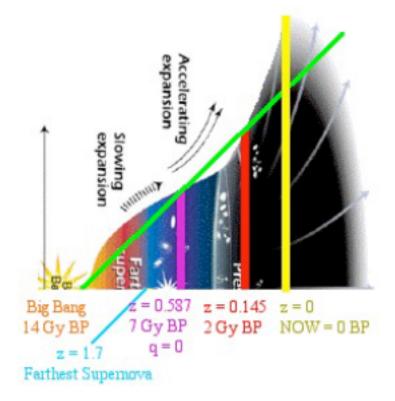
 $1 / (1+z)^3 = 0.04 / 0.06 = 2/3$, or $(1+z)^3 = 1.5$, or 1+z = 1.145 , or z = 0.145. To translate redshift into time,

in billions of years before present, or Gy BP, use this chart



from a <u>www.supernova.lbl.gov</u> file SNAPoverview.pdf to see that the time when Ordinary Matter was 6%

would have been a bit over 2 billion years ago, or 2 Gy BP.



In the diagram, there are four Special Times in the history of our Universe: the Big Bang Beginning of Inflation (about 13.7 Gy BP);

1 - the End of Inflation = Beginning of Decelerating Expansion (beginning of green line also about 13.7 Gy BP);

2 - the End of Deceleration (q=0) = Inflection Point =

= Beginning of Accelerating Expansion

(purple vertical line at about z = 0.587 and about 7 Gy BP).

According to a hubblesite web page credited to Ann Feild, the above diagram "... reveals changes in the rate of expansion since the universe's birth 15 billion years ago. The more shallow the curve, the faster the rate of expansion. The curve changes noticeably about 7.5 billion years ago, when objects in the universe began flying apart as a faster rate. ...".

According to a CERN Courier web page: "... Saul Perlmutter, who is head of the Supernova Cosmology Project ... and his team have studied altogether some 80 high red-shift type Ia supernovae. Their results imply that the universe was decelerating for the first half of its existence, and then began accelerating approximately 7 billion years ago. ...".

According to astro-ph/0106051 by Michael S. Turner and Adam G. Riess: "... current supernova data ... favor deceleration at z > 0.5 ... SN 1997ff at z = 1.7 provides direct evidence for an early phase of slowing expansion if the dark energy is a cosmological constant ...".

3 - the Last Intersection of the Accelerating Expansion of our Universe of Linear Expansion (green line) with the Third Intersection

(at red vertical line at z = 0.145 and about 2 Gy BP),

which is also around the times of the beginning of the Proterozoic Era and Eukaryotic Life, Fe2O3 Hematite ferric iron Red Bed formations, a Snowball Earth, and the start of the Oklo fission reactor. 2 Gy is also about 10 Galactic Years for our Milky Way Galaxy and is on the order of the time for the process of a collision of galaxies.

4 - Now.

Those four Special Times define four Special Epochs:

The Inflation Epoch, beginning with the Big Bang and ending with the End of Inflation. The Inflation Epoch is described by Zizzi Quantum Inflation ending with Self-Decoherence of our Universe (see gr-qc/0007006).

The Decelerating Expansion Epoch, beginning with the Self-Decoherence of our Universe at the End of Inflation. During the Decelerating Expansion Epoch, the Radiation Era is succeeded by the Matter Era, and the Matter Components (Dark and Ordinary) remain more prominent than they would be under the "standard norm" conditions of Linear Expansion.

The Early Accelerating Expansion Epoch, beginning with the End of Deceleration and ending with the Last Intersection of Accelerating Expansion with Linear Expansion. During Accelerating Expansion, the prominence of Matter Components (Dark and Ordinary) declines, reaching the "standard norm" condition of Linear Expansion at the end of the Early Accelerating Expansion Epoch at the Last Intersection with the Line of Linear Expansion.

The Late Accelerating Expansion Epoch, beginning with the Last Intersection of Accelerating Expansion and continuing forever, with New Universe creation happening many times at Many Times. During the Late Accelerating Expansion Epoch, the Cosmological Constant \land is more prominent than it would be under the "standard norm" conditions of Linear Expansion.

Now happens to be about 2 billion years into the Late Accelerating Expansion Epoch.

What about Dark Energy : Dark Matter : Ordinary Matter now ?

As to how the Dark Energy \land and Cold Dark Matter terms have evolved during the past 2 Gy, a rough estimate analysis would be:

 \land and CDM would be effectively created during expansion in their natural ratio 67 : 27 = 2.48 = 5 / 2, each having proportionate fraction 5 / 7 and 2 / 7, respectively; CDM Black Hole decay would be ignored; and

pre-existing CDM Black Hole density would decline by the same 1 / R^3 factor as Ordinary Matter, from 0.27 to 0.27 / 1.5 = 0.18.

The Ordinary Matter excess 0.06 - 0.04 = 0.02 plus the first-order CDM excess 0.27 - 0.18 = 0.09 should be summed to get a total first-order excess of 0.11, which in turn should be distributed to the \land and CDM factors in their natural ratio 67 : 27, producing, for NOW after 2 Gy of expansion:

CDM Black Hole factor = $0.18 + 0.11 \times 2/7 = 0.18 + 0.03 = 0.21$ for a total calculated Dark Energy : Dark Matter : Ordinary Matter ratio for now of

0.75 : 0.21 : 0.04

so that the present ratio of 0.73 : 0.23 : 0.04 observed by WMAP seems to me to be substantially consistent with the cosmology of the E8 model.

2013 Planck Data (arxiv 1303.5062) showed "... anomalies ... previously observed in the WMAP data ... alignment between the quadrupole and octopole moments ... asymmetry of power between two ... hemispheres ... Cold Spot ... are now confirmed at ... 3 sigma ... but a higher level of confidence ...".

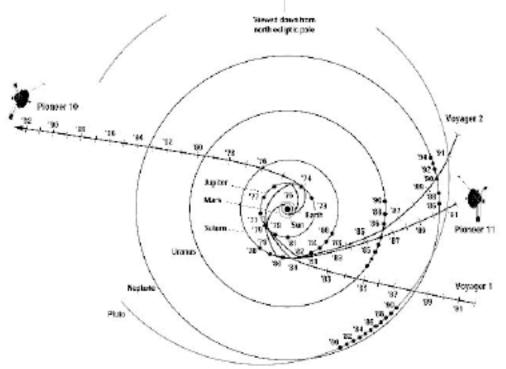
E8 model rough evolution calculation is: DE : DM : OM = 75 : 20 : 05 WMAP: DE : DM : OM = 73 : 23 : 04 Planck: DE : DM : OM = 69 : 26 : 05 basic unevolved E8 Conformal calculation: DE : DM : OM = 67 : 27 : 06

Since uncertainties are substantial, I think that there is reasonable consistency.

Conformal Gravity + Dark Energy and Pioneer Anomaly

After the Inflation Era and our Universe began its current phase of expansion, some regions of our Universe become Gravitationally Bound Domains (such as, for example, Galaxies)

in which the 4 Conformal GraviPhoton generators are frozen out, forming domains within our Universe like IceBergs in an Ocean of Water. On the scale of our Earth-Sun Solar System, the region of our Earth, where we do our local experiments, is in a Gravitationally Bound Domain.



Pioneer spacecraft are not bound to our Solar System and are experiments beyond the Gravitationally Bound Domain of our Earth-Sun Solar System.

In their Study of the anomalous acceleration of Pioneer 10 and 11 gr-qc/0104064 John D. Anderson, Philip A. Laing, Eunice L. Lau, Anthony S. Liu, Michael Martin Nieto, and Slava G. Turyshev say: "... The latest successful precession maneuver to point ...[Pioneer 10]... to Earth was accomplished on 11 February 2000, when Pioneer 10 was at a distance from the Sun of 75 AU. [The distance from the Earth was [about] 76 AU with a corresponding round-trip light time of about 21 hour.] ... The next attempt at a maneuver, on 8 July 2000, was unsuccessful ... conditions will again be favorable for an attempt around July, 2001. ... At a now nearly constant velocity relative to the Sun of 12.24 km/s, Pioneer 10 will continue its motion into interstellar space, heading generally for the red star Aldebaran ... about 68 light years away ... it should take Pioneer 10 over 2 million years to reach its neighborhood....

[the above image is] Ecliptic pole view of Pioneer 10, Pioneer 11, and Voyager trajectories. Digital artwork by T. Esposito. NASA ARC Image # AC97-0036-3. ... on 1 October 1990 ... Pioneer 11 ... was [about] 30 AU away from the Sun ...

The last communication from Pioneer 11 was received in November 1995, when the spacecraft was at distance of [about] 40 AU from the Sun. ... Pioneer 11 should pass close to the nearest star in the constellation Aquila in about 4 million years ...

... Calculations of the motion of a spacecraft are made on the basis of the range time-delay and/or the Doppler shift in the signals. This type of data was used to determine the positions, the velocities, and the magnitudes of the orientation maneuvers for the Pioneer, Galileo, and Ulysses spacecraft considered in this study. ... The Pioneer spacecraft only have two- and three-way S-band Doppler. ... analyses of radio Doppler ... data ... indicated that an apparent anomalous acceleration is acting on Pioneer 10 and 11 ... The data implied an anomalous, constant acceleration with a magnitude $a_P = 8 \times 10^{\circ}(-8) \text{ cm/cm/s}^2$, directed towards the Sun ...

... the size of the anomalous acceleration is of the order c H, where H is the Hubble constant ...

... Without using the apparent acceleration, CHASMP shows a steady frequency drift of about -6 x 10^(-9) Hz / s, or 1.5 Hz over 8 years (one-way only). ... This equates to a clock acceleration, -a_t, of -2.8 x 10^(-18) s / s^2. The identity with the apparent Pioneer acceleration is $a_P = a_t c. ...$

... Having noted the relationships

a_P = c a_t

and that of ...

a_H = c H -> 8 x 10^(-8) cm / s^2

if H = 82 km / s / Mpc ...

we were motivated to try to think of any ... "time" distortions that might ... fit the CHASMP Pioneer results ... In other words ...

Is there any evidence that some kind of "time acceleration" is being seen? ... In particular we considered ... Quadratic Time Augmentation. This model adds a quadratic-in-time augmentation to the TAI-ET (International Atomic Time -

Ephemeris Time) time transformation, as follows

ET -> ET + (1/2) a_ET ET^2

The model fits Doppler fairly well

····

There was one [other] model of the ...[time acceleration]... type that was especially fascinating. This model adds a quadratic in time term to the light time as seen by the DSN station:

delta_TAI = TAI_received - TAI_sent ->

-> delta_TAI + (1/2) a_quad (TAI_received^2 - TAI_sent^2)

It mimics a line of sight acceleration of the spacecraft, and could be thought of as an expanding space model.

Note that a_quad affects only the data. This is in contrast to the a_t ... that affects both the data and the trajectory. ... This model fit both Doppler and range very well. Pioneers 10 and 11 ... the numerical relationship between the Hubble constant and a_P ... remains an interesting conjecture. ...".

In his book "Mathematical Cosmology and Extragalactic Astronomy" (Academic Press 1976) (pages 61-62 and 72), Irving Ezra Segal says: "... Temporal evolution in ... Minkowski space ... is H -> H + s I ... unispace temporal evolution ... is ... H -> (H + 2 tan(a/2)) / (1 - (1/2) H tan(a/2)) = H + a I + (1/4) a H^2 + O(s^2) ...".

Therefore,

the Pioneer Doppler anomalous acceleration is an experimental observation of a system that is not gravitationally bound in the Earth-Sun Solar System, and its results are consistent with Segal's Conformal Theory.

My view can be summarized as a 2-phase model based on Segal's work which has two phases with different metrics:

a metric for outside the inner solar system, a dark energy phase in which gravity is described in which all 15 generators of the conformal group are effective, some of which are related to the dark energy by which our universe expands;

and

a metric for where we are, in regions dominated by ordinary matter, in which the 4 special conformal and 1 dilation degrees of freedom of the conformal group are suppressed and the remaining 10 generators (antideSitter or Poincare, etc) are effective, thus describing ordinary matter phenomena.

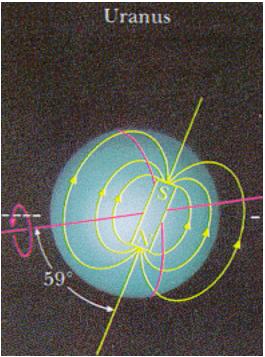
Transition at Orbit of Uranus:

It may be that the observation of the Pioneer phase transition at Uranus from ordinary to anomalous acceleration is an experimental result that gives us a first look at dark energy / dark matter phenomena that could lead to energy sources that could be even more important than nuclear energy.

In gr-qc/0104064 Anderson et al say:

"... Beginning in 1980 ... at a distance of 20 astronomical units (AU) from the Sun ... we found that the largest systematic error in the acceleration residuals was a constant bias, aP, directed toward the Sun. Such anomalous data have been continuously received ever since. ...",

so that the transition from inner solar system Minkowski acceleration to outer Segal Conformal acceleration occurs at about 20 AU, which is about the radius of the orbit of Uranus. That phase transition may account for the unique rotational axis of Uranus,



which lies almost in its orbital plane.

The most stable state of Uranus may be with its rotational axis pointed toward the Sun, so that the Solar hemisphere would be entirely in the inner solar system Minkowski acceleration phase and the anti-Solar hemisphere would be in entirely in the outer Segal Conformal acceleration phase.

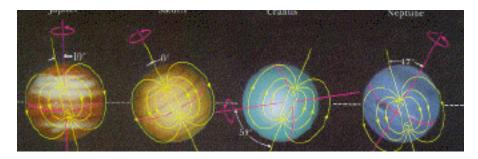
Then the rotation of Uranus would not take any material from one phase to the other, and there would be no drag on the rotation due to material going from phase to phase.

Of course, as Uranus orbits the Sun, it will only be in that most stable configuration twice in each orbit, but an orbit in the ecliptic containing that most stable configuration twice (such as its present orbit) would be in the set of the most stable ground states, although such an effect would be very small now. However, such an effect may have been been more significant on the large gas/dust cloud that was condensing into Uranus and therefore it may have caused Uranus to form initially with its rotational axis pointed toward the Sun.

In the pre-Uranus gas/dust cloud, any component of rotation that carried material from one phase to another would be suppressed by the drag of undergoing phase transition, so that, after Uranus condensed out of the gas/dust cloud, the only remaining component of Uranus rotation would be on an axis pointing close to the Sun, which is what we now observe.

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Much of the perpendicular (to Uranus orbital plane) angular momentum from the original gas/dust cloud may have been transferred (via particles "bouncing" off the phase boundary) to the clouds forming Saturn (inside the phase boundary) or Neptune (outside the phase boundary, thus accounting for the substantial (relative to Jupiter) deviation of their rotation axes from exact perpendicularity (see images above and below from "Universe", 4th ed, by William Kaufmann, Freeman 1994).



Conformal Gravity + Dark Energy and Warp Drive

Gabriele U. Varieschi and Zily Burstein in arXiv 1208.3706 showed that with Conformal Gravity Alcubierre Warp Drive does not need Exotic Matter.

In E8 Physics of viXra 1602.0319 Conformal Gravity gives Dark Energy which expands our Universe and can curve Spacetime.

Clovis Jacinto de Matos and Christian Beck in arXiv 0707.1797 said "... based on the model of dark energy a proposed by Beck and Mackey ... assume... that photons ... can exist in two different phases:

A gravitationally active phase where the zeropoint fluctuations contribute to the [dark energy] cosmological constant Λ ,

and a gravitationally inactive phase where they do not contribute to Λ .

... this type of model of dark energy can lead to measurable effects in supeconductors, via ... interaction with the Cooper pairs in the superconductor. ...

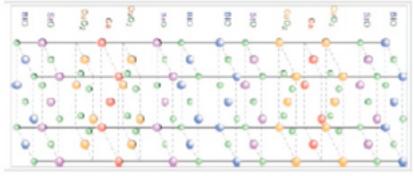
the transition between the two graviphoton's phases ... occurs at the critical temperature Tc of the superconductor, which defines a cutoff frequency of opoint fluctuations ...

Graviphotons can form weakly bounded states with Cooper pairs ...

[which] ... form a condensate ...[in]... superconduct[ors] ...

the cosmological cutoff frequency [could be measured] through the measurement of the spectral density of the noise current in resistively shunted Josephson Junctions ...".

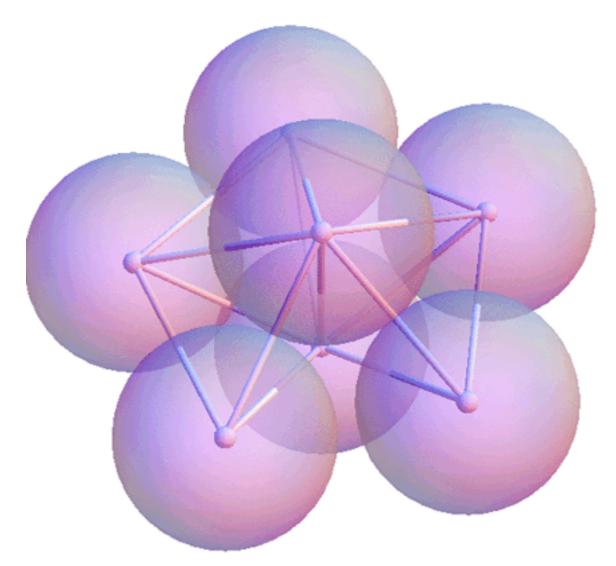
Xiao Hu and Shi-Zeng Lin in arXiv 0911.5371 and 1206.516 showed that BSCCO superconducting crystals are natural Josephson Junctions.



(BSCCO image from Wikipedia)

A Pentagonal Dipyramid configuration of 16 BSCCO crystals cannot close in flat 3-dim space, but can close if Conformal Dark Energy accumulated in the BSCCO Josephson Junctions curves spacetime. Such spacetime curvature allows construction of a Conformal Gravity Alcubierre Warp Drive that does not need Exotic Matter. "... If you spend any time playing with Geomag models,

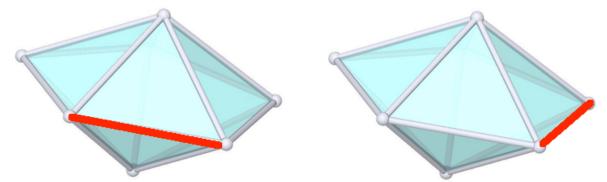
you are sure to stumble upon the structure ...



... which consists of four tetrahedra joined along faces. It looks as if you might be able to add one more bond to close the gap, creating a solid of five joined tetrahedra. But it doesn't work. The gap is slightly too wide. ..." (bit-player.org/2012/dancing-with-the-spheres)

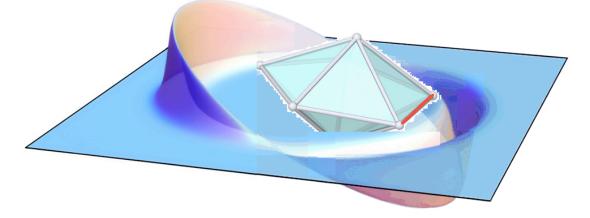
To close the 7.36 degree gap,

you can contract space in the tetrahedron containing the gap, keep unchanged the space in the other 4 tetrahedra, and expand space just outside the structure and opposite to the gap tetrahedron. In these images (from simply differently.org/Present/Data/Johnson_Solid/13.jpg)



the red edge designates two of the choices of which tetrahedron contains the gap and

in this image (from Wikipedia on Alcubierre drive)



the structure is shown with space contracting in front of the gap tetrahedron and expanding behind the structure.

"... Alcubierre drive (Wikipedia) ... Rather than exceeding the speed of light within a local reference frame, a spacecraft would traverse distances by

contracting space in front of it and expanding space behind it,

resulting in effective faster-than-light travel ... the Alcubierre drive shifts space around an object so that the object would arrive at its destination faster than light would in normal space ...".

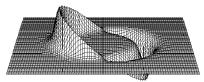
The Alcubierre Warp Drive (by John G. Cramer, Alternate View Column AV-81)

"... General relativity does not forbid faster-than-light [FTL] travel or communication, but it does require that the local restrictions of special relativity must apply ... One example of this is a wormhole connecting two widely separated locations in space ... by transiting the wormhole the object has traveled ...[at]... an effective speed of ...[many]... times the velocity of light.

Another example of FTL in general relativity is the expansion of the universe itself. As the universe expands, new space is being created between any two separated objects. The objects may be at rest with respect to their local environment and with respect to the cosmic microwave background, but the distance between them may grow at a rate greater than the velocity of light. According to the standard model of cosmology, parts of the universe are receding from us at FTL speeds, and therefore are completely isolated from us

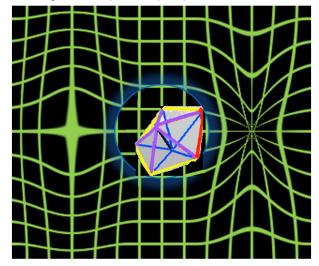
Alcubierre has proposed a way of beating the FTL speed limit that is somewhat like the expansion of the universe, but on a more local scale. He has developed a "metric" for general relativity ... that describes a region of flat space surrounded by a "warp" that propels it forward at any arbitrary velocity, including FTL speeds. Alcubierre's warp is constructed of hyperbolic tangent functions which create a very peculiar distortion of space at the edges of the flat-space volume. In effect, new space is rapidly being created ... at the back side of the moving volume, and existing space is being annihilated ... at the front side of the moving volume. Thus.

a space ship within the volume of the Alcubierre warp (and the volume itself) would be pushed forward by the expansion of space at its rear and the contraction of space in front. Here's a figure from Alcubierre's paper showing the curvature of space ...



... Since a ship at the center of the moving volume of the metric is at rest with respect to locally flat space, there are no relativistic mass increase or time dilation effects. The on-board spaceship clock runs at the same speed as the clock of an external observer, and that observer will detect no increase in the mass of the moving ship, even when it travels at FTL speeds. Moreover, Alcubierre has shown that even when the ship is accelerating, it travels on a free-fall geodesic. In other words, a ship using the warp to accelerate and decelerate is always in free fall, and the crew would experience no accelerational gee-forces. Enormous tidal forces would be present near the edges of the flat-space volume because of the large space curvature there, but by suitable specification of the metric, these would be made very small within the volume occupied by the ship ...".

(image below from George Dvorsky in Daily Explainer 11/26/12 at io9.gizmodo.com)



Appendix - Kepler Polyhedra and Planets

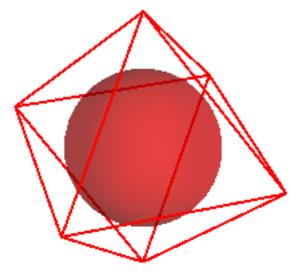
Abstract

This is my view of extension to Uranus and Neptune of Kepler's Mysterium Cosmographicum idea of relationship of Polytopes and Planetary Orbits

(images other than 24-cell are from, or adapted from, Wikipedia and Wolfram MathWorld)



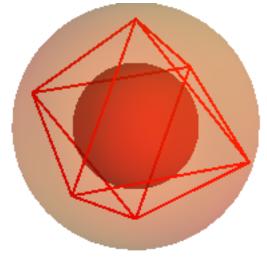
Octahedron = 6 space Axes



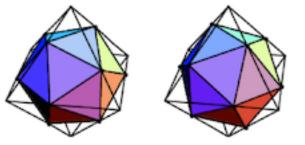
Venus / Mercury = 0.72 / 0.39 = 1.85

Octahedron Outer / Inner = sqrt(3) / 1 = $\frac{a}{2}\sqrt{2} \approx 0.707 \cdot a \int \frac{a}{6}\sqrt{6} \approx 0.408 \cdot a = 1.732$

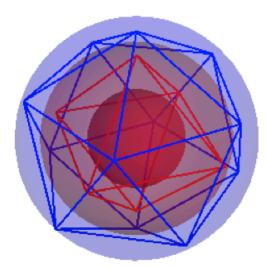
Venus = **Outer Octahedron** = Inner Icosahedron Icosahedron = 12 Golden Edge-Points of Octahedron



Earth = **Outer Icosahedron** = Inner Dodecahedron Icosahedron = 2 Octahedral embeddings = Earth + Moon



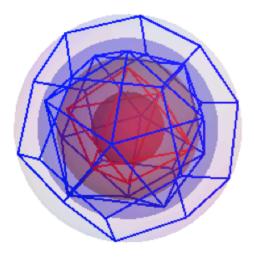
Dodecahedron = Dual Icosahedron



Mars / Earth = 1.52 / 1 = 1.52 Dodecahedron Outer / Inner = $\frac{\sqrt{3}}{4} (1 + \sqrt{5}) \approx 1.401258538 / \frac{1}{2} \sqrt{\frac{5}{2} + \frac{11}{10} \sqrt{5}} \approx 1.113516364 \approx 1.26$

Since Earth+Moon has 2 Outer Icosahedra, use 1.26 x 1.26 = 1.59

Mars = **Outer Dodecahedron** = Inner Tetrahedron Tetrahedron = 4 / 20 of Dodedahedron Vertices



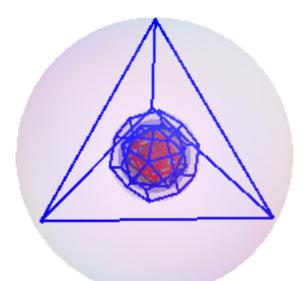
Tetrahedron = self-dual => stellated octahedron => unstable = Asteroids



Jupiter / Mars = 5.2 / 1.52 = 3.42

Tetrahedron Outer / Inner =
$$\sqrt{\frac{3}{8}} a = \frac{a}{\sqrt{24}} = 3$$

Jupiter = **Outer Tetrahedron** = Inner Cube Cube = 2 Tetrahedron Vertices = Dual Octahedron

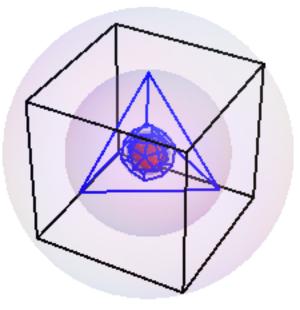


Saturn / Jupiter = 9.54 / 5.20 = 1.83

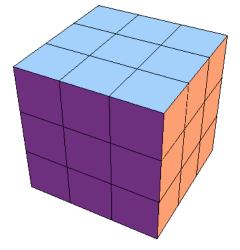
Cube Outer / Inner =
$$\frac{\sqrt{3}}{2}a$$
 $\int \frac{a}{2} = \sqrt{3} = 1.732$

Saturn = **Outer Cube** = Inner CubOctahedron

Cuboctahedron = Truncated Cube



Poincare Gravity Space = Tiled by Cube

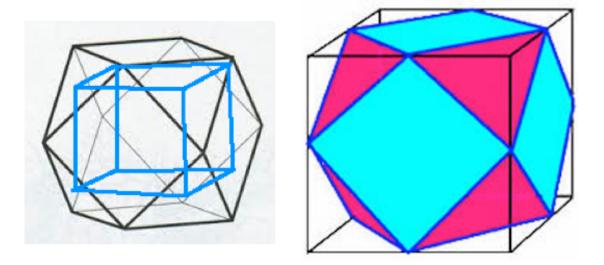


Uranus / Saturn = 19.19 / 9.54 = 2.01

CubOctahedron Outer (dilated by Basic Cube Edge / CubOcta Edge) / Inner (square face) = $\sqrt{2}$ $\frac{1}{2}\sqrt{2}$ = 2

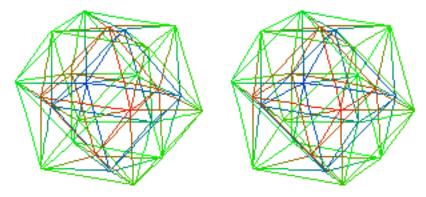
Uranus = **Outer CubOctahedron** = Inner Rhombic Dodecahedron Rhombic Dodecahedron = Dual Cuboctahedron

Cuboctahedron containing Cube of centers of Triangle Faces and Cuboctahedron within Basic Cube prior to Truncation



Uranus Orbit = Boundary of Pioneer Conformal Gravity Dark Energy

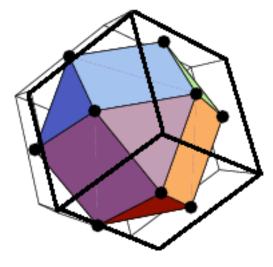
Cuboctahedron = Buckminster Fuller Vector Equilibrium = Center of 4-dim 24-cell



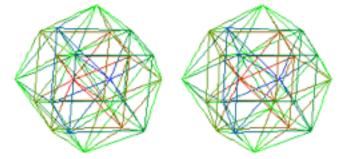
Neptune / Uranus= 30.06 / 19.19 = 1.57

Rhombic Dodecahedron Outer / Inner = $\frac{2\sqrt{3}}{3}a \approx 1.154\,700\,538a$ / $\frac{\sqrt{6}}{3}a \approx 0.816\,496\,5809a = \sqrt{2}$ = 1.414

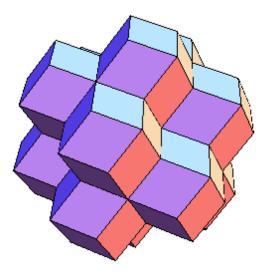
Neptune = Outer Rhombic Dodecahedron = Inner Conformal Gravity Space



Rhombic Dodecahedron = Center of 4-dim 24-cell

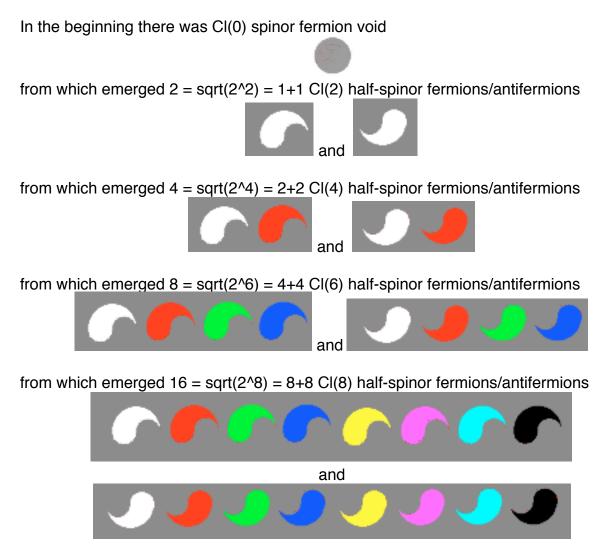


Conformal Gravity Space = Tiled by Rhombic Dodecahedra



Appendix - Spinor Growth, Octonion Inflation ended by Quaternions

Where does the E8 of E8 Physics come from ? Based on David Finkelstein's view of Fundamental Physics:



8 half-spinor fermions and 8 half-spinor antifermions are isomorphic by CI(8) Triality to each other and to the 8 CI(8) vectors



8-Periodicity of Real Clifford Algebras Cl(8) x ...(N times tensor product)... x Cl(8) = Cl(8N) shows that Cl(8) (or any tensor multiple it) is the basic building block of ALL Real Clifford Algebras, no matter how large they may be. The E8 Physics Creation Sequence begins with Spinor/Clifford Algebra Doubling

Cl(0,0) -> Cl(0,2) -> Cl(0,4) -> Cl(0,6) -> Cl(0,8) ->

that goes to Cl(0,8) which has Vector - Half-Spinor Triality and is the Basic Building Block of 8-Periodicity of Real Clifford Algebras whereby the Creation Sequence continues by Tensor Product

-> CI(0,8)xCI(0,8) = CI(0,16) -> CI(0,16)xCI(0,8) = CI(0,24) ->

CI(0,16) contains the Maximal Exceptional E8 Lie Algebra CI(0,24) contains the Vector Space of the 24-dim Leech Lattice \wedge 24 that is composed of 3 copies of E8 Lattices (2 being Integral Domains and 1 not Algebraically closed)

the Creation Sequence continues by constructing the Conformal Structure of 2x2 matrices with entries in Cl(0,24) = M(2,Cl(0,24))

-> M(2,Cl(0,24)) = Cl(1,25) ->

Since all the matrix entries are Cl(0,24) = tensor product of 3 copies of Cl(0,8)8-Periodicity allows formation of the tensor products of copies of Cl(1,25)

-> Completion of Union of All Tensor Products of Cl(1,25) = hyperfinite AQFT

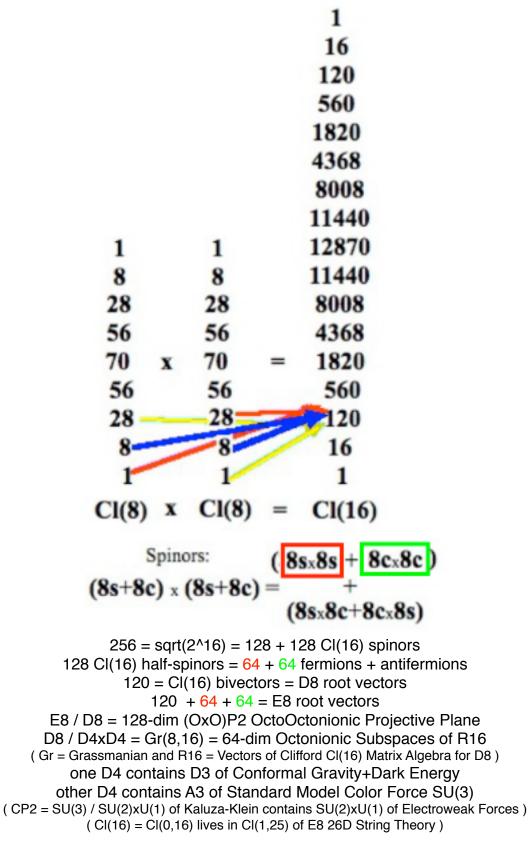
The hyperfinite AQFT has Real / Octonionic structure inherited from CI(0,8) and

it also has Quaternionic structure due to

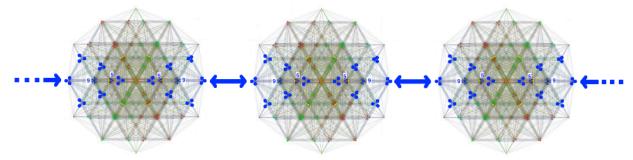
Cl(1,25) = Cl(1,9)xCl(0,8)xCl(0,8) and $Cl(1,9) = Cl(1,5) \times Cl(0,4) = Cl(2,4) \times Cl(0,4)$ where the vector space of Cl(2,4) is 6-dim Conformal Spacetime which contains 4-dim Minkowski Spacetime M4 of Cl(1,3)and the vector space of Cl(0,4) corresponds to CP2 = SU(3) / SU(2)xU(1)so that before breaking Octonionic symmetry non-unitarity of Octonion Quantum Processes allows particle creation during the Inflation Era and after breaking non-unitary Octonionic 8-dim Spacetime to unitary Quaternionic Spacetime, thus ending the Inflation Era, the Spacetime of the hyperfinite AQFT is (4+4)-dim M4 x CP2 Kaluza-Klein

> (see "Clifford Algebras and the Classical Groups" by Ian Porteous and his Chapter 2 of "Lectures on Clifford (Geometric) Algebras and Applications" and chapter E8 Quantum Theory ... page 23 of this paper)

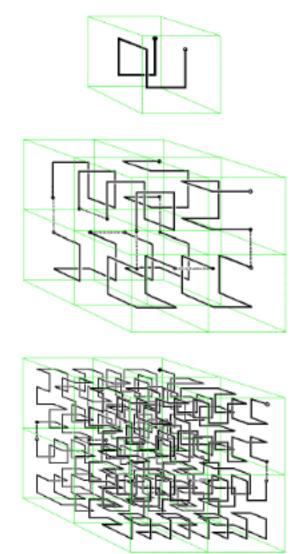
In particular, the tensor product $CI(8) \times CI(8) = CI(16)$



One Cl(1,25) containing one Cl(0,16) containing one E8 gives a Lagrangian description of one local spacetime neighborhood. To get a realistic global spacetime structure, take the tensor product Cl(1,25) x ... x Cl(1,25) with all E8 local 8-dim Octonionic spacetimes consistently aligned as described by 64-dim D8 / D4xD4 (blue dots) (this visualization uses a hexagonal type of projection of the 240 E8 root vectors to 2-dim)



which then fill up spacetime according to Gray Code Hilbert's curves:



Our Universe emerged from its parent in Octonionic Inflation



As Our Parent Universe expanded to a Cold Thin State Quantum Fluctuations occurred. Most of them just appeared and disappeared as Virtual Fluctuations, but at least one Quantum Fluctuation had enough energy to produce 64 Unfoldings and reach Paola Zizzi's State of Decoherence thus making it a Real Fluctuation that became Our Universe.

As Our Universe expands to a Cold Thin State, it will probably give birth to Our Child, GrandChild, etc, Universes.

Unlike "the inflationary multiverse" decribed by Andrei Linde in arXiv 1402.0526 as "a scientific justification of the anthropic principle", in the Cl(16,25 E8 model ALL Universes (Ours, Ancestors, Descendants) have the SAME Physics Structure as E8 Physics (viXra 1312.0036 and 1310.0182)

In the CI(1,25) E8 model, our SpaceTime remains Octonionic 8-dimensional throughout inflation.

Stephen L. Adler in his book Quaternionic Quantum Mechanics and Quantum Fields (1995) said at pages 50-52, 561: "... If the multiplication is associative, as in the complex and quaternionic cases, we can remove parentheses in ... Schroedinger equation dynamics ... to conclude that ... the inner product < f(t) | g(t) > ... is invariant ... this proof fails in the octonionic case, and hence one cannot follow the standard procedure to get a unitary dynamics. ...[so there is a]... failure of unitarity in octonionic quantum mechanics ..."

The NonAssociativity and Non-Unitarity of Octonions accounts for particle creation without the need for a conventional inflaton field.

E8 Physics has Representation space for 8 Fermion Particles + 8 Fermion Antiparticles on the original Cl(1,25) E8 Local Lagrangian Region

---- **+** -----

where a Fermion Representation slot $_$ of the 8+8 = 16 slots can be filled

by Real Fermion Particles 📍 or Real Fermion Antiparticles ¹

IF the Quantum Fluctuation(QF) has enough Energy to produce them as Real and

IF the CI(1,25) E8 Local Lagrangian Region has an Effective Path from its QF Energy to that Particular slot.

Let $Cl(16) = Cl(8) \times Cl(8)$ contained in Cl(1,25) where the first Cl(8) contains the D4 of Conformal Gravity with actions on M4 physical spacetime whose CPT symmetry determines the property matter - antimatter.

Consider, following basic ideas of Geoffrey Dixon related to his characterization of 64-dimensional spinor spaces as C x H x O (C = complex, H = quaternion, O = ocrtonion), 64-dim 64s++ = 8s+ x 8s+ of Cl(8) x Cl(8) = Cl(16) and 64-dim 64s+- = 8s+ x 8s- of Cl(8) x Cl(8) = Cl(16) so that 64s++ + 64s+- = 128s+ are +half-spinors of Cl(16) which is in E8

Then Cl(16) contains 128-dim +half-spinor space 64s++ + 64s+- of Cl(16) in E8 = Fermion Generation and 128-dim -half-spinor space 64s-+ + 64s-- of Cl(16) not in E8 = Fermion AntiGeneration

Since E8 contains only the 128 +half-spinors and none of the 128 -half-spinors of Cl(16) and

since, due to their +half-spinor property with respect to the first Cl(8), the 128s+=64s+++64s+- have only Effective Paths of QF Energy that go to the Fermion Particle slots that are also of type + that is, to the 8 Fermion Particle Representation slots

•••••••

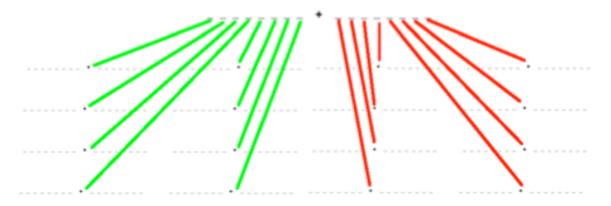
Next, consider the first Unfolding step of Octonionic Inflation. It is based on all 16 = 8 Fermion Particle slots + 8 Fermion Antiparticle Representation slots whether or not they have been filled by QF Energy.

7 of the 8 Fermion Particle slots correspond to the 7 Imaginary Octonions and therefore to the 7 Independent E8 Integral Domain Lattices and therefore to 7 New Cl(1,25) E8 Local Lagrangian Regions.

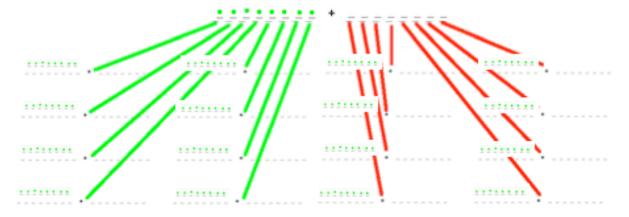
The 8th Fermion Particle slot corresponds to the 1 Real Octonion and

therefore to the 8th E8 Integral Domain Lattice (not independent - see Kirmse's mistake) and therefore to the 8th New Cl(1,25) E8 Local Lagrangian Region.

Similarly, the 8 Fermion Antiparticle slots Unfold into 8 more New New Cl(1,25) E8 Local Lagrangian Regions, so that one Unfolding Step is a 16-fold multiplication of Cl(1,25) E8 Local Lagrangian Regions:



If the QF Energy is sufficient, the Fermion Particle content after the first Unfolding is



so it is clear that the Octonionic Inflation Unfolding Process creates Fermion Particles with no Antiparticles, thus explaining the dominance of Matter over AntiMatter in Our Universe.

Each Unfolding has duration of the Planck Time Tplanck

and none of the components of the Unfolding Process Components are simultaneous, so that the total duration of N Unfoldings is 2^N Tplanck.

Paola Zizzi in gr-qc/0007006 said: "... during inflation,

the universe can be described as a superposed state of quantum ... [qubits]. the self-reduction of the superposed quantum state is ... reached at the end of inflation ...[at]... the decoherence time ... [Tdecoh = 10^9 Tplanck = 10^(-34) sec] ... and corresponds to a superposed state of ... [10^19 = 2^64 qubits]. ...".

Why decoherence at 64 Unfoldings = 2^64 qubits ?

 2^{64} qubits corresponds to the Clifford algebra Cl(64) = Cl(8x8). By the periodicity-8 theorem of Real Clifford algebras, Cl(64) is the smallest Real Clifford algebra for which we can reflexively identify each component Cl(8) with a vector in the Cl(8) vector space. This reflexive identification/reduction causes our universe to decohere at N = 2^{64} = 10^{19}

which is roughly the number of Quantum Consciousness Tubulins in the Human Brain. The Real Clifford Algebra Cl(8) is the basic building block of Real Clifford Algebras due to 8-Periodicity whereby $Cl(8N) = Cl(8) \times ...(N \text{ times tensor product})... \times Cl(8)$ An Octonionic basis for the Cl(8) 8-dim vector space is {1,i,j,k,E,I,J,K}

NonAssociativity, NonUnitarity, and Reflexivity of Octonions is exemplified by the 1-1 correspondence between Octonion Basis Elements and E8 Integral Domains

1 <=> 0E8 i <=> 1E8 j <=> 2E8 k <=> 3E8 E <=> 4E8 I <=> 5E8 J <=> 6E8 K <=> 7E8

where 1E8,2E8,3E8,4E8,5E8,6E8,7E8 are 7 independent Integral Domain E8 Lattices and 0E8 is an 8th E8 Lattice (Kirmse's mistake) not closed as an Integral Domain. Using that correspondence expands the basis {1,i,j,k,E,I,J,K} to

{0E8,1E8,2E8,3E8,4E8,5E8,6E8,7E8}

Each of the E8 Lattices has 240 nearest neighbor vectors so the total dimension of the Expanded Space is 240 x 240

so all Quantum States in the Expanded Space comes directly from the original Ci(8) 8-dim space However,

if further expansion is attempted, there is no direct connection to original CI(8) space and any Quantum Superposition undergoes Decoherence.

If each 240 is embedded reflexively into the 256 elements of Cl(8) the total dimension is

256 x 256 = 256^8 = 2^(8x8) = 2^64 =

= $CI(8) \times CI(8) = CI(8\times8) = CI(64)$ so the largest Clifford Algebra that can maintain Coherent Superposition is CI(64) which is why Zizzi Quantum Inflation ends at the CI(64) level.

At the end of 64 Unfoldings, Non-Unitary Octonionic Inflation ended having produced about (1/2) $16^{64} = (1/2) (2^{4})^{64} = 2^{255} = 6 \times 10^{76}$ Fermion Particles

The End of Inflation time was at about 10⁽⁻³⁴⁾ sec = 2⁶⁴ Tplanck

and

the size of our Universe was then about 10^(-24) cm

which is about the size of a Fermion Schwinger Source Kerr-Newman Cloud.

End of Inflation and Low Initial Entropy in Our Universe:

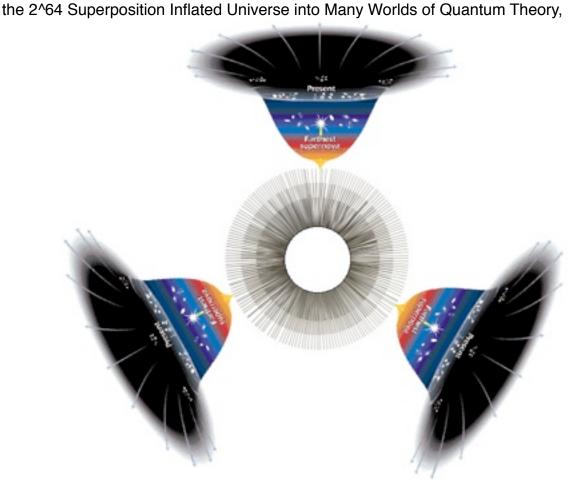
Roger Penrose in his book The Emperor's New Mind (Oxford 1989, pages 316-317) said: "... in our universe ... Entropy ... increases ... Something forced the entropy to be low in the past. ... **the low-entropy states in the past are a puzzle**. ...".

The key to solving Penrose's Puzzle is given by Paola Zizzi in gr-qc/0007006:

"... The self-reduction of the superposed quantum state is ... reached at the end of inflation ...[at]... the decoherence time ... [Tdecoh = 10^9 Tplanck = 10(-34) sec] ... and corresponds to a superposed state of ... [$10^19 = 2^64$ qubits]. This is also the number of

... I his is also the number of

superposed tubulins-qubits in our brain ... leading to a conscious event. ...". The Zizzi Inflation phase of our universe ends with decoherence "collapse" of the 2464 Superposition Inflated Universe into Many Worlds of Overture Theory.

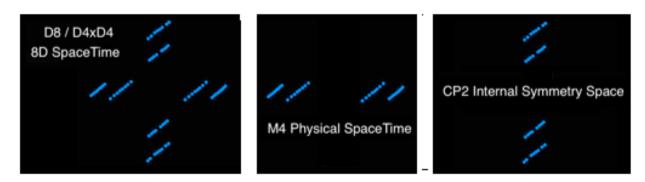


only one of which Worlds is our World. The central white circle is the Inflation Era in which everything is in Superposition; the boundary of the central circle marks the decoherence/collapse at the End of Inflation; and each line radiating from the central circle corrresponds to one decohered/collapsed Universe World (of course, there are many more lines than actually shown), only three of which are explicitly indicated in the image, and only one of which is Our Universe World.

Since our World is only a tiny fraction of all the Worlds, it carries only a tiny fraction of the entropy of the 2^64 Superposition Inflated Universe, thus solving Penrose's Puzzle.

End of Inflation and Quaternionic Structure

In Cl(1,25) E8 Physics (vixra 1405.0030) Octonionic symmetry of 8-dim spacetime is broken at the End of Non-Unitary Octonionic Inflation to Quaternionic symmetry of (4+4)-dim Kaluza-Klein M4 x CP2 physical spacetime x internal symmetry space.



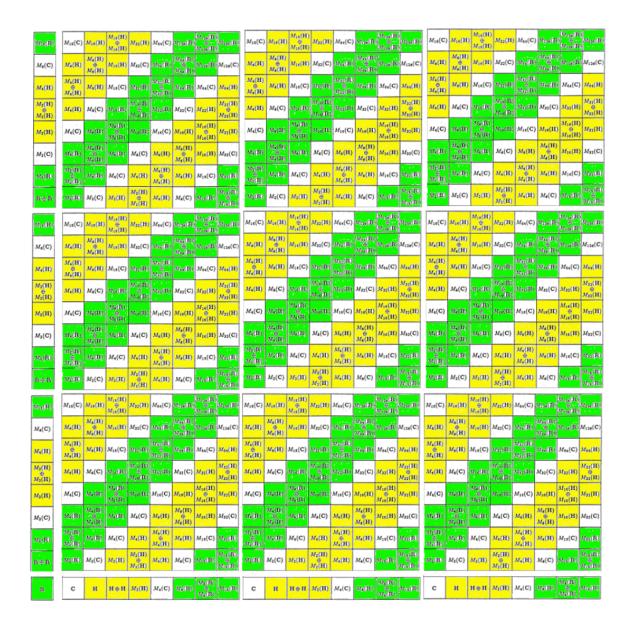
Here are some details about that transition:

The basic local entity of Cl(1,25) E8 Physics is Cl(1,25) which contains Cl(0,16) = Cl(1,15) = Cl(4,12) = Cl(5,11) = Cl(8,8) = M(R,256) = 256x256 Real Matrices which contains E8 with 8-dim Octonionic spacetime and is the tensor product Cl(0,8) x Cl(0,8) = Cl(1,7) x Cl(1,7) where Cl(0,8) = Cl(1,7) = M(R,16) is the Clifford Algebra of the 8-dim spacetime.

Non-Unitary Octonionic Inflation is based on Octonionic spacetime structure with superposition of E8 integral domain lattices. At the End of Inflation the superposition ends and Octonionic 8-dim structure is replaced by Quaternionic (4+4)-dim structure.

Since $M(R,16) = M(Q,2) \times M(Q,2)$ and M(Q,2) = CI(1,3) = CI(0,4) CI(0,8) = CI(1,7) can be represented as $CI(1,3) \times CI(0,4)$ where CI(1,3) is the Clifford Algebra for M4 physical spacetime and CI(0,4) is the Clifford Algebra for CP2 = SU(3) / U(2) internal symmetry space thus making explicit the Quaternionic structure of (4+4)-dim M4 x CP2 Kaluza-Klein.

Quaternionic structure similar to that of CI(1,3) = CI(0,4) = M(Q,2) is seen in CI(2,4) = M(Q,4) = 4x4 Quaternion matrices with grading based on 4x4 = 1 4 6 4 1



Conformal Gravity Spin(2,4) = SU(2,2) of Cl(2,4) = M(Q,4) 4x4 Quaternionic Matrices

Appendix - Quaternion Hurwitz Shells - Primes and Powers of 2

Conway and Smith, in "On Quaternions and Octonions" said:

"... 5.1 The Hurwitz Integral Quaternions ... Hurwitz ... found a ... definition ... that a+bi+cj+dk is a Hurwitz integer just if either all of a, b, c, d are in Z or all are in Z + 1/2 ... A prime Hurwitz integer P is one whose norm is a rational prime p.

Analogously to the fact that $p = p \ge 1$ and $p = 1 \ge p$ are the only ways p is the product of two rational primes, its only factorizations into two Hurwitz integers must have the form $P = P' \ge 0$ and $P = V \ge P''$, where N(P) = N(P'') = p and N(U) = N(V) = 1.

So, we must ... study the Hurwitz units ... the Hurwitz integers of norm 1.

Theorem 1. There are precisely 24 Hurwitz units, namely the eight Lipschitz units +1, $\pm i$, $\pm j$, $\pm k$, and the 16 others $\pm 1/2 \pm (1/2)i \pm (1/2)j \pm (1/2)k$

if P is a Hurwitz prime, then its only factorizations as a product of two Hurwitz integers are $P = P U^{(-1)} \times U$ and $P = V \times V^{(-1)} P$ as U and V run over the 24 Hurwitz units ... Theorem 3. Each rational prime p

admits at least one quaternionic factorization p = P0 P0".

Hurwitz quaternions whose (square) norm is rational prime are prime quaternions and there are no other prime quaternions. In particular, over the quaternions, no rational primes are prime.

The Hurwitz Integral Quaternions form the D4+ Lattice = Z4 Lattice that contains as a sublattice the D4 Lattice of the D4 Lie Algebra.

An integer N is a Power of 2 if and only if the D4+ Lattice sphere of radius N contains 24 D4+ Lattice vertices.

An integer N is a Rational Prime if and only if the D4+ Lattice sphere of radius N contains 8 (1+N) D4+ Lattice vertices.

The number of vertices of a Lattice on a sphere of given radius is described by the theta series of that lattice.

Conway and Sloane, in "Sphere Packings, Lattices, and Groups" said: "...

2.3 Theta series and connections with number theory. A very old problem asks for the number of ways of writing an integer m as a sum of four squares, or in other words for the number of quadruples of integers (x_1, x_2, x_3, x_4) such that

$$x_1^2 + x_2^2 + x_3^2 + x_4^2 = m.$$
 (29)

For example when m = 2 there are 24 solutions, consisting of all permutations of $(\pm 1, \pm 1, 0, 0)$. (We agree to count $2 = 1^2 + 1^2 + 0^2 + 0^2$, $2 = 1^2 + (-1)^2 + 0^2 + 0^2$, $2 = 1^2 + 0^2 + 1^2 + 0^2$ etc. as distinct solutions.)

There is a nice way to state this problem in terms of lattices. For any lattice Λ , let N_m be the number of vectors $x \in \Lambda$ of norm m, i.e. with $x \cdot x = m$. From (24), N_m is also the number of integral vectors ξ such that

$$\xi A \xi^{\prime\prime} = m, \qquad (30)$$

or in other words the number of times the quadratic form associated with Λ represents the number m. Eq. (30) is an example of a Diophantine

equation of degree 2 [Mor6]. Now $x_1^2 + x_2^2 + x_3^2 + x_4^2$ is the quadratic form associated with the four-dimensional cubic lattice \mathbb{Z}^4 . So the number of ways of writing *m* as a sum of four squares is equal to the number of vectors of norm *m* in the lattice \mathbb{Z}^4 .

The calculation of these numbers is facilitated by introducing the *theta* series of a lattice Λ , which is

$$\Theta_{\Lambda}(z) = \sum_{x \in \Lambda} q^{x \cdot x}$$
(31)

$$=\sum_{m=0}^{\infty}N_m q^m, \qquad (32)$$

where $q = e^{\pi i z}$. For many purposes we can just think of Θ_{Λ} as a formal power series in an indeterminate q, although for deeper investigations we must take $q = e^{\pi i z}$, where z is a complex variable. In this case $\Theta_{\Lambda}(z)$ is easily seen to be a holomorphic function of z for Im $(z) \ge 0$ [Gun1, p. 71], [Ser1, p. 109].

... The lattice Dn ... is ... the checkerboard lattice ... Theta series ...

To obtain the theta series of the lattice D_n (which consists of the points of \mathbb{Z}^n whose coordinates sum to an even number, Chap. 4, §7.1) we introduce the theta function θ_4 . θ_3 and θ_2 may be regarded as assigning unit masses to the integer and half-integer points on the real line respectively. To get θ_4 we assign masses of +1 to the even integers and -1 to the odd integers, or formally

$$\theta_4(z) = \sum_{m=-\infty}^{\infty} (-q)^{m^2} = 1 - 2q + 2q^4 - 2q^9 + 2q^{16} - \cdots$$
 (36)

Then

$$\Theta_{D_n}(z) = \frac{1}{2} \{\theta_3(z)^n + \theta_4(z)^n\}.$$

$$D_n : \frac{1}{2} (\theta_3(z)^n + \theta_4(z)^n) = \sum_{m=0}^{\infty} r_n(2m) q^{2m} J$$
(37)

... The four-dimensional lattice D4 ... theta series ...

The first 50 coefficients of the theta series for D_4 (using the first definition, Eq. (86)) are shown in Table 4.8. These coefficients are given explicitly by $N(2m) = r_4(2m)$, using the second formula in Eq. (49). Also N(2m) is the number of integral quaternions of norm m, and $(24)^{-1}N(2m)$ is a multiplicative function of m. In the notation of Schläfli and Coxeter, D_4 is the regular honeycomb $\{3, 3, 4, 3\}$ (see [Cox20, §7.8]).

Table 4.8. Theta series of 4-dimensional lattice D_4 . The table gives N(m) for m = 10r + s.

r\s	0	2	4	6	8	10	12	14	16	18
0	1	24	24	96	24	144	96	192	24	312
2	144	288	96	336	192	576	24	432	312	480
4	144	768	288	576	96	744	336	960	192	720
6	576	768	24	1152	432	1152	312	912	480	1344
8	144	1008	768	1056	288	1872	576	1152	96	1368
10	744	1728	336	1296	960	1728	192	1920	720	1440

 $[1] = (\frac{1}{2}, \frac{1}{2}, \dots, \frac{1}{2}),$ norm n/4, ... we define Dn+ = Dn u ([1]+Dn) ... Dn+ is a lattice packing if and only if n is even ... D4+ = Z4 ...

the theta series is $\frac{1}{2} \left(\theta_2(z)^n + \theta_3(z)^n + \theta_4(z)^n \right)$.

since D_4^+ is congruent to \mathbb{Z}^4 ,

we have the identity $\frac{1}{2}(\theta_2(z)^4 + \theta_3(z)^4 + \theta_4(z)^4) = \theta_3(z)^4$, i.e.

 $\theta_3(z)^4 = \theta_2(z)^4 + \theta_4(z)^4.$

•••

5. The *n*-dimensional cubic lattice \mathbb{Z}^n

The set of integers \dots , -2, -1, 0, 1, 2, 3, \dots is denoted by Z, and

$$\mathbf{Z}^n = \{ (x_1, \ldots, x_n) : x_i \in \mathbf{Z} \}$$

is the *n*-dimensional *cubic* or *integer lattice*. (\mathbb{Z}^2 is better called the square lattice, as seen in ordinary graph paper.) As generator matrix M we may simply take the identity matrix. Then det = 1, minimal norm = 1, kissing number $\tau = 2n$, and the minimal vectors are $(0, \ldots, \pm 1, \ldots, 0)$. The packing radius $\rho = 1/2$, the covering radius $R = \sqrt{n}/2 = \rho\sqrt{n}$, the density $\Delta = V_n 2^{-n}$ and the center density $\delta = 2^{-n}$. Thus Z has density $\Delta = 1$, but the densities of \mathbb{Z}^2 , \mathbb{Z}^3 and \mathbb{Z}^4 are only $\pi/4 = 0.785..., \pi/6 = 0.524...$ and $\pi^2/32 = 0.308...$. A typical deep hole is $(\frac{1}{2}, \frac{1}{2}, \dots, \frac{1}{2})$, and the Voronoi cells are cubes. \mathbb{Z}^n is self-dual. Its automorphism group consists of all permutations and sign changes of the coordinates, and has order $2^n n!$. (This is the Weyl group of B_n .)

The theta series of \mathbb{Z}^n is $\theta_3(z)^n$, and the theta series of the translate $\mathbb{Z}^n + (0^a \frac{1}{2}n^{-a})$ is

. . .

$$\theta_2(z)^{n-a} \theta_3(z)^a \tag{44}$$

If we expand

$$\Theta_{\mathbb{Z}_n}(z) = \theta_3(z)^n = \sum_{m=0}^{\infty} r_n(m) q^m,$$
(47)

then the coefficient $r_n(m)$ is the number of ways of writing m as a sum of n squares. In particular for m > 0 we have

$$r_2(m) = 4\delta(m) , \qquad (48)$$

where $\delta(m)$ is the difference between the numbers of divisors of m of the two forms 4a + 1, 4a + 3,

...

$$r_4(m) = \begin{cases} 8 \sum_{\substack{d \mid m \\ d \mid m}} d, & \text{if } m \text{ is odd,} \\ 24 \sum_{\substack{d \mid m, d \text{ odd}}} d, & \text{if } m \text{ is even,} \end{cases}$$
(49)

$$r_8(m) = 16 \sum_{d \mid m} (-1)^{m-d} d^3.$$
 (50)

If we define $r_4'(m) = r_4(m)/8$, then $r_4'(m)$ is multiplicative, i.e. satisfies

$$r_{4}'(\ell m) = r_{4}'(\ell)r_{4}'(m) \text{ whenever}$$

 $\ell \text{ and } m \text{ are relatively prime.}$ (51)

This property simplifies the calculation of $r_4'(m)$, for now it is enough to know the values when $m = p^a$ is a power of a prime. These are

$$r_4'(2^a) = 3, (a \ge 1),$$

 $r_4'(p^a) = 1 + p + p^2 + \dots + p^a, (a \ge 0),$

where p is an odd prime. A similar multiplicative property holds for the theta functions of certain other lattices. Bateman [Gro2, p. 131] has shown that $r_n(m)/2n$ is multiplicative if and only if n is 1, 2, 4 or 8. (This reflects the fact that there are unique factorization theorems for suitable rings of integers in the real, complex, quaternionic, and Cayley numbers.)

...

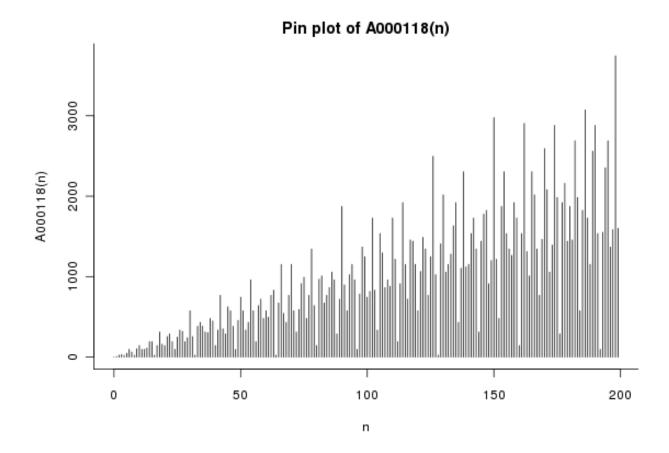
2.5 Modular forms. Further connections between lattices and number theory arise because the theta series of an integral lattice is a *modular form*. We do not state the general theorem here; some important special cases will be found in Chap. 7, Theorems 7 and 17. There is a brief account of the general theory of the connections between quadratic forms and modular forms in Cassels [Cas3, p. 382], and numerous other references: [Gun1], [Har4], [Hec2], [Hec3], [Kit3], [Kno1], [Lan9], [Ogg1], [Pet4], [Ran6], [Sch6], [Sch7], [Vig1].

theta series of lattice Z⁴ = D4+ = = Number of ways of writing n as sum of 4 squares = = Sloane OEIS A000118

....".

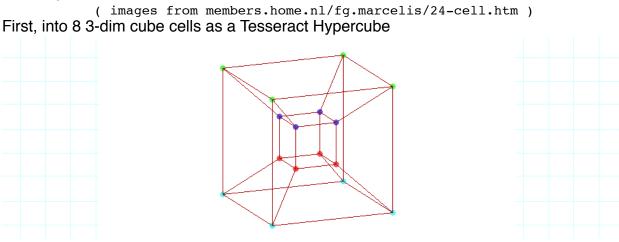
```
The green 24 numbers correspond to powers of 2
(2,4,8,16,32)
The red numbers correspond to primes beyond 2
(3,5,7,11,13,17,19,23,29,31,37,41,43,47,53)
```

1, 8, 24, 32, 24, 48, 96, 64, 24, 104, 144, 96, 96, 112, 192, 192, 24, 144, 312, 160, 144, 256, 288, 192, 96, 248, 336, 320, 192, 240, 576, 256, 24, 384, 432, 384, 312, 304, 480, 448, 144, 336, 768, 352, 288, 624, 576, 384, 96, 456, 744, 576, 336, 432, 960, 576, 192

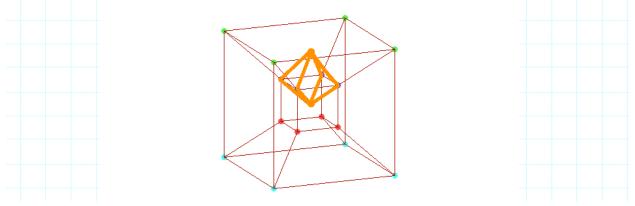


The D4+ Lattice lives in 4-dim Euclidean space and is made up of shells each of which is a set of vertices on a 3-sphere S3.

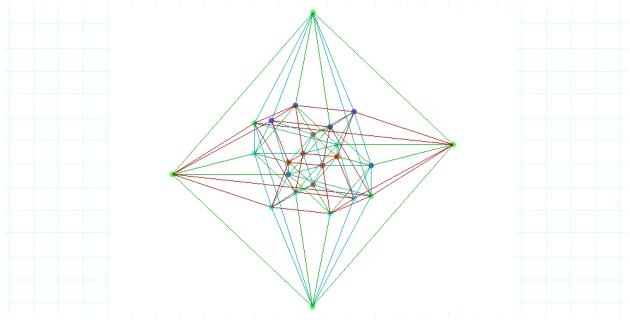
Two ways to subdivide the S3 are



The D4+ Lattice shell of radius 3 has $(1 + 3) \times 8 = 32$ vertices. They can be considered to be the centers of each of the 8 cube cells plus, distributed around the center in each of the 8 cube cells, one new vertex for each of the 3 steps in the radius of the S3 of radius 3. For all prime numbers p, and only for those numbers, the D4+ Lattice shell of radius p has (1 + p) x 8 vertices. They can be considered to be the centers of each of the 8 cube cells plus, distributed around the center in each of the 8 cube cells, one new vertex for each of the p steps in the radius of the S3 of radius p where p is a prime number. **This is a geometric characterization of prime numbers relating the radius of the 3-sphere S3 with the number of vertices on the S3**. Second, into 24 3-dim octahedron cells as a 24-cell. A 24-cell can be constructed from a Tessaract hypercube with 8 additional vertices, one at the center of each cube cell, by connecting pairs of additional vertices to the 4 vertices of the common face squares of each cube cell, producing 24 octahedron cells and 8+16 = 24 vertices of the 24-cell.



This produces a series of S3 shells of radius $p \ge 2^n$ (for prime p) each having (1 + p) ≥ 24 vertices. The D4+ Lattice shell of radius 2 has the 24 vertices of a 24-cell.



They can dually be considered to be the centers of each of the 24 octahedron cells. For all S3 of radius 2ⁿ for any n (i.e., for all radii that are powers of 2) the D4+ Lattice shell of radius 2ⁿ has 24 vertices. **This is a geometric characterization of powers of 2 relating the radius of the 3-sphere S3 with the number of vertices on the S3**. Here are the numbers of vertices in the first 45 shells of the D4+ lattice.

Red S3 shells have prime radius. Green S3 shells have power-of-2 radius. Purple S3 shells have prime x power-of-2 radius.

<pre>m = radius of shell</pre>	N(m) = no. vertices in shell of radius m
0	1
1	$8 = 1 \times 8$
2	$24 = (1 + 2) \times 8 = 1 \times 24$
3	$32 = (1 + 3) \times 8$
4	$24 = 1 \times 24$
5	$48 = (1 + 5) \times 8$
6	$96 = (1 + 3) \times 24$
7	$64 = (1 + 7) \times 8$
8	$24 = 1 \times 24$
9	$104 = (1 + 3 + 9) \times 8$
10	$144 = (1 + 5) \times 24$
11	$96 = (1 + 11) \times 8$
12	$96 = (1 + 3) \times 24$
13	$112 = (1 + 13) \times 8$
14	$192 = (1 + 7) \times 24$
15	$192 = (1 + 3 + 5 + 15) \times 8$
16	$24 = 1 \times 24$
17	$144 = (1 + 17) \times 8$
18	$312 = (1 + 3 + 9) \times 24$
19	$160 = (1 + 19) \times 8$
20	$144 = (1 + 5) \times 24$
21	$256 = (1 + 3 + 7 + 21) \times 8$
22	$288 = (1 + 11) \times 24$
23	$192 = (1 + 23) \times 8$
24	$96 = (1 + 3) \times 24$
25	
	,
26	
27	$320 = (1 + 3 + 9 + 27) \times 8$
28	$192 = (1 + 7) \times 24$
29	$240 = (1 + 29) \times 8$
30	$576 = (1 + 3 + 5 + 15) \times 24$
31	$256 = (1 + 31) \times 8$
32	$24 = 1 \times 24$
33	$384 = (1 + 3 + 11 + 33) \times 8$
34	$432 = (1 + 17) \times 24$
35	$384 = (1 + 5 + 7 + 35) \times 8$
36	$312 = (1 + 3 + 9) \times 24$
37	$304 = (1 + 37) \times 8$
38	$480 = (1 + 19) \times 24$
39	$448 = (1 + 3 + 13 + 39) \times 8$
40	$144 = (1 + 5) \times 24$
41	$336 = (1 + 41) \times 8$
42	$768 = (1 + 3 + 7 + 21) \times 24$
43	$352 = (1 + 43) \times 8$
44	$288 = (1 + 11) \times 24$
45	$624 = (1 + 3 + 5 + 9 + 15 + 45) \times 8$

Clifford Algebras have dimension Powers of 2.

The E8 Physics Creation Sequence begins with Spinor/Clifford Algebra Doubling

Cl(0,0) -> Cl(0,2) -> Cl(0,4) -> Cl(0,6) -> Cl(0,8) ->

that goes to CI(0,8) which has Vector - Half-Spinor Triality and is the Basic Building Block of 8-Periodicity of Real Clifford Algebras whereby the Creation Sequence continues by Tensor Product

-> Cl(0,8)xCl(0,8) = Cl(0,16) --> Cl(0,16)xCl(0,8) = Cl(0,24) ->

Cl(0,16) contains the Maximal Exceptional E8 Lie Algebra Cl(0,24) contains the Vector Space of the 24-dim Leech Lattice \wedge 24 that is composed of 3 copies of E8 Lattices (2 being Integral Domains and 1 not Algebraically closed)

the Creation Sequence continues by constructing the Conformal Structure of 2x2 matrices with entries in Cl(0,24) = M(2,Cl(0,24))

$$->$$
 M(2,Cl(0,24)) = Cl(1,25) $->$

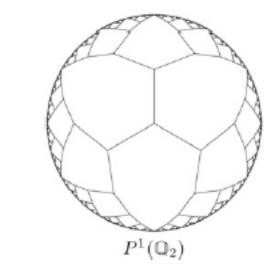
Since all the matrix entries are Cl(0,24) = tensor product of 3 copies of Cl(0,8)8-Periodicity allows formation of the tensor products of copies of Cl(1,25)

-> Completion of Union of All Tensor Products of Cl(1,25) = hyperfinite AQFT

The hyperfinite AQFT has Real / Octonionic structure inherited from CI(0,8) and

it also has Quaternionic structure due to

Cl(1,25) = Cl(1,9)xCl(0,8)xCl(0,8) and $Cl(1,9) = Cl(1,5) \times Cl(0,4) = Cl(2,4) \times Cl(0,4)$ where the vector space of Cl(2,4) is 6-dim Conformal Spacetime which contains 4-dim Minkowski Spacetime M4 of Cl(1,3)and the vector space of Cl(0,4) corresponds to CP2 = SU(3) / SU(2)xU(1)so that before breaking Octonionic symmetry non-unitarity of Octonion Quantum Processes allows particle creation during the Inflation Era and after breaking non-unitary Octonionic 8-dim Spacetime to unitary Quaternionic Spacetime, thus ending the Inflation Era, the Spacetime of the hyperfinite AQFT is (4+4)-dim M4 x CP2 Kaluza-Klein Through Cl(0,16) the sequence is in Clifford Algebras whose Vectors are Powers of 2 so that the D4 lattice spheres of Radius = Vector Dim contain 24 vertices The 24-cell has 24 vertices

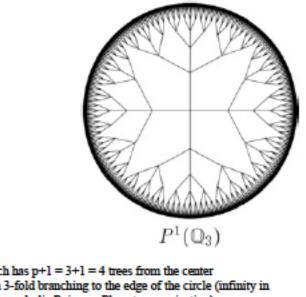


For the prime p = 2 the Broussous method gives

which as you can see has p+1 = 2+1 = 3 trees from the center with 2-fold branching to the edge of the circle (infinity in the hyperbolic Poincare Plane type projection). The binary 2-fold branching is like the YiJing and the binary + and - charges of electromagnetism and the binary system of fermion particles and antiparticles and the geometry of hypercubes.

(image from Paul Broussous web page www-math.univ-poitiers.fr/%7Ebroussou/recherche.htm)

At Cl(0,24), the Vectors have a Factor of 3 so that the D4 lattice sphere of Radius = Vector Dim = 24 contains (1+3)x24 = 96 vertices The 24-cell has 96 edges.

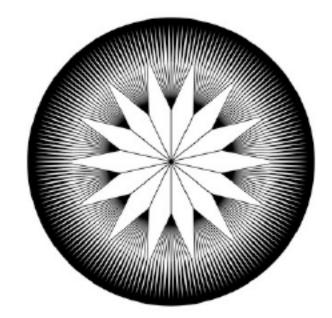


For the prime p = 3 the Broussous method gives

which has p+1 = 3+1 = 4 trees from the center with 3-fold branching to the edge of the circle (infinity in the hyperbolic Poincare Plane type projection). 3-fold branching may correspond to such things as: the geometry of sub-hypercubes of a hypercube; and the Tai Hsuan Ching of 3x3x3x3 = 81 tetragrams of ternary lines

(image from Paul Broussous web page www-math.univ-poitiers.fr/%7Ebroussou/recherche.htm)

At Cl(1,25), the Vectors have a Factor of 13 so that the D4 lattice sphere of Radius = Vector Dim = 26 contains (1+13)x24 = 336 vertices



For the prime p = 13 the Broussous method gives

which has p+1 = 13+1 = 14 trees from the center with 13-fold branching to the edge of the circle (infinity in the hyperbolic Poincare Plane type projection).

(image from Paul Broussous web page www-math.univ-poitiers.fr/%7Ebroussou/recherche.htm)

13 is the only number between 5 and 89 that is both Prime and Fibonacci. The 14 trees correspond to the 14 sections of the Klein Configuration.



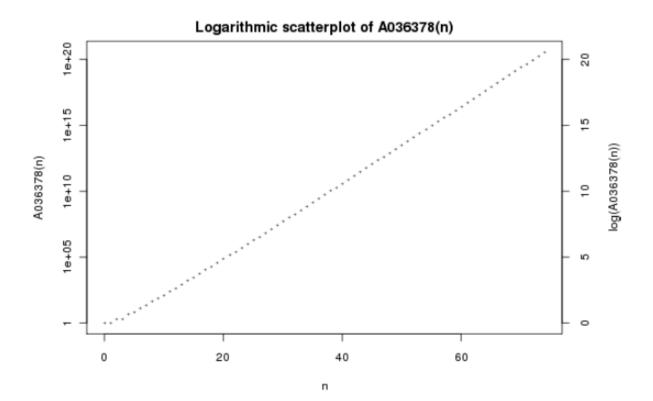
Klein Configuration represents group SL(2,7) with 336 elements. SL(2,7) is double cover of simple Klein Quartic symmetry group PSL(2,7) = SL(3,2)Klein Configuration has central 14-gon, and so 14 slices. Each slice has 24 triangles.

Prime Powers of 2 sequence = Sloane OEIS A036378 $n=0: 2^1 = 2$ has 1 prime 2, n=1: 2^2 = 4 has 1 prime З, n=2: 2^3 = 8 has 2 primes 5, 7, $n=3: 2^{4} = 16$ has 2 primes 11, 13, n=4: 2^5 = 32 has 5 primes 17, 19, 23, 29, 31, $n=5: 2^{6} = 64$ has 7 primes 37, 41, 43, 47, 53, 59, 61, n=6: 2^7 = 128 has 13 primes 67, 71, 73, 79, 83, 89, 97, 101, 103, 107, 109, 113, 127, n=7: 2^8 = 256 has 23 primes 131, 137, 139, 149, 151, 157, 163, 167, 173, 179, 181, 191, 193, 197, 199, 211, 223, 227, 229, 233, 239, 241, 251, n=8: 2^9 = 512 has 43 primes 257, 263, 269, 271, 277, 281, 283, 293, 307, 311, 313, 317, 331, 337, 347, 349, 353, 359, 367, 373, 379, 383, 389, 397, 401, 409, 419, 421, 431, 433, 439, 443, 449, 457, 461, 463, 467, 479, 487, 491, 499, 503, 509, n=9: 2^10 = 1024 has 75 primes 521, 523, 541, 547, 557, 563, 569, 571, 577, 587, 593, 599, 601, 607, 613, 617, 619, 631, 641, 643, 647, 653, 659, 661, 673, 677, 683, 691, 701, 709, 719, 727, 733, 739, 743, 751, 757, 761, 769, 773, 787, 797, 809, 811, 821, 823, 827, 829, 839, 853, 857, 859, 863, 877, 881, 883, 887, 907, 911, 919, 929, 937, 941, 947, 953, 967, 971, 977, 983, 991, 997, 1009, 1013, 1019, 1021 n=10: 2^11 = 2048 has 137 primes

Prime Powers of 2 sequence = Sloane OEIS A036378

Number of primes p between powers of 2, $2^n is$

1, 1, 2, 2, 5, 7, 13, 23, 43, 75, 137, 255, 464, 872, 1612, 3030, 5709, 10749, 20390, 38635, 73586, 140336, 268216, 513708, 985818, 1894120, 3645744, 7027290, 13561907, 26207278, 50697537, 98182656, 190335585, 369323305, 717267168, 1394192236 ...



Conway and Smith, in "On Quaternions and Octonions" said:

"... algebraists take "integer" to mean member of what's called a maximal order ... those octonions for which all the coordinates are ordinary integers ...

we call ... the Gravesian octaves or integers.

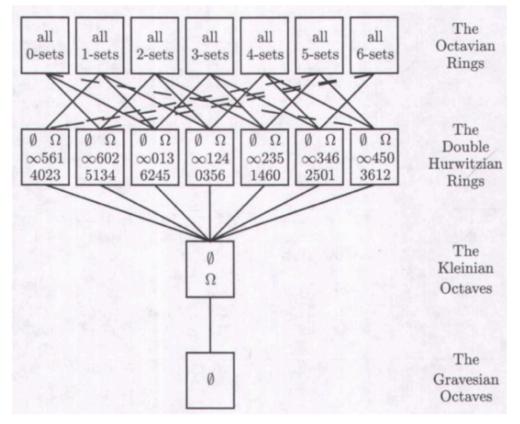
... Theorem 1. The orders containing the Gravesian integers are precisely the 16 integer systems ...

an octonion a whose coordinates are in (1/2) Z ...[and]... are not also in Z form what we shall call the halving-set ... introduce the notation ...

$$i_{abcd}$$
 for $\frac{i_a + i_b + i_c + i_d}{2}$, $i_{a\overline{b}c\overline{d}}$ for $\frac{i_a - i_b + i_c - i_d}{2}$

... We can specify one of the 16 systems by saying just which the halving-sets sets are. The multiplicative structure of the octonions already involves a distinguished family of quadruplets, namely those that correspond to quaternion subalgebras, together with their complements. These, ... [and]... the empty and full sets, we call the sixteen oo-sets: $\infty 602$ $\infty 124 \quad \infty 235 \quad \infty 346 \quad \infty 450 \quad \infty 561$ $\infty 013$ Ø $\Omega = \infty 0123456$ 0356 0146 0125 1236023413452456.

... An octonion whose halving-set is an oo-set we call an "oo-integer" ...



... or "Kirmse integer" ... [which] ... are not multiplicatively closed. ...

define the n-sets and n-integers (n = by interchanging oo with n in the definition of oosets and oc-integers ... with outer n-sets in bold ...

$\infty 124$	0356	0124	$\infty 356$		$\infty 124$	0356	$\infty 124$	0356
$\infty 235$	1460	0235	146∞		1235	$\infty 460$	$\infty 235$	1460
$\infty 346$	2501	0346	$25\infty1$		1346	250∞	2346	$\infty 501$
$\infty 450$	3612	$\infty 450$	3612		1450	$36\infty 2$	2450	361∞
$\infty 561$	4023	0561	$4\infty 23$		$\infty 561$	4023	2561	$40\infty3$
$\infty 602$	5134	$\infty 602$	5134		1602	$5\infty34$	$\infty 602$	5134
$\infty 013$	6245	$\infty 013$	6245		$\infty 013$	6245	2013	$6\infty45$
Ø	Ω	Ø	Ω		Ø	Ω	Ø	Ω
$\infty - sets$		0 -	0 - sets		1 - sets		2-sets	
3124	$0\infty56$	$\infty 124$	0356) (5124	03∞6	6124	035∞
$\begin{array}{c} 3124 \\ \infty 235 \end{array}$	$0\infty 56$ 1460	$\infty 124 \\ 4235$	$\begin{array}{c} 0356 \\ \mathbf{1\infty60} \end{array}$		5124 $\infty 235$	03∞6 1460	6124 6235	$egin{array}{c} 035\infty\ 14\infty0 \end{array}$
$\infty 235$	1460	4235	$1\infty60$		$\infty 235$	1460	6235	$14\infty0$
$\infty 235 \ \infty 346$	$\begin{array}{c} 1460 \\ 2501 \end{array}$	$\begin{array}{c} 4235 \\ \infty 346 \end{array}$	$1\infty60$ 2501		∞235 5346	$\begin{array}{c} 1460 \\ \mathbf{2\infty01} \end{array}$	6235 ∞346	$14\infty0$ 2501
$\infty 235 \\ \infty 346 \\ 3450$	$1460 \\ 2501 \\ \infty 612$	$4235 \\ \infty 346 \\ \infty 450$	$1\infty60$ 2501 3612		$\infty 235$ 5346 $\infty 450$	1460 $2\infty01$ 3612	$6235 \\ \infty 346 \\ 6450$	$14\infty0$ 2501 $3\infty12$
$\infty 235$ $\infty 346$ 3450 3561	$1460 \\ 2501 \\ \infty 612 \\ 402 \infty$	$4235 \ \infty 346 \ \infty 450 \ 4561$	$1\infty 60$ 2501 3612 $\infty 023$		$\infty 235$ 5346 $\infty 450$ $\infty 561$	$1460 \\ 2\infty01 \\ 3612 \\ 4023$	6235 $\infty 346$ 6450 $\infty 561$	$14\infty0$ 2501 $3\infty12$ 4023
$\infty 235$ $\infty 346$ 3450 3561 3602	$1460 \\ 2501 \\ \infty 612 \\ 402\infty \\ 51\infty 4$	$\begin{array}{c} 4235 \\ \infty 346 \\ \infty 450 \\ 4561 \\ 4602 \end{array}$	$1\infty 60$ 2501 3612 $\infty 023$ 513∞		$\infty 235$ 5346 $\infty 450$ $\infty 561$ 5602	1460 $2\infty01$ 3612 4023 $\infty134$	$6235 \\ \infty 346 \\ 6450 \\ \infty 561 \\ \infty 602$	$14\infty0$ 2501 $3\infty12$ 4023 5134

... The n-integers are multiplicatively closed for each n = 0,...,6. ... The seven systems are ... isomorphic ...

the 0-integers ... halving-sets are

Ø	0124	0235	0346	$\infty 450$	0561	$\infty 602$	$\infty 013$
$\Omega=\infty0123456$	$\infty 356$	$\infty 146$	$\infty 125$	1236	$\infty 234$	1345	2456.

The resulting systems are seven of the sixteen orders ... the seven maximal ones ... The intersections of pairs of these, which are also the intersections of certain triples, yield the seven "double Hurwitzian" systems. (The halving-sets 0, S2, oc124, 0356 for the typical one of these show that it is obtained by Dickson doubling from a Hurwitzian ring of quaternions.) The intersection of all seven maximal systems, which is equally the intersection of any two of the double Hurwitzian systems, we call the Kleinian octaves, since they can be obtained from Graves's integer octaves by adjoining (1/2) (1 + i0 + ... + (1/2) (1 + sqrt(-7)), + i6), which ... is a "Kleinian" integer ...

the number of vectors in E8 of norm 2n > 0 is 240 times the sum of the cubes of the divisors of n

• • •

a primitive octavian integer p of norm mn has precisely

240 left-hand divisors of norm m

and 240 right-hand divisors of norm n,

each set geometrically similar to the 240 units of O8 ...

This result is analogous to the result ... for the Hurwitz integers, except that in O8,

the factorizations are not unique "up to unit-migration" in view of the lack of associativity ... the set of left-hand divisors of a given octavian integer is geometrically similar to the set of all octavian integers of a certain norm

....

Theorem 7. The number of factorizations of a primitive octavian,

say Q = ((P1 P2) (P3 (P4 ... Pk))),

modelled on a given factorization of its norm is 240^(k-1).

Moreover, if all but Pi and Pj are fixed,

then the sets of values for Pi and Pj are geometrically similar to the set of 240 units. ...".

Appendix - Grothendieck Universe Quantum Theory and Code

The First Grothendieck Universe is the Empty Set.

The Second Grothendieck Universe is Hereditarily Finite Sets such as a Generalized Feynman Checkerboard Quantum Theory based on E8 Lattices and Discrete Cl(1,25) Clifford Algebra. (see viXra 1501.0078)

The Third Grothendieck Universe is the Completion of Union of all tensor products of Cl(1,25) Real Clifford algebra

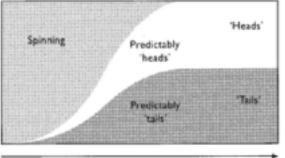
Since the Cl(1,25) E8 Lagrangian is Local and Classical, it is necessary to patch together Local Lagrangian Regions to form a Global Structure describing a Global Cl(1,25) E8 Algebraic Quantum Field Theory (AQFT).

The usual Hyperfinite II1 von Neumann factor for creation and annihilation operators on Fermionic Fock Space over C⁽²ⁿ⁾ is constructed by completion of the union of all tensor products of 2x2 Complex Clifford algebra matrices, which have Periodicity 2, so for the Cl(1,25) E8 model based on Real Clifford Algebras with Periodicity 8, Cl(1,25) = 2x2 matrices of Cl(0,24) where $Cl(0,24) = Cl(0,8) \times Cl(0,8)$,

the completion of the union of all tensor products of Cl(1,25) produces a generalized Hyperfinite II1 von Neumann factor that gives the Cl(1,25) E8 model a natural Algebraic Quantum Field Theory.

(see Chapter on E8 Quantum Theory)

The overall structure of CI(160-E8 AQFT is similar to the Many-Worlds picture described by David Deutsch in his 1997 book "The Fabric of Reality" said (pages 276-283): "... there is no fundamental demarcation between snapshots of other times and snapshots of other universes ... Other times are just special cases of other universes ... Suppose ... we toss a coin ... Each point in the diagram represents one snapshot



Increasing clock readings

... in the multiverse there are far too many snapshots for clock readings alone to locate a snapshot relative to the others. To do that, we need to consider the intricate detail of which snapshots determine which others. ...

in some regions of the multiverse, and in some places in space,

the snapshots of some physical objects do fall, for a period, into chains,

each of whose members determines all the others to a good approximation ...".

The Real Clifford Algebra Cl(1,25) containing E8 for the Local Lagrangian of a Region is equivalent to a " snapshot" of the Deutsch "multiverse".

The completion of the union of all tensor products of all Cl(1,25) E8 Local Lagrangian Regions forms a generalized hyperfinite II1 von Neumann factor AQFT and emergently self-assembles into a structure = Deutsch multiverse.

For the Cl(1,25) E8 model AQFT to be realistic, it must be consistent with **EPR entanglement relations**. Joy Christian in arXiv 0904.4259 said: "... a [geometrically] correct local-realistic framework ... provides exact, deterministic, and local underpinnings ... The alleged non-localities ... result from misidentified [geometries] of the EPR elements of reality. ... The correlations are ... the classical correlations [such as those] among the points of a 3 or 7-sphere ... S3 and S7 ... are ... parallelizable ... The correlations ... can be seen most transparently in the elegant language of Clifford algebra ...". Since E8 is a Lie Group and therefore parallelizable and lives in Clifford Algebra Cl(1,25), **the Cl(1,25) E8 model is consistent with EPR**.

The Creation-Annihilation Operator structure of CI(1,25) E8 AQFT is given by the

Maximal Contraction of E8 = semidirect product A7 x h92 where h92 = 92+1+92 = 185-dim Heisenberg algebra and A7 = 63-dim SL(8) The Maximal E8 Contraction A7 x h92 can be written as a 5-Graded Lie Algebra 28 + 64 + (SL(8,R) + 1) + 64 + 28Central Even Grade 0 = SL(8,R) + 1 The 1 is a scalar and SL(8,R) = Spin(8) + Traceless Symmetric 8x8 Matrices, so SL(8,R) represents a local 8-dim SpaceTime in Polar Coordinates. Odd Grades -1 and +1 = 64 + 64 Each = 64 = 8x8 = Creation/Annihilation Operators for 8 components of 8 Fundamental Fermions. Even Grades -2 and +2 = 28 + 28 Each = Creation/Annihilation Operators for 28 Gauge Bosons of Gravity + Standard Model.

The Cl(1,25) E8 AQFT inherits structure from the Cl(1,25)- 8 Local Lagrangian

Gauge Gravity + Standard Model + Fermion Particle-AntiParticle 8-dim SpaceTime

The Cl(1,25)-E8 generalized Hyperfinite II1 von Neumann factor Algebraic Quantum Field Theory is based on the Completion of the Union of all Tensor Products of the form

CI(1,25) x ...(N times tensor product)... x CI(1,25)

For $N = 2^8 = 256$ the copies of Cl(1,25) are on the 256 vertices of the 8-dim HyperCube



For $N = 2^{16} = 65,536 = 4^{8}$ the copies of Cl(1,25) fill in the 8-dim HyperCube as described by William Gilbert's web page: "... The n-bit reflected binary Gray code will describe a path on the edges of an n-dimensional cube that can be used as the initial stage of a Hilbert curve that will fill an n-dimensional cube. ...".

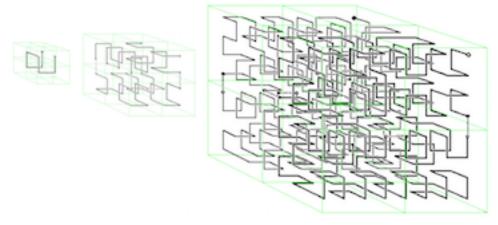
The vertices of the Hilbert curve are at the centers of the 2⁸ sub-8-HyperCubes whose edge lengths are 1/2 of the edge lengths of the original 8-dim HyperCube

As N grows, the copies of Cl(1,25) continue to fill the 8-dim HyperCube of E8 SpaceTime

using higher Hilbert curve stages from the 8-bit reflected binary Gray code subdividing the initial 8-dim HyperCube into more and more sub-HyperCubes.

If edges of sub-HyperCubes, equal to the distance between adjacent copies of Cl(1,25), remain constantly at the Planck Length, then the

full 8-dim HyperCube of our Universe expands as N grows to 2^16 and beyond similarly to the way shown by this 3-HyperCube example for N = 2^3, 4^3, 8^3 from Wiliam Gilbert's web page:



The Union of all Cl(1,25) tensor products is the Union of all subdivided 8-HyperCubes

and

their Completion is a huge superposition of 8-HyperCube Continuous Volumes which Completion belongs to the Third Grothendieck Universe. AQFT Quantum Code

Cerf and Adami in quantum-ph/9512022 describe virtual qubit-anti-qubit pairs (they call them ebit-anti-ebitpairs) that are related to negative conditional entropies for quantum entangled systems and are similar to fermion particle-antiparticle pairs. Therefore quantum information processes can be described by particle-antiparticle diagrams much like particle physics diagrams and **the Algebraic Quantum Field Theory of the Cl(1,25) E8 Physics Model should have a Quantum Code Information System** that is **based on structure of a unit cell in 26D String Theory** represented by **Real Clifford Algebra Cl(0,8) x Cl(0,8) x Cl(0,8) = Cl(0,24)** (see Appendix - Details of World-Line String Bohm Quantum Theory)

> Since Quantum Reed-Muller code [[256 , 0 , 24]] corresponds to Real Clifford Algebra Cl(0,8)

Tensor Product Quantum Reed-Muller code [[256,0,24]] x [[256,0,24]] x [[256,0,24]] corresponds to AQFT (Algebraic Quantum Field Theory) hyperfinite von Neumann factor algebra that is Completion of the Union of All Tensor Products of Cl(1,25)

Quantum Reed-Muller code [[256 , 0 , 24]] is described in quantum-ph/9608026 by Steane as mapping a quantum state space of 256 qubits into 256 qubits, correcting [(24-1)/2] = 11 errors, and detecting 24/2 = 12 errors. Let C(n,t) = n! / t! (n-t)!Then

[[256, 0, 24]] is of the form

 $\begin{bmatrix} 2^n, & 2^n - C(n,t) - 2 & SUM(0 & t-1) & C(n,k), & 2^t + 2^t(t-1) \end{bmatrix} \\ \begin{bmatrix} 2^n, & 2^n - C(8,4) - 2 & SUM(0 & k & 3) & C(8,k), & 2^t + 2^t(4-1) \end{bmatrix} \\ \begin{bmatrix} 2^n, & 2^n - C(8,4) - 2 & SUM(0 & k & 3) & C(8,k), & 2^t + 2^t(4-1) \end{bmatrix} \\ \begin{bmatrix} 2^n, & 2^n - C(8,4) - 2 & SUM(0 & k & 3) & C(8,k), & 2^t + 2^t(4-1) \end{bmatrix} \\ \begin{bmatrix} 2^n, & 2^n - C(8,4) - 2 & SUM(0 & k & 3) & C(8,k), & 2^t + 2^t(4-1) \end{bmatrix} \\ \begin{bmatrix} 2^n, & 2^n - C(8,4) - 2 & SUM(0 & k & 3) & C(8,k), & 16 + 8 \end{bmatrix} \\ \begin{bmatrix} 2^n, & 2^n - C(8,4) - 2 & SUM(0 & k & 3) & C(8,k), & 16 + 8 \end{bmatrix} \\ \begin{bmatrix} 2^n, & 2^n - C(8,4) - 2 & SUM(0 & k & 3) & C(8,k), & 16 + 8 \end{bmatrix} \\ \begin{bmatrix} 2^n, & 2^n - C(8,4) - 2 & SUM(0 & k & 3) & S/(8/k), & 16 + 8 \end{bmatrix} \\ \end{bmatrix}$

The quantum code [[256, 0, 24]] can be constructed from the classical Reed-Muller code (256, 93, 32) of the form

(2^8,	2^8 - SUM(0 k t) C(n,k),	2^(t+1))
(2^8,	2^8 - SUM(0 k 4) C(n,k),	2^5)
(2^8,	2^8 - (70+56+28+8+1),	32)
(2^8,	1+8+28+56,	32)

To construct the quantum code [[256, 0, 24]] :

First, form a quantum code generator matrix from the 128x256 generator matrix G of the classical code (256, 93, 32) :

| G | O | | 0 | G | | 0 | 1 G |

Second, form the generator matrix of a quantum code of distance 16 by adding to the quantum generator matrix a matrix Dx such that G and Dx together generate the classical Reed-Muller code (256, 163, 16) :

```
( 2^8, 1+8+28+56+70, 16):
```

G	0
0	G
Dx	0

This quantum code has been made by combining the classical codes (256, 93, 32) and (256, 163, 16), so that it is of the form [[256, 93 + 163 - 256, min(32, 16)]] = [[256, 0, 16]].

It is close to what we want, but has distance 16. For the third and final step, increase the distance to 16+8 = 24 by adding Dz to the quantum generator matrix:

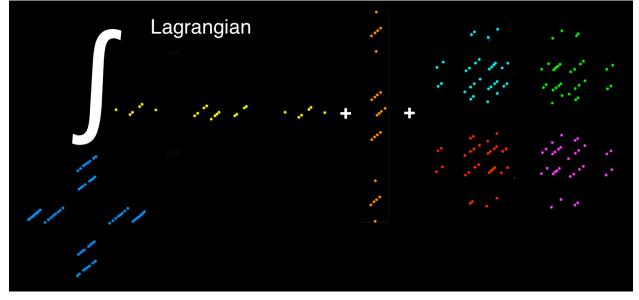
G	0
0	G
Dx	Dz

This is the generator matrix of the quantum code [[256, 0, 24]] as constructed by Steane.

The two classical Reed-Muller codes used to build [[256, 0, 24]] are (256, 163, 32) and (256, 93, 16), classical Reed-Muller codes of orders 4 and 3, which are dual to each other. Due to the nested structure of Reed-Muller codes, they contain the Reed-Muller codes of orders 2, 1, and 0 :

		Classical Reed-Muller Codes of Length 2^8 = 256			Order
(256,	1+8+28+56+70+56+28+8+1,	1)	8
(256,	1+8+28+56+70+56+28+8,	2)	7
(256,	1+8+28+56+70+56+28,	4)	6
(256,	1+8+28+56+70+56,	8)	5
(256,	1+8+28+56+70,	16)	4
(256,	1+8+28+56,	32)	3
(256,	1+8+28,	64)	2
(256,	1+8,	128)	1
(256,	1,	256)	0

In the Lagrangian of the Cl(1,25) E8 Physics Model



the Higgs scalar prior to dimensional reduction corresponds to the 0th order classical Reed-Muller code (256, 1, 256), the classical repetition code;

the 8-dimensional vector spacetime

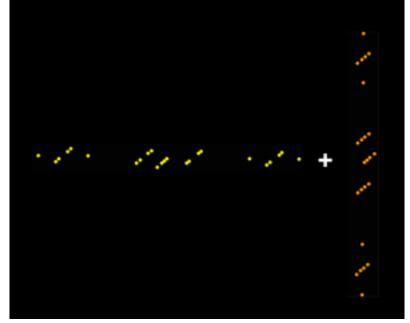


prior to dimensional reduction corresponds to non-0th-order part of the 1st order classical Reed-Muller code (256, 9, 128),

which is dual to the 6th order classical Reed-Muller code (256, 247, 4), which is the extended Hamming code,

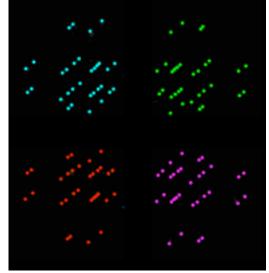
extended from the binary Hamming code (255, 247, 3), which is dual to the simplex code (255, 8, 128);

the 28-dimensional bivector adjoint gauge boson spaces



prior to dimensional reduction correspond to the non-1st-order part of the 2nd order classical Reed-Muller code (256, 37, 64) .

The 8 first generation fermion particles and 8 first generation fermion antiparticles of the 16-dim full spinor representation of the 256-dimensional Cl(0,8) Clifford algebra



correspond to the distance of the classical Reed-Muller code (256, 93, 16), and to the 16-dimensional Barnes-Wall lattice \wedge 16, which lattice comes from the (16,5,8) Reed-Muller code. Each \wedge 16 vertex has 4320 nearest neighbors.

The other 8 of the 16+8 = 24 distance of the quantum Reed-Muller code [[256, 0, 24]] corresponds to the 8-dimensional vector spacetime, and to the 8-dimensional E8 lattice which comes from the (8,4,4) Hamming code, with weight distribution 0(1) 4(14) 8(1). It can also be constructed from the repetition code (8,1,1). The dual of (8,1,1) is (8,7,2), a zero-sum even weight code, containing all binary vectors with an even number of 1s. Each E8 lattice vertex has 240 nearest neighbors. In Euclidean R8, there is only one way to arrange 240 spheres so that they all touch one sphere, and only one way to arrange 56 spheres so that they all touch a set of two spheres in contact with each other, and so forth, giving the following classical spherical codes: (8,240,1/2), (7,56,1/3), (6,27,1/4), (5,16,1/5), (4,10,1/6), and (3,6,1/7). (If you use an Octonion Integral Domain instead of Euclidean R8 without multiplication then there are 7 algebraically independent ways to arrange the 240 spheres.)

corresponds to the 24-dimensional Leech lattice,

and to the classical extended Golay code (24, 12, 8)

in which lattice each vertex has 196,560 nearest neighbors. In Euclidean R24,

there is only one way to arrange 196,560 spheres so that they all touch one sphere, and only one way to arrange 4600 spheres so that they all touch a set of two spheres in contact with each other, and so forth, giving the following classical spherical codes: (24,196560,1/2), (23,4600,1/3), (22,891,1/4), (21,336,1/5), (20,170,1/6),

Appendix - Details of World-Line String Bohm Quantum Theory

A physically realistic Lattice Bosonic String Theory with Strings = World-Lines and Monster Group Symmetry containing gravity and the Standard Model can be constructed consistently with the E8 physics model 248-dim E8 = 120-dim adjoint D8 + 128-dim half-spinor D8 = (28 + 28 + 64) + (64 + 64)

Paths in C8 / WE8 correspond to World-Lines of Observers acting as Bosonic Strings. Andrew Gray in arXiv quant-ph/9712037 said:

"... probabilites are ... assigned to entire fine-grained histories ...

base[d] ... on the Feynman path integral formulation ...

The formulation is fully relativistic and applicable to multi-particle systems.

It ... makes the same experimental predictions as quantum field theory ...".

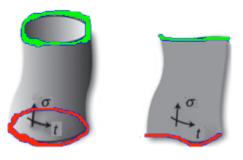
Luis E. Ibanez and Angel M. Uranga in "String Theory and Particle Physics" said:

"... String theory proposes ... small one-dimensional extended objects, strings,

of typical size Ls = 1/ Ms, with Ms known as the string scale ...

As a string evolves in time, it sweeps out a two-dimensional surface in spacetime, known as the worldsheet, which is the analog of the ... worldline of a point particle ... for the bosonic string theory ... the classical string action is the total area spanned by the worldsheet ... This is the ... Nambu– Goto action ...".

In my unconventional view



the red line and the green line are different strings/worldlines/histories and the world-sheet is the minimal surface connecting them, carrying the Bohm Potential,

as Standard Model gauge bosons carry Force Potential between Point Particles. The t world-sheet coordinate is for Time of the string-world-line history. The sigma world-sheet coordinate is for Bohm Potential Gauge Boson at a given Time.

(images adapted from "String Theory and Particle Physics" by Ibanez and Uranga)

Further, Ibanez and Uranga also said:

"... The string groundstate corresponds to a 26d spacetime tachyonic scalar field T(x). This **tachyon** ... is ... unstable

••••

The massless two-index tensor splits into irreducible representations of SO(24) ... Its **trace** corresponds to a scalar field, the **dilaton** ϕ , whose vev fixes the string interaction coupling constant gs

the antisymmetric part is the 26d 2-form field BMN

•••

The symmetric traceless part is the 26d graviton GMN ...".

Closed string **tachyons** localized at orbifolds of fermions produce virtual clouds of particles / antiparticles that dress fermions.

Dilatons are Goldstone bosons of spontaneously broken scale invariance that (analagous to Higgs) go from mediating a long-range scalar gravity-type force to the nonlocality of the Bohm-Sarfatti Quantum Potential.

The **antisymmetric** SO(24) little group is related to the Monster automorphism group that is the symmetry of each cell of Planck-scale local lattice structure.

Joe Polchinski in "String Theory, Volume 1, An Introduction to the Bosonic String" said: "... we find at $m^2 = -4$ / alpha' the tachyon,

and at m² = 0 the 24 x 24 states of the graviton, dilaton, and antisymmetric tensor ...".

Must the 24x24 symmetric matrices be interpreted as the graviton ? - !!! NO !!!

The 24x24 Real Symmetric Matrices form the Jordan Algebra J(24,R).

Jordan algebras correspond to the matrix algebra of quantum mechanical states, that is, from a particle physics point of view, the configuration of particles in spacetime upon which the gauge groups act.

24-Real-dim space has a natural Octonionic structure of 3-Octonionic-dim space.

The corresponding Jordan Algebra is J(3,O) = 3x3 Hermitian Octonion matrices.

Their 26-dim traceless part J(3,O)o describes the 26-dim of Bosonic String Theory

and

the algebra of its Quantum States,

so that

the 24x24 traceless symmetric spin-2 particle is the Quantum Bohmion.

Joseph Polchinski, in his books String Theory vols. I and II(Cambridge 1998), says: "... the **closed** ... **unoriented** ... **bosonic string** ... **theory** has the maximal 26dimensional Poincare invariance ... It is possible to have a consistent theory ...[with]... the **dilaton** ... the [**string-]graviton** ...[and]... the **tachyon** ...[whose]... negative masssquared means that the no-string 'vacuum' is actually unstable ... ". The **dilaton** of E8 Physics sets the Planck scale as the scale for the 16 dimensions that are orbifolded fermion particles and anti-particles and the 4 dimensions of the CP2 Internal Symmetry Space of M4xCP2 spacetime. The remaining 26-16-4 = 6 dimensions are the Conformal Physical Spacetime with Spin(2,4) = SU(2,2) symmetry that produces M4 Physical Spacetime. The **string-graviton** of E8 Physics is a spin-2 interaction among strings. If Strings = World Lines and World Lines are past and future histories of particles, then string-graviton interactions determine a Cramer Transaction Quantum Theory discussed in quantum-ph/0408109.

Roger Penrose in "Road to Reality" (Knopf 2004) says: "... **quantum** mechanics ... alternates between ... **unitary** evolution **U** ... and state reduction R ...

quantum state reduction ... is ... objective ... OR ...

it is always a gravitational phenomenon ... [A] conscious event ... would be ... orchestrated OR ... of ... large-scale quantum coherence ... of ... microtubules ...".

String-Gravity produces Sarfatti-Bohm Quantum Potential with Back-Reaction.

It is distinct from the MacDowell-Mansouri Gravity of stars and planets. The **tachyon** produces the instability of a truly empty vacuum state with no strings. It is natural, because if our Universe were ever to be in a state with no strings, then tachyons would create strings = World Lines thus filling our Universe with the particles and World-Lines = strings that we see. Something like this is necessary for particle creation in the Inflationary Era of non-unitary Octonionic processes. Our construction of a 26D String Theory consistent with E8 Physics uses a structure that is not well-known, so I will mention it here before we start:

There are 7 independent E8 lattices, each corresponding to one of the 7 imaginary octionions denoted by iE8, jE8, kE8, EE8, IE8, JE8, and KE8 and related to both D8 adjoint and half-spinor parts of E8 and with 240 first-shell vertices. An 8th E8 lattice 1E8 with 240 first-shell vertices related to the D8 adjoint part of E8 is related to the 7 octonion imaginary lattices (viXra 1301.0150v2).

It can act as an effectively independent lattice as part of the basis subsets {1E8,EE8} or {1E8,iE8,jE8,kE8}.

With that in mind, here is the construction:

Step 1: Consider the 26 Dimensions of Bosonic String Theory as the 26-dimensional traceless part J3(O)o

a O+ Ov O+* b O-

Ov* O-* -a-b

(where Ov, O+, and O- are in Octonion space with basis $\{1,i,j,k,E,I,J,K\}$ and a and b are real numbers with basis $\{1\}$) of the 27-dimensional Jordan algebra J3(O) of 3x3 Hermitian Octonion matrices.

Step 2:

Take a D3 brane to correspond to the Imaginary Quaternionic associative subspace spanned by {i,j,k} in the 8-dimenisonal Octonionic Ov space.

Step 3:

Compactify the 4-dimensional co-associative subspace spanned by $\{E,I,J,K\}$ in the Octonionic Ov space as a CP2 = SU(3)/U(2), with its 4 world-brane scalars corresponding to the 4 covariant components of a Higgs scalar. Add this subspace to D3, to get D7.

Step 4:

Orbifold the 1-dimensional Real subspace spanned by {1} in the Octonionic Ov space by the discrete multiplicative group $Z2 = \{-1,+1\}$, with its fixed points $\{-1,+1\}$ corresponding to past and future time. This discretizes time steps and gets rid of the world-brane scalar corresponding to the subspace spanned by {1} in Ov. It also gives our brane a 2-level timelike structure, so that its past can connect to the future of a preceding brane and its future can connect to the past of a succeeding brane. Add this subspace to D7, to get D8.

D8, our basic Brane, looks like two layers (past and future) of D7s.

Beyond D8 our String Theory has 26 - 8 = 18 dimensions, of which 25 - 8 have corresponding world-brane scalars:

8 world-brane scalars for Octonionic O+ space;

8 world-brane scalars for Octonionic O- space;

1 world-brane scalars for real a space; and

1 dimension, for real b space, in which the D8 branes containing spacelike D3s are stacked in timelike order.

Step 5:

To get rid of the world-brane scalars corresponding to the Octonionic O+ space, orbifold it by the 16-element discrete multiplicative group

 $Oct16 = \{+/-1, +/-i, +/-j, +/-k, +/-E, +/-I, +/-J, +/-K\}$ to reduce O+ to 16 singular points {-1,-i,-j,-k,-E,-I,-J,-K,+1,+i,+j,+k,+E,+I,+J,+K}.

Let the 8 O+ singular points {-1,-i,-j,-k,-E,-I,-J,-K} correspond to

the fundamental fermion particles

{neutrino, red up quark, green up quark, blue up quark,

electron, red down quark, green down quark, blue down quark} located on the past D7 layer of D8.

Let the 8 O+ singular points {+1,+i,+j,+k,+E,+l,+J,+K} correspond to the fundamental fermion particles {neutrino, red up quark, green up quark, blue up quark, electron, red down quark, green down quark, blue down quark} located on the future D7 layer of D8.

The 8 components of the 8 fundamental first-generation fermion p articles = 8x8 = 64 correspond to the 64 of the 128-dim half-spinor D8 part of E8. This gets rid of the 8 world-brane scalars corresponding to O+, and leaves:

8 world-brane scalars for Octonionic O- space;

1 world-brane scalars for real a space; and

1 dimension, for real b space, in which the D8 branes containing spacelike D3s are stacked in timelike order.

Step 6:

To get rid of the world-brane scalars corresponding to the Octonionic O- space, orbifold it by the 16-element discrete multiplicative group

 $Oct16 = \{+/-1, +/-i, +/-j, +/-k, +/-E, +/-I, +/-J, +/-K\}$ to reduce O- to 16 singular points {-1,-i,-j,-k,-E,-I,-J,-K,+1,+i,+j,+k,+E,+I,+J,+K}.

Let the 8 O- singular points {-1,-i,-j,-k,-E,-I,-J,-K} correspond to the fundamental fermion anti-particles {anti-neutrino, red up anti-quark, green up anti-quark, blue up anti-quark, positron, red down anti-quark, green down anti-quark, blue down anti-quark} located on the past D7 layer of D8.

Let the 8 O- singular points {+1,+i,+j,+k,+E,+I,+J,+K} correspond to the fundamental fermion anti-particles {anti-neutrino, red up anti-quark, green up anti-quark, blue up anti-quark, positron, red down anti-quark, green down anti-quark, blue down anti-quark} located on the future D7 layer of D8.

The 8 components of 8 fundamental first-generation fermion anti-particles = 8x8 = 64 correspond to the 64 of the 128-dim half-spinor D8 part of E8. This gets rid of the 8 world-brane scalars corresponding to O-, and leaves: 1 world-brane scalars for real a space; and 1 dimension, for real b space, in which the D8 branes containing spacelike D3s are stacked in timelike order.

Step 7:

Let the 1 world-brane scalar for real a space correspond to a Bohm-type Quantum Potential acting on strings in the stack of D8 branes. Interpret strings as world-lines in the Many-Worlds, short strings representing virtual

particles and loops.

Step 8:

Fundamentally, physics is described on HyperDiamond Lattice structures. There are 7 independent E8 lattices, each corresponding to one of the 7 imaginary octionions. denoted by iE8, jE8, kE8, EE8, IE8, JE8, and KE8 and related to both D8 adjoint and half-spinor parts of E8 and with 240 first-shell vertices. An 8th 8-dim lattice 1E8 with 240 first-shell vertices related to the E8 adjoint part of E8 is related to the 7 octonion imaginary lattices. Give each D8 brane structure based on Planck-scale E8 lattices so that each D8 brane is a superposition/intersection/coincidence of the eight E8 lattices. (see viXra 1301.0150)

Step 9:

Since Polchinski says "... If r D-branes coincide ... there are r^2 vectors, forming the adjoint of a U(r) gauge group ...", make the following assignments:

a gauge boson emanating from D8 from its 1E8 and EE8 lattices is a U(2) ElectroWeak boson thus accounting for the photon and W+, W- and Z0 bosons.

a gauge boson emanating from D8 from its IE8, JE8, and KE8 lattices is a U(3) Color Gluon boson thus accounting for the 8 Color Force Gluon bosons.

The 4+8 = 12 bosons of the Standard Model Electroweak and Color forces correspond to 12 of the 28 dimensions of 28-dim Spin(8) that corresponds to one of the 28 of the 120-dim adjoint D8 parts of E8.

a gauge boson emanating from D8 from its 1E8, iE8, jE8, and kE8 lattices is a U(2,2) boson for conformal U(2,2) = Spin(2,4)xU(1) MacDowell-Mansouri gravity plus conformal structures consistent with the Higgs mechanism and with observed Dark Energy, Dark Matter, and Ordinary matter.

The 16-dim U(2,2) is a subgroup of 28-dim Spin(2,6) that corresponds to the other 28 of the 120-dim adjoint D8 part of E8.

Step 10: Since Polchinski says

"... there will also be r^2 massless scalars from the components normal to the D-brane. ... the collective coordinates ... X⁴u ... for the embedding of n D-branes in spacetime are now enlarged to nxn matrices.

This 'noncummutative geometry' ... [may be]... an important hint about the nature of spacetime. ...",

make the following assignment:

The 8x8 matrices for the collective coordinates linking a D8 brane to the next D8 brane in the stack are needed to connect the eight E8 lattices of the D8 brane to the eight E8 lattices of the next D8 brane in the stack.

The 8x8 = 64 correspond to the 64 of the 120 adjoint D8 part of E8.

We have now accounted for all the scalars

and

have shown that the model has the physics content of the realistic E8 Physics model with Lagrangian structure based on E8 = (28 + 28 + 64) + (64 + 64) and

AQFT structure based on CI(1,25) with real Clifford Algebra periodicity and generalized Hyperfinite II1 von Neumann factor algebra.

A Single Cell of E8 26-dimensional Bosonic String Theory, in which Strings are physically interpreted as World-Lines, can be described by taking the quotient of its 24-dimensional O+, O-, Ov subspace modulo the 24-dimensional Leech lattice. Its automorphism group is the largest finite sporadic group, the Monster Group, whose order is 8080, 17424, 79451, 28758, 86459, 90496, 17107, 57005, 75436, 80000, 00000

> = 2^46 .3^20 .5^9 .7^6 .11^2 .13^3 .17.19.23.29.31.41.47.59.71 or about 8 x 10^53.

A Leech lattice construction is described by Robert A. Wilson in his 2009 paper "Octonions and the Leech lattice":

"... The (real) octonion algebra is an 8-dimensional (non-division) algebra with an orthonomal basis { 1=ioo, i0, i1, i2, i3, i4, i5, i6 } labeled by the projective line PL(7) = { oo } u F7

The E8 root system embeds in this algebra ... take the 240 roots to be ... 112 octonions ... +/- it +/- iu for any distinct t,u ... and ... 128 octonions (1/2)(+/- 1 +/- i0 +/- ... +/- i6) which have an odd number of minus signs.

Denote by L the lattice spanned by these 240 octonions

Let s = (1/2)(-1 + i0 + ... + i6) so s is in L ... write R for Lbar ...

(1/2) (1 + i0) L = (1/2) R (1 + i0) is closed under multiplication ... Denote this ...by A ... Writing B = (1/2) (1 + i0) A (1 + i0) ...from ... Moufang laws ... we have L R = 2 B, and ... B L = L and R B = R ...[also]... 2 B = L sbar

the roots of B are [16 octonions]... +/- it for t in PL(7) ... together with [112 octonions]... (1/2) (+/- 1 +/- it +/- i(t+1) +/- i(t+3)) ...for t in F7 ... and ... [112 octonions]... (1/2) (+/- i(t+2) +/- i(t+4) +/- i(t+5) +/- i(t+6)) ...for t in F7

the octonionic Leech lattice ... contains the following 196560 vectors of norm 4, where M is a root of L and j,k are in $J = \{ +/- it \mid t \text{ in } PL(7) \}$, and all permutations of the three coordinates are allowed:

 (2 M, 0, 0)
 Number: 3x240 = 720

 (M sbar, +/- (M sbar) j, 0)
 Number: 3x240 x 16 = 11520

 ((M s) j, +/- M k, +/- (M j) k)
 Number: 3x240 x 16 x 16 = 184320

The key to the simple proofs above is the observation that LR = 2B and BL = L: these remarkable facts appear not to have been noticed before ... some work ... by Geoffrey Dixon ...". Geoffrey Dixon says in his book "Division Algebras, Lattices, Physics, Windmill Tilting" using notation {e0,e1,e2,e3,e4,e5,e6,e7} for the Octonion basis elements that Robert A. Wilson denotes by {1=ioo,i0,i1,i2,i3,i4,i5,i6} and I often denote by {1,i,j,k,E,I,J,K}: "...

$$\begin{split} \Xi_0 &= \{\pm e_a\},\\ \Xi_2 &= \{(\pm e_a \pm e_b \pm e_c \pm e_d)/2 : a, b, c, d \text{ distinct},\\ e_a(e_b(e_c e_d)) &= \pm 1\}, \end{split}$$

$$\begin{split} \Xi^{even} &= \Xi_0 \cup \Xi_2,\\ \mathcal{E}_8^{even} &= \text{span}\{\Xi^{even}\},\\ \Xi_1 &= \{(\pm e_a \pm e_b)/\sqrt{2} : a, b \text{ distinct}\},\\ \Xi_3 &= \{(\sum_{a=0}^7 \pm e_a)/\sqrt{8} : \text{ even number of +'s}\},\\ \Xi^{odd} &= \Xi_1 \cup \Xi_3,\\ \mathcal{E}_8^{odd} &= \text{span}\{\Xi^{odd}\} \end{split}$$

(spans over integers) ...

Eeven has 16+224 = 240 elements ... Eodd has 112+128 = 240 elements ... E8even does not close with respect to our given octonion multiplication ...[but]... the set Eeven[0-a], derived from Eeven by replacing each occurrence of e0 ... with ea, and vice versa, is multiplicatively closed. ...".

Geoffrey Dixon's Eeven corresponds to B

Geoffrey Dixon's Eeven[0-a] corresponds to the seven At

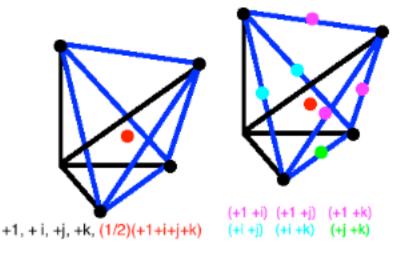
Geoffrey Dixon's Eodd corresponds to L

Ignoring factors like 2 , j , k , and +/-1 the Leech lattice structure is:

(L,0,0)	Number: 3x240 = 720
(B,B,0)	Number: 3x240 x 16 = 11520
(Ls,L,L)	Number: 3x240 x 16 x 16 = 184320
(Number: 3x240 = 720 Number: 3x240 x 16 = 11520 Number: 3x240 x 16 x 16 = 184320

My view is that **the E8 domain B is fundamental** and the E8 domains L and L s are derived from it.

That view is based on analogy with the 4-dimensional 24-cell and its dual 24-cell. Using Quaternionic coordinates {1,i,j,k} the 24-cell of 4-space has one Superposition Vertex for each 16-region of 4-space. A Dual 24-cell gives a new Superposition Vertex at each edge of the region.



The Initial 24-cell Quantum Operators act with respect to 4-dim Physical Spacetime. {1,i,j,k} represent time and 3 space coordinates.

(1/2)(+1+i+j+k) represents a fundamental first-generation Fermion particle/antiparticle (there is one for for each of the 16-regions).

The Dual 24-cell Quantum Operators act with respect to 4-dim CP2 Internal Symmetry Space. Since CP2 = SU(3)/SU(2)xU(1),

(+1 +i) (+1 +j) (+1 +k) are permuted by S3 to form the Weyl Group of Color Force SU(3), (+i +i) (+i +k) are permuted by S2 to form the Weyl Group of Weak Force SU(2),

(+j +k) is permuted by S1 to form the Weyl Group of Electromagnetic Force U(1).

The B-type 24-cell is fundamental because it gives Fundamental Fermions.

The L-type dual 24-cell is derivative because it gives Standard Model Gauge Bosons.

Robert A.Wilson in "Octonions and the Leech lattice" also said

"... B is not closed under multiplication ... Kirmse's mistake

...[but]... as Coxeter ... pointed out ...

... there are seven non-associative rings At = (1/2)(1 + it)B(1 + it), obtained from B by swapping 1 with it ... for t in F7 ...".

H. S. M. Coxeter in "Integral Cayley Numbers" (Duke Math. J. 13 (1946) 561-578) said "... Kirmse ... defines ... an integral domain ... which he calls J1 [Wilson's B] ...[but]... J1 itself is not closed under multiplication ... Bruck sent ... a revised description ...[of a]... domain J ... derived from J1 by transposing two of the i's [imaginary Octonions]... It is closed under multiplication ... there are ... seven such domains, since the (7choose2) = 21 possible transpositions fall into 7 sets of 3, each set having the same effect. In each of the seven domains, one of the ... seven i's ... plays a special role, viz., that one which is not affected by any of the three transpositions. ... J contains ... 240 units ... ". J is one of Wilson's seven At and, in Octonionic coordinates {1,i,j,k,e,ie,je,ke}, is shown below with physical interpretation color-coded as 8-dim Spacetime Coordinates x 8-dim Momentum Dirac Gammas Gravity SU(2,2)=Spin(2,4) in a D4 + Standard Model SU(3)xU(2) in a D4 8 First-Generation Fermion Particles x 8 Coordinate Components

8 First-Generation Fermion AntiParticles x 8 Coordinate Components

112 = (16+48=64) + (24+24=48) Root Vectors corresponding to D8: ±1, ±i, ±j, ±k, ±e, ±ie, ±je, ±ke, tie (±1 ±i ±e)/2)/2 (±1 ±j ±е ±je $\pm ke$)/2 (±1 ±k ±e ±j ±k ±je ±ke)/2 (±i $\pm ke$)/2 (±k tie ±i ±j ±ie <u>±je</u>)/2 (128 = 64 + 64 Root Vectors corresponding to half-spinor of D8: tie (±1 tje ±ke)/2 (±1 tie)/2 ±j ±k)/2 (±1 ±i ±k tje (±1 ±i ±ke)/2 ±j ±i ±j ±k ±е)/2 ((±i ±e ±je $\pm ke$)/2 ±j ±е tie $\pm ke$)/2 (tie)/2 ±k ±е tje (

The above Coxeter-Bruck J is, in the notation I usually use, denoted 7E8. It is one of Coxeter's seven domains (Wilson's seven {A0,A1,A2,A3,A4,A5,A6}) that I usually denote as { 1E8, 2E8, 3E8, 4E8, 5E8, 6E8, 7E8 }.

Since the Leech lattice structure is

(L,0,0)	Number: 3x240 = 720
(B,B,0)	Number: 3x240 x 16 = 11520
(Ls,L,L)	Number: $3x240 \times 16 \times 16 = 184320$

if you replace the structural B with 7E8 and the Leech lattice structure becomes

(L,0,0)	Number: 3x240 = 720
(7E8,7E8,0)	Number: $3x240 \times 16 = 11520$
(Ls ,L ,L)	Number: $3x240 \times 16 \times 16 = 184320$

and the Leech lattice of E8 26-dim String Theory is the Superposition of 8 Leech lattices based on each of { B, 1E8, 2E8, 3E8, 4E8, 5E8, 6E8, 7E8 } just as the D8 branes of E8 26-dim String Theory are each the Superposition of the 8 domains { B, 1E8, 2E8, 3E8, 4E8, 5E8, 6E8, 7E8 }.

What happens to a Fundamental Fermion Particle whose World-Line string intersects a Single Cell ?

The Fundamental Fermion Particle does not remain a single Planck-scale entity. **Tachyons create clouds of particles/antiparticles** as described by Bert Schroer in hep-th/9908021: "... any compactly localized operator applied to the vacuum generates clouds of pairs of particle/antiparticles ... More specifically it leads to the impossibility of having a local generation of pure one-particle vectors unless the system is interaction-free ...".

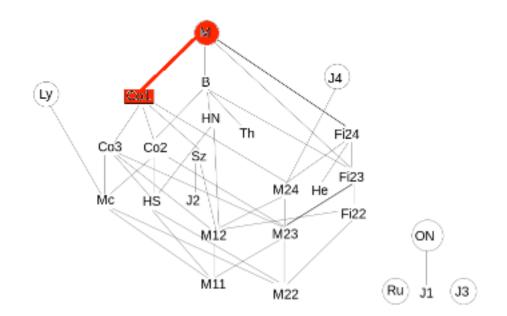
What is the structural form of the Fundamental Fermion Cloud ?

In "**Kerr-Newman [Black Hole]** solution as a Dirac particle", hep-th/0210103, H. I. Arcos and J. G. Pereira say: "... For $m^2 < a^2 + q^2$, with m, a, and q respectively the source mass, angular momentum per unit mass, and electric charge, the Kerr-Newman (KN) solution of Einstein's equation reduces to a naked singularity of circular shape, enclosing a disk across which the metric components fail to be smooth ... due to its topological structure, the extended KN spacetime does admit states with half-integral angular momentum. ... The state vector ... evolution is ... governed by the Dirac equation. ... for symmetry reasons, the electric dipole moment of the KN solution vanishes identically, a result that is within the limits of experimental data ... a and m are thought of as parameters of the KN solution, which only asymptotically correspond respectively to angular momentum per unit mass and mass. Near the singularity, a represents the radius of the singular ring ... With ... renormalization ... for the usual scattering energies, the resulting radius is below the experimental limit for the extendedness of the electron ...".

What is the size of the Fundamental Fermion Kerr-Newman Cloud ?

The FFKN Cloud is one Planck-scale Fundamental Fermion Valence Particle plus an effectively neutral cloud of particle/antiparticle pairs. The symmetry of the cloud is governed by the 24-dimensional Leech lattice by which the Single Cell was formed.

Here (adapted from Wikipedia) is a chart of the Monster M and its relation to other Sporadic Finite Groups and some basic facts and commentary:



The largest such subgroups of M are B, Fi24, and Co1.

B, the Baby Monster, is sort of like a downsized version of M, as B contains Co2 and Fi23 while M contains Co1 and Fi24.

Fi24 (more conventionally denoted Fi24') is of order $1255205709190661721292800 = 1.2 \times 10^{24}$ It is the centralizer of an element of order 3 in the monster group M and is a triple cover of a 3-transposition group. It may be that Fi24' symmetry has its origin in the Triality of E8 26-dim String Theory.

The order of Co1 is 2^21.3^9.5^4.7^2.11.13.23 or about 4 x 10^18.

Aut(Leech Lattice) = double cover of Co1.

The order of the double cover 2.Co1 is $2^22.3^9.5^4.7^2.11.13.23$ or about 0.8 x 10^19. Taking into account the non-sporadic part of the Leech Lattice symmetry according to the ATLAS at brauer.maths.qmul.ac.uk/Atlas/v3/spor/M/ the maximal subgroup of M involving Co1 is $2^(1+24)$.Co1 of order 139511839126336328171520000 = 1.4×10^{26}

As 2.Co1 is the Automorphism group of the Leech Lattice modulo to which the Single Cell was formed, and as

the E8 26-dim String Theory Leech Lattice is a superposition of 8 Leech Lattices, 8 x 2^(1+24).Co1 describes the structure of the FFKN Cloud. Therefore, the volume of the FFKN Cloud should be on the order of 10^27 x Planck scale, and the FFKN Cloud should contain on the order of 10^27 particle/antiparticle pairs and its size should be somewhat larger than, but roughly similar to, $10^{(27/3)} \times 1.6 \times 10^{(-33)}$ cm = roughly $10^{(-24)}$ cm.

The full 26-dimensional Lattice Bosonic String Theory can be regarded as an infinite-dimensional Affinization of the Theory of a Single Cell.

James Lepowsky said in math.QA/0706.4072:

"... the Fischer-Griess Monster M ... was constructed by Griess as a symmetry group (of order about 10^54) of a remarkable new commutative but very, very highly nonassociative, seemingly ad-hoc, algebra B of dimension 196,883. The "structure constants" of the Griess algebra B were "forced" by expected properties of the conjectured-to-exist Monster. It was proved by J. Tits that M is actually the full symmetry group of B. ...

There should exist a (natural) infinite-dimensional Z-graded module for M (i.e., representation of M)

such that

V = DIRSUM(n=-1,0,1,2,3,...) V_n ...

... the graded dimension of the graded vector space V ... = ... SUM(n=-1,0,1,2,3,...) (dim V_n) q^n

where

 $J(q) = q^{(-1)} + 0 + 196884q + higher-order terms,$

the classical modular function with its constant term set to 0. J(q) is the suitably normalized generator of the field of SL(2, Z)-modular invariant functions on the upper half-plane, with q = exp(2 pi i tau), tau in the upper half-plane ...

Conway and Norton conjectured ... for every g in M (not just g = 1), the the generating function

... the graded trace of the action of g on the graded space V ... = ...

SUM(n=-1,0,1,2,3,...) (tr g | V_n) q^n

should be the analogous "Hauptmodul" for a suitable discrete subgroup of SL(2,R), a subgroup having a fundamental "genus-zero property," so that its associated field of modular-invariant functions has a single generator (a Hauptmodul) ... (... the graded dimension is of course the graded trace of the identity element g = 1.) The Conway-Norton conjecture subsumed a remarkable coincidence that had been noticed earlier

- that the 15 primes giving rise to the genus-zero property ... are precisely the primes dividing the order of the ... Monster ...

the McKay-Thompson conjecture ... that there should exist a natural ... infinitedimensional Z-graded M-module V whose graded dimension is J(q) ... was (constructively) proved The graded traces of some, but not all, of the elements of the Monster - the elements of an important subgroup of M, namely, a certain involution centralizer involving the largest Conway sporadic group Co1 - were consequences of the construction, and these graded traces were indeed (suitably) modular functions ... We called this V "the moonshine module V[flat]" ... The construction ... needed ... a natural infinite-dimensional "affinization" of the Griess algebra B acting on V[flat] This "affinization," which was part of the new algebra of vertex operators, is analogous to, but more subtle than, the notion of affine Lie algebra More precisely, the vertex operators were needed for a "commutative affinization" of a certain natural 196884-dimensional enlargement B' of B, with an identity element (rather than a "zero" element) adjoined to B. This enlargement B' naturally incorporated the Virasoro algebra - the central extension of the Lie algebra of formal vector fields on the circle - acting on V[flat] ...

The vertex operators were also needed for a natural "lifting" of Griess's action of M from the finite-dimensional space B to the infinite-dimensional structure V[flat], including its algebra of vertex operators and its copy of the affinization of B'.

Thus the Monster was now realized as the symmetry group of a certain explicit "algebra of vertex operators" based on an infinite-dimensional Z-graded structure whose graded dimension is the modular function J(q).

Griess's construction of B and of M acting on B was a crucial guide for us, although we did not start by using his construction; rather, we recovered it, as a finite-dimensional "slice" of a new infinite-dimensional construction using vertex operator considerations. ...

The initally strange-seeming finite-dimensional Griess algebra was now embedded in a natural new infinite-dimensional space on which a certain algebra of vertex operators acts ... At the same time, the Monster, a finite group, took on a new appearance by now being understood in terms of a natural infinite-dimensional structure. ... the largest sporadic finite simple group, the Monster, was "really" infinite-dimensional ...

The very-highly-nonassociative Griess algebra, or rather, from our viewpoint, the natural modification of the Griess algebra, with an identity element adjoined, coming from a "forced" copy the Virasoro algebra, became simply the conformalweight-two subspace of an algebra of vertex operators of a certain "shape." ...

the constant term of J(q) is zero, and this choice of constant term, which is not uniquely determined by number-theoretic principles, is not traditional in number theory. It turned out that the vanishing of the constant term ... was canonically "forced" by the requirement that the Monster should act naturally on V[flat] and on an associated algebra of vertex operators.

This vanishing of the degree-zero subspace of V[flat] is actually analogous in a certain strong sense to the absence of vectors in the Leech lattice of square-length two; the Leech lattice is a distinguished rank-24 even unimodular (self-dual) lattice with no vectors of square-length two.

In addition, this vanishing of the degree-zero subspace of V[flat] and the absence of square-length-two elements of the Leech lattice are in turn analogous to the absence

of code-words of weight 4 in the Golay error-correcting code, a distinguished selfdual binary linear code on a 24-element set, with the lengths of all code-words divisible by 4. In fact, the Golay code was used in the original construction of the Leech lattice, and the Leech lattice was used in the construction of V[flat]

This was actually to be expected ... because it was well known that the automorphism groups of both the Golay code and the Leech lattice are (essentially) sporadic finite simple groups; the automorphism group of the Golay code is the Mathieu group M24 and the automorphism group of the Leech lattice is a double cover of the Conway group Co1 mentioned above, and both of these sporadic groups were well known to be involved in the Monster ... in a fundamental way....

The Golay code is actually unique subject to its distinguishing properties mentioned above ... and the Leech lattice is unique subject to its distinguishing properties mentioned above ... Is V[flat] unique? If so, unique subject to what? ... this uniqueness is an unsolved problem ...

V[flat] came to be viewed in retrospect by string theorists as an inherently stringtheoretic structure: the "chiral algebra" underlying the Z2-orbifold conformal field theory based on the Leech lattice.

The string-theoretic geometry is this: One takes the torus that is the quotient of 24-dimensional Euclidean space modulo the Leech lattice, and then one takes the quotient of this manifold by the "negation" involution $x \rightarrow x$, giving rise to an orbit space called an "orbifold"&emdash; a manifold with, in this case, a "conical" singularity. Then one takes the "conformal field theory" (presuming that it exists mathematically) based on this orbifold, and from this one forms a "string theory" in two-dimensional space-time by compactifying a 26-dimensional "bosonic string" on this 24-dimensional orbifold. The string vibrates in a 26-dimensional space, 24 dimensions of which are curled into this 24-dimensional orbifold ...

Borcherds used ... ideas, including his results on generalized Kac-Moody algebras, also called Borcherds algebras, together with certain ideas from string theory, including the "physical space" of a bosonic string along with the "no-ghost theorem" ... to prove the remaining Conway-Norton conjectures for the structure V[flat] ... What had remained to prove was ... that ... the conjugacy classes outside the involution centralizer - were indeed the desired Hauptmoduls ... He accomplished this by constructing a copy of his "Monster Lie algebra" from the "physical space" associated with V[flat] enlarged to a central-charge-26 vertex algebra closely related to the 26-dimensional bosonic-string structure mentioned above. He transported the known action of the Monster from V[flat] to this copy of the Monster Lie algebra, and ... he proved certain recursion formulas he succeeded in concluding that all the graded traces for V[flat] must coincide with the formal series for the Hauptmoduls ...

this vertex operator algebra V[flat] has the following three simply-stated

properties ...

• (1) V[flat], which is an irreducible module for itself ..., is its only irreducible module, up to equivalence ... every module for the vertex operator algebra V [flat] is completely reducible and is in particular a direct sum of copies of itself. Thus the vertex operator algebra V[flat] has no more representation theory than does a field! (I mean a field in the sense of mathematics, not physics. Given a field, every one of its modules - called vector spaces, of course - is completely reducible and is a direct sum of copies of itself.)

 (2) dim V[flat]_0 = 0. This corresponds to the zero constant term of J(q); while the constant term of the classical modular function is essentially arbitrary, and is chosen to have certain values for certain classical numbertheoretic purposes, the constant term must be chosen to be zero for the purposes of moonshine and the moonshine module vertex operator algebra.

• (3) The central charge of the canonical Virasoro algebra in V[flat] is 24. "24" is the "same 24" so basic in number theory, modular function theory, etc. As mentioned above, this occurrence of 24 is also natural from the point of view of string theory.

These three properties are actually "smallness" properties in the sense of conformal field theory and string theory. These properties allow one to say that V[flat] essentially defines the smallest possible nontrivial string theory ... (These "smallness" properties essentially amount to: "no nontrivial representation theory," "no nontrivial gauge group," i.e., "no continuous symmetry," and "no nontrivial monodromy"; this last condition actually refers to both the first and third "smallness" properties.)

Conversely, conjecturally ... V[flat] is the unique vertex operator algebra with these three "smallness" properties (up to isomorphism). This conjecture ... remains unproved. It would be the conformal-field-theoretic analogue of the uniqueness of the Leech lattice in sphere-packing theory and of the uniqueness of the Golay code in error-correcting code theory ...

Proving this uniqueness conjecture can be thought of as the "zeroth step" in the program of classification of (reasonable classes of) conformal field theories. M. Tuite has related this conjecture to the genus-zero property in the formulation of monstrous moonshine.

Up to this conjecture, then, we have the following remarkable characterization of the largest sporadic finite simple group: The Monster is the automorphism group of the smallest nontrival string theory that nature allows ... Bosonic 26-dimensional space-time ... "compactified" on 24 dimensions, using the orbifold construction V[flat] ... or more precisely, the automorphism group of the vertex operator algebra with the canonical "smallness" properties. ...

This definition of the Monster in terms of "smallness" properties of a vertex operator algebra provides a remarkable motivation for the definition of the precise notion of vertex (operator) algebra. The discovery of string theory (as a mathematical, even if not necessarily physical) structure sooner or later must lead naturally to the question of whether this "smallest" possible nontrivial vertex operator algebra V . exists, and the question of what its symmetry group (which turns out to be the largest sproradic finite simple group) is.

And on the other hand, the classification of the the finite simple groups - a mathematical problem of the absolutely purest possible sort - leads naturally to the question of what natural structure the largest sporadic group is the symmetry group of; the answer entails the development of string theory and vertex operator algebra theory (and involves modular function theory and monstrous moonshine as well).

The Monster, a singularly exceptional structure - in the same spirit that the Lie algebra E8 is "exceptional," though M is far more "exceptional" than E8 - helped lead to, and helps shape, the very general theory of vertex operator algebras. (The exceptional nature of structures such as E8, the Golay code and the Leech lattice in fact played crucial roles in the construction of V[flat] ...

V[flat] is defined over the field of real numbers, and in fact over the field of rational numbers, in such a way that the Monster preserves the real and in fact rational structure, and that the Monster preserves a rational-valued positive-definite symmetric bilinear form on this rational structure. ...

the "orbifold" construction of V[flat] ...[has been]... interpreted in terms of algebraic quantum field theory, specifically, in terms of local conformal nets of von Neumann algebras on the circle ...

the notion of vertex operator algebra is actually the "one-complex-dimensional analogue" of the notion of Lie algebra. But at the same time that it is the "onecomplexdimensional analogue" of the notion of Lie algebra, the notion of vertex operator algebra is also the "one-complex- dimensional analogue" of the notion of commutative associative algebra (which again is the corresponding "onerealdimensional"

notion). ... This analogy with the notion of commutative associative algebra comes from the "commutativity" and "associativity" properties of the vertex operators ... in a vertex operator algebra ...

The remarkable and paradoxical-sounding fact that the notion of vertex operator algebra can be, and is, the "one-complex-dimensional analogue" of BOTH the notion of Lie algebra AND the notion of commutative associative algebra lies behind much of the richness of the whole theory, and of string theory and conformal field theory.

When mathematicians realized a long time ago that complex analysis was

qualitatively entirely different from real analysis (because of the uniqueness of analytic continuation, etc., etc.), a whole new point of view became possible. In vertex operator algebra theory and string theory, there is again a fundamental passage from "real" to "complex," this time leading from the concepts of both Lie algebra and commutative associative algebra to the concept of vertex operator algebra and to its theory, and also leading from point particle theory to string theory. ...

While a string sweeps out a two-dimensional (or, as we've been mentioning, onecomplex-dimensional) "worldsheet" in space-time, **a point particle of course sweeps out a one-real-dimensional "world-line" in space-time**, with time playing the role of the "one real dimension," and this "one real dimension" is related in spirit to the "one real dimension" of the classical operads that I've briefly referred to - the classical operads "mediating" the notion of associative algebra and also the notion of Lie algebra (and indeed, any "classical" algebraic notion), and in addition "mediating" the classical notion of braided tensor category. The "sequence of operations performed one after the other" is related (not perfectly, but at least in spirit) to the ordering ("time-ordering") of the real line.

But as we have emphasized, the "algebra" of vertex operator algebra theory and also of its representation theory (vertex tensor categories, etc.) is "mediated" by an (essentially) one-complex-dimensional (analytic partial) operad (or more precisely, as we have mentioned, the infinite-dimensional analytic structure built on this). When one needs to compose vertex operators, or more generally, intertwining operators, after the formal variables are specialized to complex variables, one must choose not merely a (time-)ordered sequencing of them, but instead, a suitable complex number, or more generally, an analytic local coordinate as well, for each of the vertex operators.

This process, very familiar in string theory and conformal field theory, is a reflection of how the one-complex-dimensional operadic structure "mediates" the algebraic operations in vertex operator algebra theory.

Correspondingly, "algebraic" operations in this theory are not instrinsically "timeordered";

they are instead controlled intrinsically by the one-complex-dimensional operadic structure. The "algebra" becomes intrinsically geometric.

"Time," or more precisely, as we discussed above, the one-real-dimensional world-line, is being replaced by a one-complex-dimensional world-sheet.

This is the case, too, for the vertex tensor category structure on suitable module categories. In vertex operator algebra theory, "algebra" is more concerned with one-complex-

dimensional geometry than with one-real-dimensional time. ...".

Appendix - ADE World-Line String Bohm Quantum Consciousness

(see Saul-Paul Sirag's ADEX and Consciousness: A Hyperspace View (extensively paraphrased here))

Universal Geometric Entity = completion of union of tensor products of Cl(1,25) Each Cl(1,25) contains Lie Algebra E8 corresponding to McKay Group Algebra C[ID] so E8 x C[ID] is basic Local Geometric Entity

Universal Body Physical World = = 240 Root Vectors (120 pairs) of E8 Lie Algebra 240 E8 Root Vectors decompose into 112 of D8 and 128 of E7xA1 D8 = Bosonic Part = 8-dim Spacetime + Conformal Gravity + Standard Model D8 contains two copies of 24 D4 Root Vectors plus 63-dim SL(8) of unimodular 8-dim spacetime plus 1-dim Center of a Creation-Annihilation Heisenberg Group One D4 contains generators of Conformal Gravity plus Standard Model Ghosts Other D4 contains Standard Model Generators plus Conformal Gravity Ghosts E7xA1 = Fermionic Part = Fermion Particles + Fermion AntiParticles The 126+2 = 128 Root Vectors of E7xA1 represent 8 components of 8 first-generation fermion particles = 64 plus 8 components of 8 first-generation fermion antiparticles = 64

WE8 = Weyl Group of E8 = 128x27x5x8! divides Complex 8-dim C8 into C8 / WE8

Universal Mind Mental World == 120 elements of C[ID] Group Algebra of ID McKay Group of E8ID McKay Group of E8 decomposes into McKay Groups of D8 and E7xA1McKay Group of D8= Q6= 24= 8 x 3 x 1= vertices of 24-cellMcKay Group of E7xA1= 20D= 96= 8 x 3 x 4= edges of 24-cellMcKay Group of E8= ID= 120= 8 x 3 x 5= vertices of 600-cell

ME8 = ID = McKay Group of E8 divides Complex Plane C2 into C2 / ME8

120 WE8 mirror planes in C8 are mapped into C8 / WE8 The point where all the mirrors intersect is the origin of C8 / WE8 to which is attached the identity fiber C2 / ME8. Paths in C8 / WE8 correspond to World-Lines of Observers. (World-Lines = Bosonic Strings) Each deformation of C2 / ME8 selects a different path in C8 / WE8 so C2 / ME8 is the source of Mental Images of the Physical World. E8 Dynkin Balance Numbers:

E8 Dynkin Representations:

147,250

248 - 30,380 - 2,450,240 - 146,325,270 - 6,899,079,264 - 6,696,000 - 3,875

E8 deformation mapping form:

E₈:
$$V = x^3 + y^5 + z^2 + t_1x + t_2y + t_3xy + t_4y^2 + t_5y^3 + t_6xy^2 + t_7xy^3 + t_8$$

The 7D separatrix Σ is in C8/ WE8, since {t1,..., t8} are invariants of the E8 Coxeter group (also called the Weyl group). Since there are 120 mirror hyperplanes in C8, 120 is the maximum number of points in the special orbits making up Σ in C8 / WE8.

By contrast, the regular orbits have $128 \times 27 \times 5 \times 8! = 696729600$ elements, which is the order of WE8. These regular orbits are the points inside the chambers between the 7D walls of Σ . Note that $128 \times 27 \times 5$ is the product of the E8 balance numbers (1, 2, 3, 4, 5, 6, 4, 2, 3), while 8! is 40320, the order of the Symmetric-8 group which permutes the eight basic mirrors of E8 ... the sum of the squares of the E8 balance numbers is (via the McKay correspondence) the dimension of ID ...

1 - The control parameters of the catastrophe bundle are {t1,..., t8}.

2 - The t8 parameter (always with 1 as coefficient) plays the role of time along the many paths ramifying out from the origin of C8 / WE8,

where there is attached the identity fiber C2 / ME8 .

3 - Movement along any of these paths corresponds to

the selection of different values of the control parameters, and thus different fibers which entail an unfolding of the singularity structure C2 / ME8 .

4 - The changes in the fiber attached to a path are mild if the movement along the path (while picking out different fibers) remains within a chamber of the separatrix.

If movement along the path crosses the separatrix, the change will be drastic.

5 - As fibers farther and farther from the origin in C8 / W are encountered

and more separatrix walls are crossed, the fibers become more unfolded.

Beyond the unfoldings of the fibers as described above,

the E8 Lie algebra itself provides the structures for the resolution of the deformed (unfolded) fibers, including most importantly the identity fiber C2 / ME8.

The Unfolding of the Mental Images of the Physical World based on the Bosonic String World-Line Paths in C8 / WE8 corresponds to the Unfolding of the Bohm Implicate Order

Unfolding of the Implicate Order of Bohm Quantum Theory

The Unfolding can be clarified by the projection diagram:

where g is E8 and X is a subregular nilpotent element within the nilpotent variety in E8. The Lie Group version of this projection diagram takes G(E8) to its maximal torus T and then to T / WE8.

The projection tau is from E8 onto its Cartan subalgebra t.

The projection w is from t to the orbit space t / WE8, where 0 is the origin in t / WE8. The projection pi is from E8 to S which is

the 10-dim slice transverse to the nilpotent variety in E8

and s is a subregular (i.e., singular) element in this variety.

The nilpotent variety n in E8 is the identity fiber in the fiber bundle with projection X: (E8,X) -> (t / WE8, 0)

so the dimensionality of n is dim(E8) - dim(t /WE8) = (Coxeter #)(Rank) = 30x8 = 240The projection phi maps the Kleinian singularity C2 / ME8 onto the origin of t / WE8 and as a universal deformation maps

unfolded versions of C2 /ME8 onto the parameters $\{t1, ..., t8\}$ which are homogeneous polynomial invariants of WE8.

phi provides for the deformation (or unfolding) of the Kleinian singularities. (THIS IS CONVENTIONAL BOHM PILOT ACTION)

the lifting of the slice S into the nilpotent variety n that provides for the simultaneous resolution (or desingularization) of all the fibers in S.

(THIS IS JACK SARFATTI'S UNCONVENTIONAL BACKREACTION) the most singular fiber is the identity fiber in S, the singularity structure C2 / ME8. In the process of desingularization,

the singular point evolves into a series of exceptional curves,

which are 1D complex projective lines P1,

which geometrically are a "bouquet" of 2D spheres which takes the form of a dual structure to the E8 Coxeter graph. For E8, the Kleinian singularity C2 / ME8 has its singular point resolved into a bouquet of 8 (2D)-spheres



The Unfolding of the Implicate Order originates at the Origin Singularity C2 / ME8 which has structure C2 / ID of the 600-cell



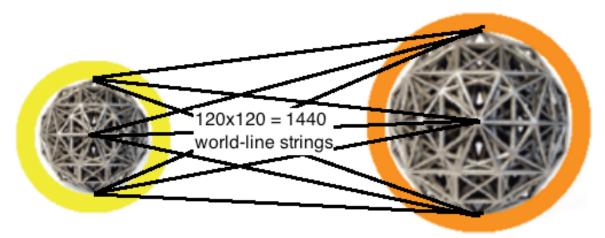
The resolution of the ADE singularity structure C2 / ME8 at the origin of C8 /WE8 where ME8 is a finite subgroup of SU(2) corresponding to the 600-cell is accomplished by the lifting of C2 / ME8 to a higher dimensional space C8. This lifting is a key part of the universal resolution of the unfolding of C2 / ME8.

Lifting goes from Origin to an ALE (Asymptotically Locally Euclidean) space at Infinity. The E8 ALE space is the E8 McKay group ID . ALE means that this 4D space looks like a Euclidean space, except that the boundary at infinity is not the 3-sphere S3 (which is the boundary at infinity of R4) but is S3 / ID = 600-cell



As a hyper-Kahler (H-K) space it has a metric which respects three complex structures I, J, K that obey the quaternion group formula I2 = J2 = K2 = IJK = -1As a 4D H-K space an ALE space is not compact but at infinity looks like R4 / ME8 with boundary S3 / ME8 in the sense that the singular point becomes desingularized as a "bouquet" of S2-spheres idual of the ADE Coxeter graph for E8 . The Unfolding of the Origin C2 /ME8 onto the parameters {t1, ..., t8} in the space C8 is along World-Line Strings emanating from the 120 vertices of the Origin 600-cell and forms a Bosonic String Theory with 2D worldsheets swept out by World-Line Strings and embedded in 26D spacetime reduced by orbifolding of fermions to 10D spacetime which produces Standard Bohm Qantum Potential without Back-Reaction.

When the 120 basic World-Line Strings leading from the C2 / ID Origin 600-cell connect up with the 120 vertices of the ALE S3 / ID 600-cell at Infinity



and

the corresponding 120 basic World-Line Strings back to the Origin C2 / ID 600-cell are taken into account, you get Sarfatti-Bohm Quantum Potential with Back-Reaction.

"... Bohm's Quantum Potential can be viewed as an internal energy of a quantum system ..." according to Dennis, de Gosson, and Hiley (arXiv 1412.5133) and Peter R. Holland says in "The Quantum Theory of Motion" (Cambridge 1993): "... the total force ... from the quantum potential ... does not ... fall off with distance ... because ... the quantum potential ... depends on the form of ...[the quantum state]... rather than ... its ... magnitude ...".

Penrose-Hameroff-type Quantum Consciousness is due to Resonant Quantum Potential Connections among Quantum State Forms.

The Quantum State Form of a Conscious Brain is determined by the configuration of a subset of its 10^18 to 10^19 Tubulin Dimers with math description in terms of a large Real Clifford Algebra:

Resonance is discussed by Carver Mead in "Collective Electrodynamics" (MIT 2000): "... we can build ... a resonator from ... electric dipole ... configuration[s] ...



[such as

Tubulin Dimers]

Because there are charges at the two ends of the dipole, we can have a contribution to the electric coupling from the scalar potential ... as well [as] from the magnetic coupling ... from the vector potential ... electric dipole coupling is stronger than magnetic dipole coupling ... the coupling of ... two ... configurations ... is the same, whether retarded or advanced potentials are used. Any ... configuration ... couples to any other on its light cone, whether past or future. ... The total phase accumulation in a ... configuration ... is the sum of that due to its own current, and that due to currents in other ... configurations ... far away ...

The energy in a single resonator alternates between the kinetic energy of the electrons (inductance), and the potential energy of the electrons (capacitance). With the two resonators coupled, the energy shifts back and forth between the two resonators in such a way that the total energy is constant ... The conservation of energy holds despite an arbitrary separation between the resonators ... Instead of scaling linearly with the number of charges that take part in the motion, the momentum of a collective system scales as the square of the number of charges! ... The inertia of a collective system, however, is a manifestation of the interaction, and cannot be assigned to the elements separately. ... Thus, it is clear that collective quantum systems do not have a classical correspondence limit. ...".

For the 10^18 Tubulin Dimers of the human brain,

the resonant frequencies are the same and exchanges of energy among them act to keep them **locked in a Quantum Protectorate collective coherent state**.

Philip W. Anderson in cond-mat/0007287 and cond-mat/007185 said:

"... Laughlin and Pines have introduced the term "Quantum protectorate" as a general descriptor of the fact that certain states of quantum many-body systems exhibit properties which are unaffected by imperfections, impurities and thermal fluctuations. They instance ... flux quantization in superconductors, equivalent to the Josephson frequency relation which again has mensuration accuracy and is independent of imperfections and scattering. ...

... the source of quantum protection is a collective state of the quantum field involved such that the individual particles are sufficiently tightly coupled that elementary excitations no longer involve a few particles but are collective excitations of the whole system, and therefore, macroscopic behavior is mostly determined by overall conservation laws ... a "quantum protectorate" ...[is]... a state in which the many-body correlations are so strong that the dynamics can no longer be described in terms of individual particles, and therefore perturbations which scatter individual particles are not effective ...".

Mershin, Sanabria, Miller, Nawarathna, Skoulakis, Mavromatos, Kolomenskii, Scheussler, Ludena, and Nanopoulos in physics/0505080 "Towards Experimental Tests of Quantum Effects in Cytoskeletal Proteins" said:

1...

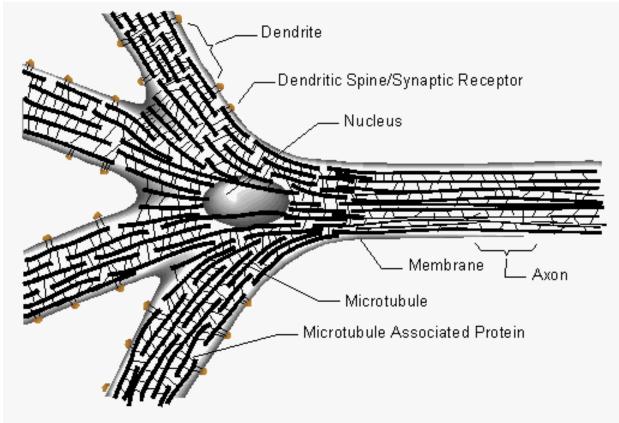
Classically, the various dimers can only be in the ...[

conformations. Each dimer is influenced by the neighboring dimers resulting in the possibility of a transition. This is the basis for classical information processing, which constitutes the picture of a (classical) cellular automaton.

If we assume ... that each dimer can find itself in a QM superposition of ...[those]... states, a quantum nature results. Tubulin can then be viewed as a typical two-state quantum mechanical system, where the dimers couple to conformational changes with $10^{-9} - 10^{-11}$ sec transitions, corresponding to an angular frequency ~ $10^{10} - 10^{12}$ Hz. In this approximation, the upper bound of this frequency range is assumed to represent (in order of magnitude) the characteristic frequency of the dimers, viewed as a two-state quantum-mechanical system ...[

The Energy Gap of our Universe as superconductor condensate spacetime is from 3 x 10⁽⁻¹⁸⁾ Hz (radius of universe) to 3 x 10⁴³ Hz (Planck length). Its RMS amplitude is 10¹³ Hz = 10 THz = energy of

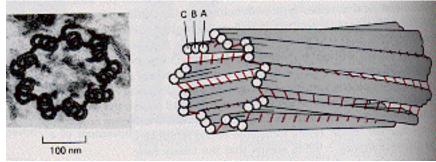
neutrino masses = critical temperature Tc of BSCCO superconducting crystal Josephson Junctions]... large-scale quantum coherence ...[has been observed]... at temperatures within a factor of three of biological temperatures. MRI magnets contain hundreds of miles of superconducting wire and routinely carry a persistent current. There is no distance limit - the macroscopic wave function of the superfluid condensate of electron pairs, or Cooper pairs, in a sufficiently long cable could maintain its quantum phase coherence for many thousands of miles ... there is no limit to the total mass of the electrons participating in the superfluid state. The condensate is "protected" from thermal fluctuations by the BCS energy gap at the Fermi surface ... The term "quantum protectorate" ... describe[s] this and related many-body systems ...". The Human Brain has about 10^11 Neuron cells, each about 1,000 nm in size. The cytoskeleton of cells, including neurons of the brain, is made up of Microtubules



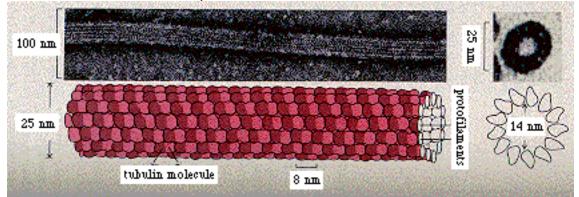
(image from "Orchestrated Objective Reduction of Quantum Coherence in Brain Microtubules: The "Orch OR" Model for Consciousness" by Penrose and Hameroff)

Each Neuron contains about 10^9 Tubulin Dimers, organized into Microtubules some of which are organized by a Centrosome. Centrosomes contain a pair of Centroles.

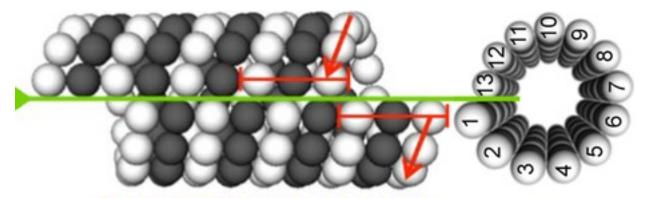
A Centriole is about 200 nm wide and 400 nm long. Its wall is made up of 9 groups of 3 Microtubules, reflecting the symmetry of 27-dim J(3,O)



Each Microtubule is a hollow cylindrical tube with about 25 nm outside diameter and 14 nm inside diameter, made up of 13 columns of Tubulin Dimers



(illustrations and information about cells, microtubules, and centrioles are from Molecular Biology of the Cell, 2nd ed, by Alberts, Bray, Lewis, Raff, Roberts, and Watson (Garland 1989))



(image from Wikipedia on Microtubule)

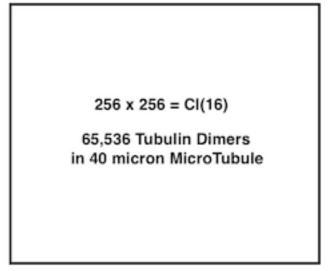
Each Tubulin Dimer is about 8 nm x 4 nm x 4 nm, consists of two parts, alpha-tubulin and beta-tubulin (each made up of about 450 Amino Acids, each containing roughly 20 Atoms) A Microtubule 40 microns = 40,000 nm long contains $13 \times 40,000$ / 8 = 65,000 Dimers



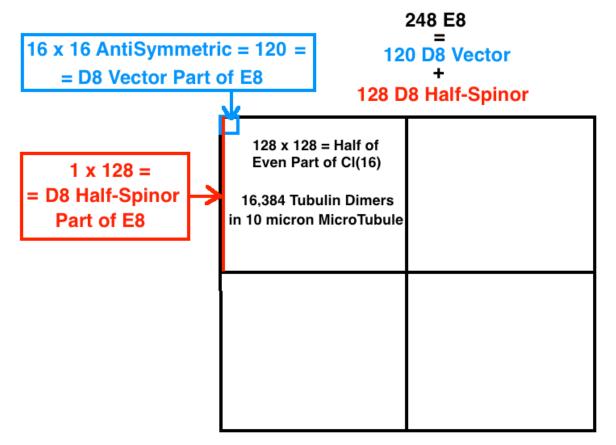
(images adapted from nonlocal.com/hbar/microtubules.html by Rhett Savage) The black dots indicate the position of the Conformation Electrons. There are two energetically distinct configurations for the Tubulin Dimers: Conformation Electrons Similarly Aligned (left image) - State 0 Conformation Electrons Maximally Separated (right image) - State 1

The two structures - State 0 ground state and State 1 higher energy state - make Tubulin Dimers the basis for a Microtubule binary math / code system.

Microtubule binary math / code system corresponds to Clifford Algebras Cl(8) and Cl(8)xCl(8) = Cl(16) containing E8



A 40 micron Microtubule contains Dimers representing the 65,536 elements of Cl(16) which contains the 248 elements of Lie Algebra E8 that defines E8 Physics Lagrangian.



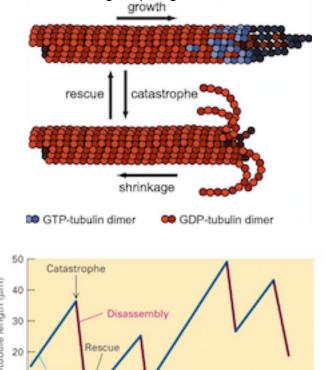
E8 lives in only half of the block diagonal Even Part half of Cl(16) so that E8 of E8 Physics can be represented by the 16,384 Dimers of a 10 micron Microtubule.

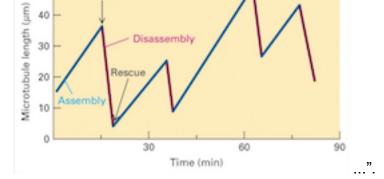
According to 12biophys.blogspot.com Lecture 11 Microtubule structure is dynamic: "... One end of the microtubule is composed of stable (GTP) monomers while the rest of the tubule is made up of unstable (GDP) monomers. The GTP end comprises a cap of stable monomers.

Random fluctuations either increase or decrease the size of the cap.

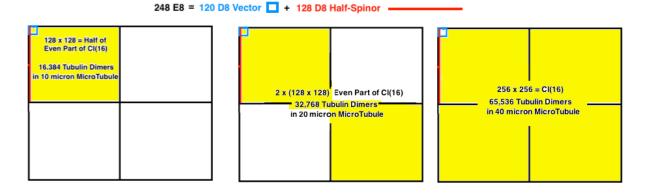
This results in 2 different dynamic states for the microtubule.

Growing: cap is present Shrinking: cap is gone ...





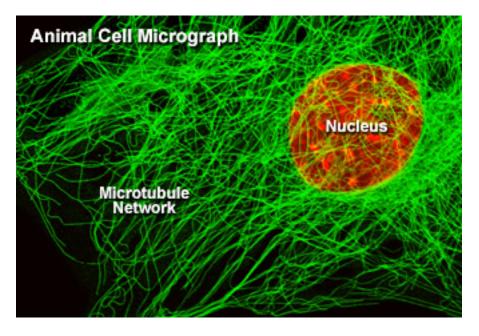
Microtubules spend most of their lives between 10 microns and 40 microns, sizes that can represent E8 as half of the Even Part (half) of Cl(16) (10 microns)



or as the Even Part (half) of Cl(16) (20 microns) or as full Cl(16) (40 microns).

In a given Microtubule	
the 128 D8 Half-Spinor part Dimers in its stable GTP regio and	is represented by a line of 128
•	by a 12 x 10 block of Dimers in its stable GTP region oted from 12biophys.blogspot.com Lecture 11)
128 Dimer Line = 128 x 8 = 1,024 nm = 1 min GTP tubulin molecules add to end of microtubule	e x10 = 120 Dimer Rectangle protofilaments containing GDP tubulin are unstable and released

The image immediately above does not show how thin is the Microtubule. The following image (from micro.magnet.fsu.edu) shows overall Microtubule shape



How do the Microtubules communicate with each other ?

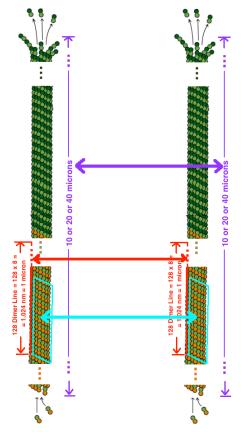
Consider the Superposition of States State 0 and State 1 involving one Tubulin Dimer with Conformation Electron mass m and State1 / State 0 position separation a .

The Superposition Separation Energy Difference is the internal energy

E_ssediff = G m^2 / a

that can be seen as either the **energy of 26D String Theory spin two gravitons** or the **Bohm Quantum Potential internal energy**, equivalently.

Communication between two Microtubules is by the Bohm Quantum Potential between their respective corresponding Dimers (purple arrow) with the correspondence being based on connection between respective E8 subsets, the 128 D8 Half-Spinors (red arrow) and the 120 D8 BiVectors (cyan arrow)



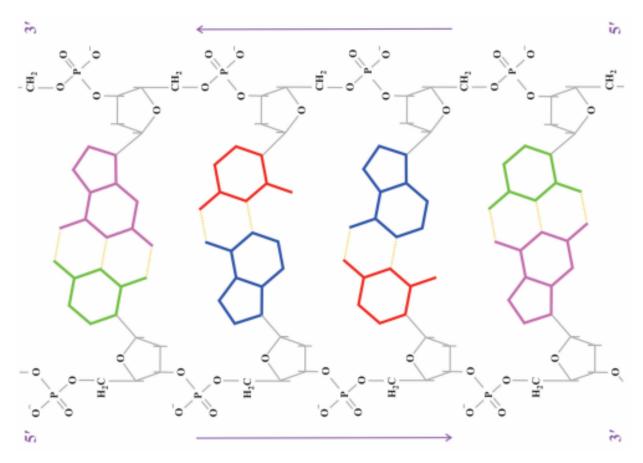
How is information encoded in the Microtubules ?

Each Microtubule contains E8, allowing Microtubules to be corrrelated with each other. The parts of the Microtubule beyond E8 are in Cl(16) for 40 micron Microtubules, or the Even Subalgebra of Cl(16) for 20 micron Microtubules, or half of the Even Subalgebra of Cl(16) for 10 micron Microtubules so since by 8-Periodicity of Real Clifford Algebras Cl(16) = Cl(8) x Cl(8) and since Cl(8) information is described by the Quantum Reed-Muller code [[256 , 0 , 24]] **the information content** of Cl(16) and its Subalgebras **is described by the Tensor Product Quantum Reed-Muller code [[256 , 0 , 24]] x [[256 , 0 , 24]]**

For a 40-micron Microtubule there are, outside the 248-E8 part, about 65,000 TD Qubits available to describe one Quantum Thought State among about 2^65,000 possibilities, analagous to the Book of Genesis of (22+5)^78,064 Hebrew Letter/Final possibilities.

65,536-dimensional CI(16) not only contains the E8 of E8 Physics and the information content of Microtubules but also contains **the information content of DNA chromosome condensation** and **the information content of mRNA triple - amino acid transformations**.

In "Living Matter: Algebra of Molecules" (CRC Press 2016) Valery V. Stcherbic and Leonid P. Buchatsky say: "... DNA structure contains four nucleotides: adenine A, guanine G, cytosine C and thymine T. ...



... The Sugar-phosphate group consists of 2-deoxyribose and phosphoric acid residues. DNA chain orientation is identified by carbon atoms of 2-deoxyribose: (5')CH2 and (3')COH. The biological function of DNA and storage and transfer of genetic information to daughter cells is based on specific, complimentary pairing of nucleotides: A is paired with T, and G with C.

• • •

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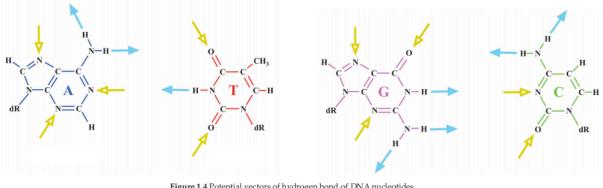


Figure 1.4 Potential vectors of hydrogen bond of DNA nucleotides. Yellow arrows—acceptors, blue arrows—donors of hydrogen.

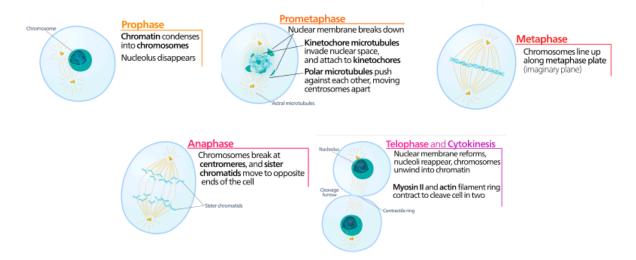
The space of DNA nucleotide states contains T2^3 \otimes C2^4 \otimes A2^5 \otimes G2^6 = 2^18 elements of Clifford algebras. This space reduction to four nucleotides means compression of DNA information by a factor of 2^18 / 4 = 65536. Reduction of the nucleotide state space leads to DNA compactization and chromosome condensation. ...".

In "Chromosome Condensation and Cohesion" (eLS December 2010) Laura Angelica Diaz-Martinez and Hongtau Yu say: "... The diploid human genome consists of 46 chromosomes, which collectively contain about 2 m of deoxyribonucleic acid (DNA). During mitosis, the genome is packaged into 46 pairs of sister chromatids, each less than 10 μ m long. ...".

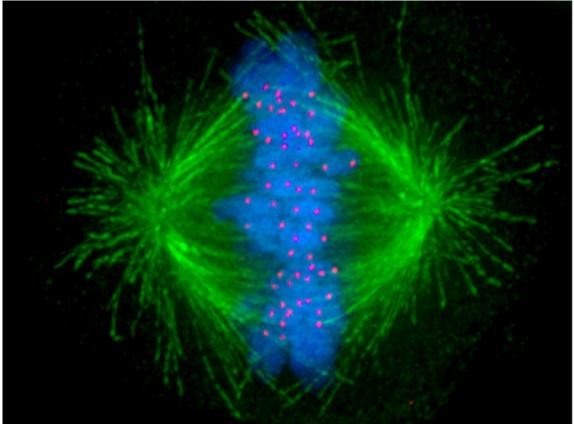
The DNA information condensation factor of 65,536 is the dimension of Cl(16) which is the Real Clifford Algebra containing 248-dim E8 of E8 Physics as 120-dim bivector D8 plus 128-dim D8 half-spinor and is also the Clifford Algebra of Microtubule information in Quantum Consciousness.

Microtubule information = 65,536 = CI(16) = DNA condensation information

Wikipedia describes interaction of Microtubules with DNA in mitosis condensation: "...



... Micrograph showing condensed chromosomes in blue, kinetochores in pink, and microtubules in green during metaphase of mitosis ...



...". Information lost by condensing DNA is stored in Microtubules through Anaphase after which it has been restored to the new Duplicated DNA.

Stcherbic and Buchatsky also say: "... Ribonucleic acid (RNA) can also store genetic information. A single RNA helix is seldom used as a carrier of genetic information (only in some viruses); its main role is storing DNA sites as copies of individual proteincoding genes (mRNA) or in formation of large structural complexes, e.g., ribosomes and spliceosomes. At self-splicing, RNA may perform the function of an enzyme. RNA also performs an important role during DNA replication. So called RNA-primers are necessary to synthesize DNA complementary chains, although this fact is not obvious. RNA contains sugar, ribose, which hydroxyl groups make more reactive than DNA. Besides, RNA contains uracil U, which is somewhat lighter than thymine.

•••

At translation of mRNA triplets into genetic code amino acids,

the dynamics of triplets to amino acids transformation should be taken into account.

At transition ... functional volume is equal to $3^5 = 243$.

To this volume there should be added the volume of auxiliary spaces,

equal to 13 = 5 + 4 + 3 + 1.

Accordingly, we get

256 functions of mRNA triplet transformation into amino acids of the genetic code. Reverse transition ... from amino acids ... to triplet ... needs $5^3 + 3^1 = 128$ functions. In addition, 128 triplets of mRNA-tRNA pairing should be added to this number. ...".

The 256 of mRNA triplet to amino acids is represented by CI(8) Clifford algebra and

the 128+128 = 256 of amino acids to mRNA triplets is representd by another CI(8) so

that the mRNA triple - amino acid connection is represented by the tensor product Cl(8) x Cl(8) which by 8-Periodicity of Real Clifford Algebras is the Real Clifford Algebra Cl(16) which also contains 248-dim E8 of viXra 1508.0157 E8 Physics

and is also the Clifford Algebra

of Microtubule information in viXra 1512.0300 Quantum Consciousness.

What about information in the Many Microtubules of Human Consciousness ?

The information in one Microtubule is based on Cl(16) which is contained in the Cl(1,25) of 26D String Theory E8 Physics (see Chapter on E8 Quantum Theory)

How does this give rise to Penrose-Hameroff Quantum Consciousness ?

Consider the Superposition of States State 0 and State 1 involving one Tubulin Dimer with Conformation Electron mass m and State1 / State 0 position separation a . **The Superposition Separation Energy Difference is the internal energy** E ssediff = G m² / a

that can be seen as the **energy of 26D String Theory spin two gravitons** which physically represent the **Bohm Quantum Potential internal energy**. (see Appendix - Details of World-Line String Bohm Quantum Theory)

For a given Tubulin Dimer a = 1 nanometer $= 10^{-7}$ cm so that T = h / E_electron = (Compton / Schwarzschild) (a / c) = 10^{26} sec = 10^19 years

Now consider the case of N Tubulin Dimers in Coherent Superposition connected by the Bohm Quantum Potential Force that does not fall off with distance. Jack Sarfatti defines coherence length L by $L^{3} = N a^{3}$ so that the Superposition Energy E_N of N superposed Conformation Electrons is $E_N = G M^2 / L = N^{(5/3)} E_sediff$

The decoherence time for the system of N Tubulin Electrons is

T_N = h / E_N = h / N^(5/3) E_ssediff = N^(-5/3) 10^26 sec

so we have the following rough approximate Decoherence Times T_N

Number of Involved	Time
Tubulin Dimers	T_N

10^(11+9) = 10^20 10^(-33 + 26) = 10^(-7) sec 10^11 neurons x 10^9 TD / neuron 10^20 Tubuin Dimers in Human Brain

10^16	10^(-27 + 26) = 10^(-1) sec - 10 Hz
	Human Alpha EEG is 8 to 13 Hz
	Fundamental Schumann Resonance is 7.8 Hz
	Time of Traverse by a String World-Line Quantum Bohmion of a Quantum
Consciousness Hamiltonian Circuit of 10^16 TD separated from nearest neighbors	
by 1	10 nm is 10^16 x 10 nm / c = (10^16 x 10^(-6)) cm / c = 10^10 cm / c = 0.3 sec

Appendix - Condensate Structure of Higgs and Spacetime

"... The Nambu Jona-Lasinio model ...

is a theory of Dirac particles with a local 4-fermion interaction and, as such, it belongs to the same class of effective theories as the BCS theory of superconducting metals ... the Nambu Jona-Lasinio model has very recently been applied to the standard model. In this application the Higgs meson is a ttbar top quark mass excitation ...".

(from Nambu Jona-Lasinio Models Applied to Dense Hadronic Matter, by Georges Ripka, in a Workshop on Nuclear Physics, Iguazu Falls, 28 Aug - 1 Sep 1989)

As to the Higgs in the E8 physics model (viXra 1602.0319), consider a generalized Nambu Jona-Lasinio model in which the Higgs is a Fermion-AntiFermion condensate. As the most massive fermion, the Truth Quark - AntiQuark pairs would be so dominant that the Higgs could be effectively considered as a condensate of Truth Quark - Truth AntiQuark pairs but the detailed picture would be as a condensate of Fermion - Anti-Fermion pairs where there are 24 types of Fermions, each Quark coming in color R, G, or B:

> E-Neutrino and Electron Down Quark (R, G, B) and Up Quark (R, G, B) M-Neutrino and Muon Strange Quark (R, G, B) and Charm Quark (R, G, B) T-Neutrino and Tauon Beauty Quark (R, G, B) and Truth Quark (R, G, B)

so that there are $24 \times 24 = 576$ Fermion-AntiFermion pairs for each Higgs and each Higgs can be in Bohm Quantum Resonance with 24×24 Bohm Quantum String states: dilaton; antisymmetric Planck-cell group; and symmetric Bohm Quantum Potential.

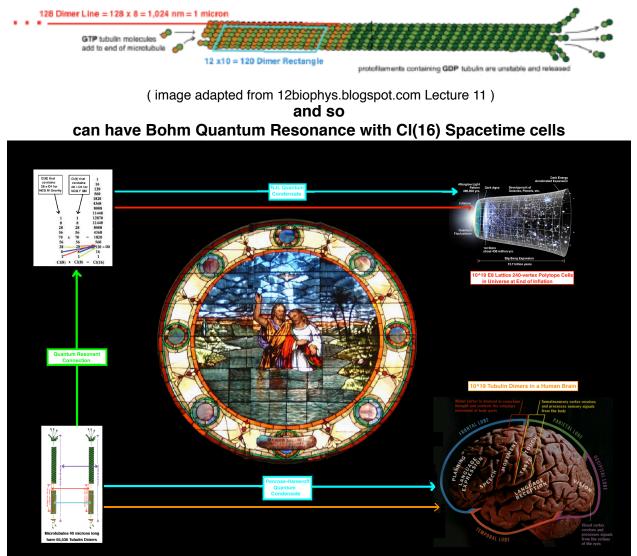
As to Spacetime in the E8 physics model (viXra 1602.0319), consider a generalized Nambu Jona-Lasinio model in which 8-dim Classical Lagrangian Spacetime is a condensate of Geoffrey Dixon's 64-dim Particle spinor T = RxCxHxO = Real x Complex x Quaternion x Octonion and its corresponding 64-dim AntiParticle spinor Tbar. The T - Tbar pairs of the condensate form the 128-dim part of E8 that lives in the Cl(16) Real Clifford Algebra as

248-dim E8 = 120-dim bivector D8 + 128-dim half-spinor D8

By Triality, the D8 / D4xD4 = 64-dim part of E8 representing Spacetime is equivalent to T and Tbar, with T representing Fermions and Tbar representing AntiFermions.

Each cell of E8 Classical Lagrangian Spacetime corresponds to 65,536-dim Cl(16) which contains 248-dim E8 = 120-dim D8 bivectors +128-dim D8 half-spinors

Human Brain Microtubules 40 microns long have 65,536 Tubulin Dimers



(image from Wikipedia and Time)

so that at any and all Times the State of Consciousness of a Human is in exact resonant correspondence with a subset of the cells of E8 Classical Lagrangian Spacetime

Therefore

E8 Classical Lagrangian Spacetime NJL Condensate is effectively the **Spirit World** in which the **Human States of Consciousness = Souls exist.**

After the death of the Human Physical Body the Spirit World interactions with its Soul are no longer constrained by Physical World interactions with its Body so that the Spirit World can harmonize the individual Soul with the collective Universal Soul by the process of Gehinnom whereby the Soul is prepared for Gan Eden.

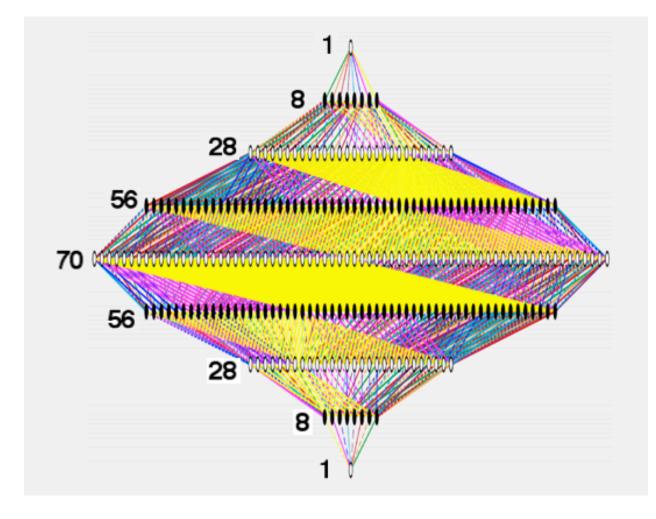
Appendix - Adinkra and Pyramid

According to The Oxford Encyclopedia of African Thought, Vol. 1, by Irele and Jeyifo: "... Adinkra are visual forms that ... integrate striking aesthetic power, evocative mathematical structures, and philosophical conceptions ...:

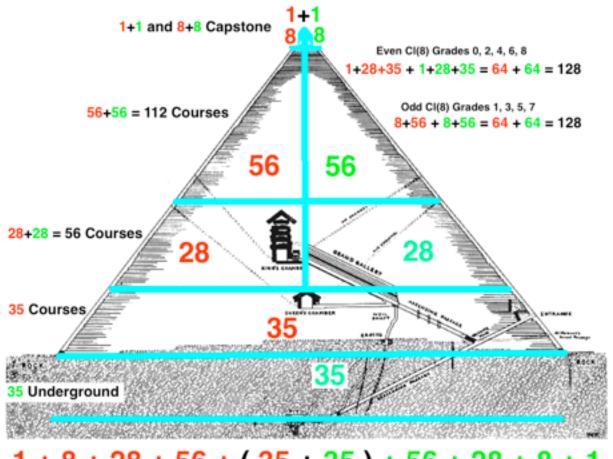
Gates, Doran, Faux, Hubsch, Iga, Landweber, and Miller (arxiv 0811.3410) said: "... we relate Adinkras to Clifford algebras ...".

G. D. Landweber's 2006 program Adinkramat at <u>http://www.cohomology.com</u>/ produces Adinkra graphs of MI^Ncubic, such as

N = 8 of real Clifford Algebra Cl(8) with 28-dim grade 2 = Spin(8) and graded structure 1 + 8 + 28 + 56 + 70 + 56 + 28 + 8 + 1with $2^8 = 256$ elements corresponding to the 256 Odu and sqrt(256) = 16-dim spinors = 8-dim +half-spinors and 8-dim -half-spinors



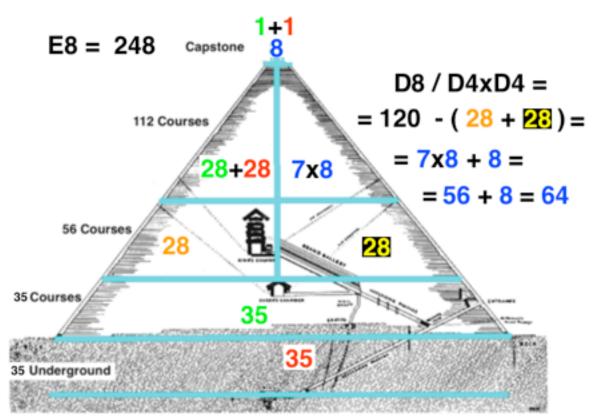
Clifford Algebras were not known to European mathematicians until Clifford in the 19th century and not known to European physicists until Dirac in the 20th century but it seems to me that their structure was known to Africans in ancient times. For example, the courses of the Great Pyramid of Giza correspond to the graded structure of Cl(8):



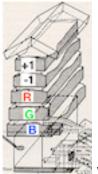
1 + 8 + 28 + 56 + (35 + 35) + 56 + 28 + 8 + 1

(image adapted from David Davidson image - for larger size see tony5m17h.net/GreatPyrCl8.png)

248-dim E8 (like 256-dim Cl(8)) can also be seen in terms of the Great Pyramid (the 8-dim difference is related to the Cl(8) Primitive Idempotent and the Higgs).



E8 / D8 = 248 - 120 = 128 = 64 + 64



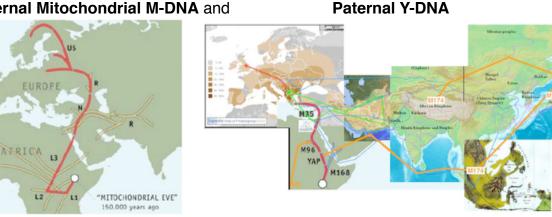
The ²⁸ is in the area of the Upper Chamber which has 5 slabs that represent the 5 charges (+1,-1 electric and R,G,B color) of the Standard Model.

The is in the area of the Grand Gallery which rises at a slope of about 26 degrees, or about half of the Golden Ratio slope of the Great Pyramid which is $\operatorname{arccosine}(1 / ((1 + \operatorname{sqrt}(5))/2)) = 51.8$ degrees. The Grand Gallery could represent a segment of a space-time path (World-Line) in the context of Conformal Gravity.

Some of my Ancestors

Frank Dodd (Tony) Smith, Jr. - 2017

Maternal Mitochondrial M-DNA and



show that my Mother's side Maternal ancestors U5 migrated out of Africa about 150,000 years ago to Finland

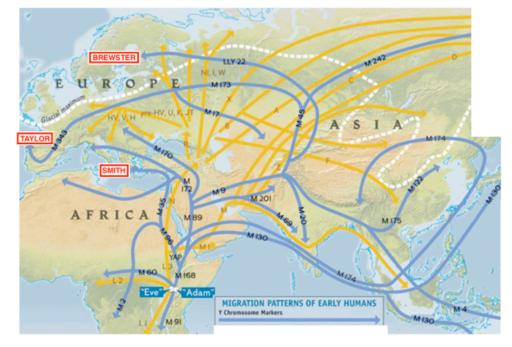
and that my Father's side Paternal ancestors E3b1= E-V13 migrated out of Africa about 50,000 years ago to Roman Legions and on to Britain.

As to Individual Ancestors, my Mother's side goes back to Angus McIntosh born 1715 in Inverness and John Whistler, born in Africa, husband of Ann McIntosh, daughter of Angus. John and Ann are my 5-Great Grandparents (7th Generation back).

My Father's side goes back to John Brewster I of Suffolk born 1279 (Y-DNA M-253) my 20-Great Grandfather (22nd Generation back),

with a branch to 11-Great Grandfather John Taylor born 1522 (Y-DNA R1b)

22nd Generation has 2²2 = 4,194,304 Grandparents. Earth population 1300 was about 400,000,000.



Material herein is taken from various sources, including but not limited to Wikipedia, ancestrycom, geni.com, fabpedigree.com, werelate.org, Burkes Landed Gentry, Alumni Cantabrigienses, U. Cambridge from Earliest Times to 1535

Paris and Cambridge around 1300

Around 1300 Scholasticism and Empiricism were being developed at the University of Paris, then the world's leading University, and Cambridge and Oxford Universities which were getting organized based on Paris. Developers of Scholasticism and Empiricism included:

Doctor Mirabilis = Roger Bacon (1219-1292) who advocated Aristotelian Empiricism, Doctor Angelicus = Thomas Aquinas (1225-1274) also an advocate of Aristotle. Doctor Illuminatus = Ramon Llull (1232-1315) who produced a system of Logic and a mathematical Art based on what is now known as the Clifford Algebra Cl(16) and the 120 dimensional Lie algebra Spin(16). 700 years ago the details of that mathematics were not known, nor was it known that the math structure of the Art gives a realistic representation of E8 Physics of the Standard Model and Gravity along with its Algebraic Quantum Field Theory. (see viXra 1602.0319) Doctor Subtilis = John Duns Scotus (1266-1308) who developed Llull's system of Logic into sophisticated Scholasticism, but did not have the math and physics knowledge to show that the mathematical Art of Doctor Illuminatus gives a realistic physics model.

A Second Scholasticism began in 1540 when Ignatius Loyola under Pope Paul III founded the Jesuits, who joined with the Franciscans (Bacon, Llull and Scotus) and the Dominicans (Aquinas) in developing Scholasticism but, without the ability to experimentally measure the relative strengths of the forces of the Standard Model and Gravity and the relative masses of the elementary fermion particles and to compare those observations with the physics model of Llull's mathematical Art, by 1700 Scholasticism had been displaced by the Enlightenment of Descartes et al.

Although I can trace my Brewster Line ancestry back to 1279 birth of John Brewster I, the earliest connection that I have found of them with Cambridge Scholasticism is Robert Brewster of Scrooby (1440-1505) Cambridge MA 1468-9. Most of my Brewster Line family connections with Cambridge were 1588 to 1624, the Golden Age of Second Scholasticism.

However, my Taylor ancestry goes back further, including 21-Great Grandfather Aymer d'Angouleme, comte d'Angouleme, born 1160 20-Great Grandfather Count D'Agouleme William Taillefer born 1200 brother of Isabelle of Angouleme,Queen Consort of England

as wife of King John of England from 1200 to his death in 1216 shortly after the Magna Carta had been initially signed with rebel barons.

In 1209 three Oxford clerks were arrested in connection with the death of a townswoman and King John ordered their death. After their hanging, many Oxford clerks fled Oxford and some of them founded Cambridge.

After King John's death in 1216 Isabelle returned to Angouleme and married Hugh X of Lusignan. Their son William de Valence (1225-1296) was the first Earl of Pembroke (3rd creation). His son Aymer de Valence, 2nd Earl of Pembroke (1275-1324) married Marie de St. Pol. Apocryphal legend: Marie was maiden, wife, and widow all on her wedding day when her husband was killed in front of her in a friendly jousting match. Fact: Marie founded Pembroke College Cambridge with license from Edward III on Christmas Eve 1347.

1647 Brewster-Taylor New Haven Phantom Ship

- 1480 Robert Bacon born; John Taylor, Jr., triplet #1, my 13-Great Grandfather, born
- 1573 Francis Bacon, Grandson of Robert Bacon, adm Fel-Cmnr Trinity Cambridge Francis Brewster I born
- 1617 Francis Brewster II adm Fel Cmnr Pembroke Cambridge



- 1619 Comet African Slaves to Jamestown
- 1624 Francis Brewster II MA Cambridge
- 1632 Francis Brewster I dies
- 1642 Nathaniel Brewster, 4-Great Grandfather of Abraham Lincoln, AB Harvard
- 1647 Nathaniel Bacon, 3-Great Grandson of Robert Bacon, born

New Haven Phantom Ship

Francis Brewster II my 9-Great Grandfather

- John Taylor V (not of the triplets family) 4-Great Grandfather of William Tecumseh Sherman also 4th cousin of my 10-Great Grandfather Thomas Taylor, Jr. (of the triplets family) who was father of my 9-Great Grandfather John Taylor I the immigrant born 1607
- 1649 Cromwell signs Charles I death warrant
- 1650 John Taylor I (of the triplets family) and son James Taylor immigants to Virginia
- 1651 John Taylor I dies
- 1653 Cromwell is Lord Protector
- 1658 Oliver Cromwell dies
- 1660 Charles II, restored Stuart, chartered slave shipment directly from Africa
- 1661 Nathaniel Bacon adm Fel Cmnr St. Catherines Cambridge
- 1665 Nathaniel Brewster first minister of the Presbyterian Church at Setauket
- 1667 Nathaniel Bacon MB Cambridge
- 1674 Nathaniel Bacon immigrant to Virginia
- 1675 Comet
- 1676 Bacon's Rebellion burns Jamestown, Bacon dies, Charles II puts it down
- 1690 Nathaniel Brewster dies

From scrapbookyourfamilytree.com isaacs-story "... "Vision of the Phantom Ship," ... by Jesse Talbot in 1850, recalls ... a New Haven vessel lost at sea in [1647] ...

... merchants at New Haven ... built or had built a ship in Rhode Island (about 150 tons) to be used in trade with England and other countries ... sailors and ship builders called this ship 'crank sided and walty' (or in terms we understand today, very unstable) ... In the winter of 1645/46 the "Great Shippe" was chartered by "The Company of Merchants of New Haven" with Captain George Lamberton in command. ...Because ...

loading ... was delayed, it was not ready to sail until ... about the middle of January **164[7]**, seventy persons boarded the ship, among them were ...



George Lamberton ...

[and my 9-Great Grandfather **Francis Brewster II**, ancestor of Abraham Lincoln and **John Taylor V** (not of the triplets family) 4-Great Grandfather of William Tecumseh Sherman and 3-Great Grandson of my 15-Great Grandfather William Taylor, II, born 1429, who was common ancestor of James Madison, Jr., Zachary Taylor and William Tecumseh Sherman] ...

The vessel was iced in so solidly at its pier, that in order to get to Sea every able man and boy had to help hand-chop a three mile channel out of Long Island Sound. Then the ship had to be towed stern-first through the ice out to the waters of the North Atlantic. This was a chillingly bad omen, and the crew members almost mutinied because of it. ... The ship's master, George Lamberton, an experienced mariner, predicted many times that the "walty" ship would "prove their grave." ...

The ship was never heard from again ...

Six months later ... On a humid June afternoon, heavy thunderstorms descended upon New Haven harbor. Excitement overtook the town as person after person saw their `Great Shippe' emerging from the cloudbanks and sailing into the harbor. However, it was sailing against the winds and above the waves - in the fogged clouds and not touching the waters below. As it approached the shore, and as dusk fell, the main topmast broke off, fell and entangled other sails on the deck. Pieces of the ship seemed to break off. Many watching from the harbor saw a human figure on the bow, sword raised and pointing to the sea, just before the ship, ragged, broken and haunted, rolled over on her side and disappeared into the mists ...

No debris-wood, casks, sails - from the ship was ever found. The water calmed and the mists lifted. The ship had vanished. ...".

From colonialwarsct.org "... Henry Wadsworth Longfellow's The Phantom Ship

In Mather's Magnalia Christi, Of the old colonial time, May be found in prose the legend That is here set down in ryhme. A ship sailed from New Haven, And the keen and frosty airs, That filled her sails at parting, were heavy with good men's prayer. "O Lord if it be thy pleasure" - Thus prayed the old divine -"To bury our friends in the ocean, Take them, for they are thine!" But Master Lamberton muttered, And under his breath said he. "This ship is so crank and walty, I fear our grave she will be!" And the ships that came from England, When the winter months were gone, Brought no tidings of this vessel Nor of Master Lamberton. This put the people to praying that the Lord would let them hear What in his greater wisdom He had done with friends so dear. And at last their prayers were answered: It was in the month of June, An hour before the sunset Of a windy afternoon, When, steadily steering landward, A ship was seen below, And they knew it was Lamberton, Master, Who sailed long ago. On she came, with a cloud of canvas, Right against the wind that blew Until the eye could distinguish The faces of the crew. Then fell her straining topmasts, Hanging tangled in the shrouds, And her sails were loosened and lifted, And blown away like the clouds. And the masts, with all their rigging, Fell slowly, one by one, And the hulk dilated and vanished.mAs sea-mist in the sun! And the people who saw this marvel Each said unto his friend, That this was the mould of their vessel, And thus her tragic end. And the pastor of the village Gave thanks to God in prayer, That, to quiet their troubled spirits, He had sent this Ship of Air.

The Brewster Line and Taylor Branch of ancestry intersected in 1780 and give Common Ancestry with Madison, Taylor, Lincoln and Sherman

Brewster Ancestry Line:

20-Great Grandfather Sir John Brewster I born 1279 died 1299 19-Great Grandfather Sir John Brewster II born 1299 died 1325 18-Great Grandfather Sir John Brewster III born 1325 died 1379 17-Great Grandfather Galfridus Brewster I born 1350 died 1410 he was also 17-Great Grandfather to HRH Charles and to Lady Diana 16-Great Grandfather John Brewster born 1380 died 1441 15-Great Grandfather Humphrey Brewster born 1410 died 1443 14-Great Grandfather Robert Brewster of Scrooby born 1440 (Cambridge MA 1468-9) died 1505 At Cambridge in the Scholastic Era he could have learned about Ramon Llull (1232-1315) 13-Great Grandfather William Brewster of Rushmere born 1470 died 1521 12-Great Grandfather Robert Brewster born 1494 died 1540 his brother William Brewster of Hatfield b 1510 (B.Can.L. Cambridge 1532-3). 11-Great Grandfather Humphrey Clearke Brewster born 1526 died 1593 his son Humphrey Jr matric pens St Johns Cambridge 1588 died 1613 age 44 10-Great Grandfather Francis Brewster I born 1573 died 1632 his Second Cousin William "Elder" Brewster was Pilgrim leader of Mayflower Compact his son John born 1600 adm pens Emmanuel Cambridge 1610 his son Robert born 1599 matric Fel Cmnr Pembroke Cambridge 1617 9-Great Grandfather Francis Brewster II born 1598 (adm Fel Cmnr Pembroke1617 Cambridge MA 1624) he died 1647 on the New Haven Phantom Ship with John Taylor 8-Great Grandfather Nathaniel Brewster born 1618 (Harvard AB 1642) died 1690 he was 4-Great Grandfather of President Abraham Lincoln 7-Great Grandfather Daniel Brewster born 1662 died 1748 6-Great Grandfather John Brewster born 1705 died 1778 5-Great Grandfather John Brewster born 1728 died 1816 in SC 4-Great Grandfather James Brewster b 1756 d 1804 in SC married Mildred Downs 1780 in NC 3-Great Grandmother Sarah Brewster b 1783 d 1857 in GA married James Dickerson 2-Great Grandmother Mary Brewster Dickerson b 1819 d 1895 in GA she married Benjamin Franklin Smith b 1815 d 1893 in GA Great Grandfather James Madison Smith b 1841 d 1884 in GA Grandfather James Madison Smith b 1877 d 1932 in GA Father Frank Dodd Smith b 1906 d 1986 in GA Frank Dodd (Tony) Smith, Jr., born 1941

My closest Common Ancestor with Abraham Lincoln is Nathaniel Brewster (Harvard AB 1642)

Abraham Lincoln 4-Great Grandfather Nathaniel Brewster born 1618 (Harvard AB 1642) Abraham Lincoln 3-Great Grandmother Sarah Brewster born 1656 married Jonathan Smith (son of Bull) Abraham Lincoln 2-Great Grandmother Abigail Smith born 1678 married Isaiah Harrison Abraham Lincoln Great Grandmother Abigail Harrison born 1710 married Alexander (Jr.) Herring Abraham Lincoln Grandmother Bethsheba Herring born 1742 married Abraham (Capt.) Lincoln Abraham Lincoln Father Thomas Lincoln born 1778 Abraham Lincoln born 1809

Taylor Ancestry Branch:

36-Great Grandfather Frankish Aristocrat, born 697

35-Great Grandfather Gerold Von Vinzgau, Graf im Kraichgau und Anglachgau, born circa 725 34-Great Grandfather Udalrich I, Graf in Breisgau, born circa 770 33-Great Grandfather Udalrich II, Graf im Breisgau, born 783 32-Great Grandfather Wulfhard Taillefer d'Angouleme, born circa 783 31-Great Grandfather Wulgrin Tallefer d'Angouleme, born circa 828 30-Great Grandfather Alduin, born circa 866 29-Great Grandfather William I "Taillefer" d'Angouleme, born circa 895 28-Great Grandfather Arnaud "Manzer" d'Angouleme, born circa 927 27-Great Grandfather William Taillefer d'Angouleme, born circa 978 26-Great Grandfather Geoffrey d'Angouleme, born 1014 25-Great Grandfather Foulgues d'Angouleme, born 1015 24-Great Grandfathe Guilaume V 'Taillifer' d'Angouleme, born 1067-1103 23-Great Grandfather Vulgrin II d'Angouleme, born 1070-1130 22-Great Grandfather Guillaume 'Taillefer' d'Angouleme, born circa 1115 21-Great Grandfather Aymer d'Angouleme, comte d'Angouleme, born 1160 20-Great Grandfather Count D'Agouleme William Taillefer born 1200 brother of Isabelle of Angouleme, Queen Consort of England 19-Great Grandfather Baron Hanger Taylifer born 1256 18-Great Grandfather Sir John Taylor (Taylifer), Kt, born circa 1324 17-Great Grandfather William Taylor, I, born before 1377 16-Great Grandfather John Taylor, II, born 1403 15-Great Grandfather William Taylor, II, born 1429 Master of the Rolls of the Court of Chancery 14-Great Grandfather John Taylor, Sr., born 1450 13-Great Grandfather John Taylor, Jr., triplet #1, born 1480 Doctor of Civil Law and Doctor of Canon Law at Cambridge in 1520 12-Great Grandfather Rowland Taylor, Archdeacon of Exeter, born 1510, burned at stake 1555 Doctor of Laws degree from Cambridge in 1534 11-Great Grandfather Thomas Taylor, Sr., born 1548 10-Great Grandfather Thomas James Taylor, Jr., born 1574 9-Great Grandfather John Taylor I, the Immigrant born 1607 8-Great Grandfather Col. James Taylor born 1633 7-Great Grandfather James Taylor II born 1675 his daughter Frances and son Zachary were ancestors of Presidents: James Madison Jr Grandmother Frances Taylor born 1700 married Ambrose Madison James Madison Jr Father Col. James Madison born 1723 James Madison Jr born 1751 Zachary Taylor Grandfather Zachary Taylor I born 1707 Zachary Taylor Father Richard Taylor born 1744 Zachary Taylor born 1784 6-Great Grandmother Martha Taylor born 1702 married Thomas Chew 5-Great Grandmother Frances Chew born 1730 married Henry Downs, Jr. 4-Great Grandmother Mildred Downs born 1760 married James Brewster 1780 in NC 3-Great Grandmother Sarah Brewster born 1783 married James Dickerson 2-Great Grandmother Mary Brewster Dickerson born 1819 married Benjamin Franklin Smith born 1815 Great Grandfather James Madison Smith born 1841 Grandfather James Madison Smith born 1877 Father Frank Dodd Smith born 1906 Frank Dodd (Tony) Smith, Jr., born 1941

According to Wikipedia: "... In 848 Angoulême was sacked by the Viking chief Hastein. ...



... In 896 or 930 the city suffered another attack from invading Vikings but this time the Vikings faced an effective resistance.

Guillaume I, third Count of Angoulême, at the head of his troops

made them surrender in a decisive battle. During this engagement, he split open to the waist Stonius, the Norman chief, with a massive blow together with his helmet and breastplate.

It was this feat that earned him the name Taillefer ... Latin: Incisor ferri, meaning "hewer of iron" ...

which was borne by all his descendants until Isabella of Angoulême

who was also known as Isabelle Taillefer, the wife of King John of England.

The title was withdrawn from the descendants on more than one occasion by Richard Coeur-de-Lion then the title passed to King John of England at the time of his marriage to Isabella of Angoulême, daughter of Count Aymer of Angoulême ...".

My 20-Great Grandfather William Taillefer (1200-1274), younger brother of Isabella of Angouleme, was Count D'Angouleme. A successor Count of Angouleme (Count from 1496 to 1515) was King Fancis I of France who was patron of Giovanni da Verrazano who first came to what is now **New York City** and who named it **New Angouleme** in 1524.

Later (1609 or so) the Dutch fur traders came there and in 1614 named the area New Netherland and New Angouleme became **New Amsterdam**. In 1664 it was traded to the English and renamed **New York**.

My closest Common Ancestor with William Tecumseh Sherman is William Taylor II whose 3-Great Grandson John Taylor V died on the New Haven Phantom Ship with Francis Brewster II

- William Tecumseh Sherman 9-Great Grandfather William Taylor, II, born circa 1429 Master of the Rolls of the Court of Chancery
- William Tecumseh Sherman 8-Great Grandfather John I. Taylor I, born 1451
- William Tecumseh Sherman 7-Great Grandfather John Taylor of Shadoxhurst, born circa 1480 not of the triplets family
- William Tecumseh Sherman 6-Great Grandfather John Taylor born 1522
- William Tecumseh Sherman 5-Great Grandfather John Taylor IV born 1563
- William Tecumseh Sherman 4-Great Grandfather John Taylor V born 1603 died Phantom Ship
- William Tecumseh Sherman 3-Great Grandfather Thomas Taylor born 1642
- William Tecumseh Sherman 2-Great Grandfather Nathan Taylor born 1681
- William Tecumseh Sherman GreatGrandmother Mindwell Taylor born 1727 married Daniel Sherman

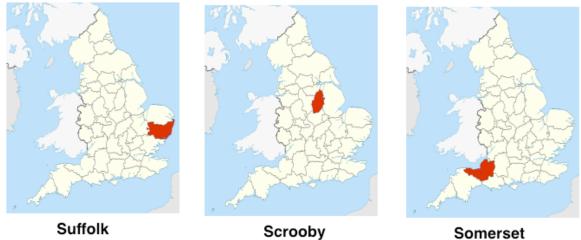
William Tecumseh Sherman Grandfather Taylor Sherman born 1759

William Tecumseh Sherman Father Charles R. Sherman born 1788

William Tecumseh Sherman born 1820.

Francis Brewster I

12-Generation 10-Great Grandfather of Frank Dodd (Tony) Smith Jr Born 1566 in Suffolk England. Died 1644 in Somerset England.



Suffolk and Somerset were Parliamentarian in the English Civil War.

The earliest Brewster to attend University was the 2-Great-Grandfather of Francis I Robert Brewster, of Scrooby, b. 1440 d. 1505, MA Cambridge 1468-9.

Francis I did not attend University

but was able to send his three sons to Cambridge where his brother had matriculated and to send two of his grandsons to Cambridge and to Harvard.

How did Francis I make enough money to send children and grandchildren to Cambridge and Harvard ?

His father Humphrey Clearke Brewster (1526-1593) (according to Burke's Landed Gentry) "... purchased the manor and living of Wrentham, and in 1556, built the hall there, at which his descendants continued to reside until 1794 ... The income of the proprietors of Wrentham was derived from lands in more than twenty parishes in Suffolk and Norfolk. In the former county the Brewsters possessed leading influence, and in the great rebellion became partisans of the parliament ... Humphrey [Clearke] Brewster ... had ... sons ... [William b. ca 1566] and

Francis [I] his heir ... b. in 1566 ... d. in 1644 ...[and]

Humphrey [Jr]... [who matriculated as Pensioner St. John's Cambridge in 1588; admitted Middle Temple 1596 from New Inn, b. 1569 died 1613 at age 44] ...

and

four dau[ghter]s ... Elizabeth ... Susan ... Mary ... and Jane ...

The elder son and heir **Francis Brewster [I**], Esq. of Wrentham Hall ... an active parliamentarian during the rebellion as a magistrate and deputy-lieutenant ... had ...[sons Francis II 1598-1647, Robert 1599-1663, and John b. 1600 and daughters Gillian Brewster and Mary Garth]

> [Fellow-commoner; the first of the three ranks in which students were matriculated Pensioner; the second of the three ranks in which students were matriculated Sizar. The third of these ranks. In old times sizars performed many menial services.]

- John ... b. in [1600]... d. in 1677 ...[subscribed Oxford 1613 admitted Pensioner Emmanuel Cambridge 1620 adm at Gray's Inn 1623]... was a member of the parliament committee formed for the preservation of the peace of the county of Essex ...
- Robert ... b. in [1599]... d. in 1663 ... [matriculated as Fellow Commoner Pembroke Cambridge in 1617; MP for Dunwich and for Suffolk]... had two sons ...

Francis ... b. in 1623 ... [matriculated as Fellow Commoner St. Catherine's Cambridge in 1642 adm at Gray's Inn 1646]... d. 1671 ...

Robert ... b. in 1625 ... d. in 1681 ...

Francis [II], of Wrentham, b. in [1598] ... [was admitted (age 17) as Fellow Commoner Pembroke Cambridge in 1617; matriculated in 1618; received BA in 1620;



received MA in 1624. He was a Barber/Surgeon and a Puritan. ...

By the sixteenth century ... the Castle of Bristol ... had fallen into disuse, but the City authorities had no control over royal property and the precincts became a refuge for lawbreakers ... On 23 Aug 1626 ...[Frances II]... received a lease of the ... castle ... from King Charles I, for a period of 80 years ... In 1630 the city bought the castle ...

In 1638 ...[Francis II]... was one of the original settlers of New Haven ... the Civil War broke out [in 1642 The overall outcome of the war was threefold: the trial and execution of Charles I (1649); the exile of his son, Charles II (1651); ... the replacement of English monarchy with ... the Commonwealth of England (1649-53) ... then the Protectorate under ... Oliver Cromwell (1653–58) and his son (1658–59)]...

Around 1647 he died at sea aboard the Lombard Phantom Ship]... having had issue ...[daughters Mary French b. 1633 and Hannah Thompson and ? Herbert sons Nathaniel 1618-1690, John b. 1632 and Robert b. 1638 and Francis 1627-1694, Joseph b. 1628 and Benjamin b. 1644]

Mary, daughter of Francis II, testified at a 1654 New Haven witch trial

Witchcraft officially became a crime in Connecticut in 1642 ... New Haven enacted its witchcraft law in 1655 ... almost all of alleged witches were hanged ... no witch was ever burned at the stake in Connecticut (<u>www.damnedct.com/connecticut-witchcraft-trials</u> and !The Witchcraft Delusion in Colonial Connecticut (1647-1697) by John M. Taylor)]

Nathaniel ... b. in [1618 d. 1690]...

[enrolled in Harvard in 1639 and was in Harvard's first graduating class,



receiving the AB degree in 1642, ... Nathaniel then moved to England and became a cleric in the Church of England. In 1644 Nathaniel married Abigail Reynes with whom he had 3 children. In 1653 Oliver Cromwell was made Lord Protector of England, Scotland, and Ireland. After Abigail's death in 1654 Nathaniel attended Trinity College in Dublin receiving the B.D. degree in 1656. While in Dublin Nathaniel married Sarah Ludlow with whom he had 7 children. The English Restoration Uniformity Act of 1662 drove Puritan ministers from the Church of England to Presbyterian and Congregational Churches. In 1663 Nathaniel moved to Boston. In 1665, the year of Isaac Newton's B.A. degree from Trinity College, Cambridge (which then closed for the 1665-1666 Great !Plague), Nathaniel moved to Suffolk County, Long Island, becoming the first minister of the Presbyterian Church at Setauket (Brookhaven Twp.)]...

This family had many ramifications;

one offshot ... was established in the United States by William [Elder] Brewster ... the ruling elder and spritual guide of the Pilgrim Fathers who, in 1620, went out to America to avoid the religious persecutions to which they were exposed, and were the founders of New England ...[He was born 1565 in Scrooby Nottinghamshire; matriculated as Pensioner Peterhouse College Cambridge 1580; Y-DNA Haplogroup I-M253; died 1644 Plymouth, **second cousin of Francis I** [His father]... William Brewster of Scrooby b. 1534 ... died in 1590 ... was appointed Receiver and Bailiff of the Archbishop's estates at Scrooby in 1575 for the duration of his lifetime. ...[and]... was succeeded by his son ... From 1606-7 [Elder] Brewster held Separatist meetings in the manor house. Around 1636-7 most of the manor house and its outbuildings were demolished following a demolition order granted by Charles I (www.scrooby.net/page/scroobyManorHouse)]

...[Brewster] Mottto - Verite soyet ma garde [Truth be my shield]...".

John Whistler

1700-1750

In Scotland, my 6-Great Grandfather Angus McIntosh of Inverness supported exiled Stuarts and participated in the Jacobite Rebellion to overthrow the House of Hanover. He and his daughter, my **5-Great Grandmother Ann McIntosh** were captured and she was shipped to Orange County VA as an Indentured Servant.

In Africa, my **5-Great Grandfather John Whistler** (or his ancestors) was captured and shipped to Orange County VA as a Slave.

1750-1800s

In Virginia, my 5-Great Grandparents John Whistler and Ann McIntosh were effectively husband and wife as slave / servant of Arjalon Price in Orange County VA. In 1756 they had my 4-Great Grandmother Molly a/k/a Mary a/k/a Frankey McIntosh who became property valued at 20 pounds.

For that pregnancy Ann was banned from the church and whipped fifty lashes. In 1787 Molly gave birth to my 3-Great Grandmother Mary McIntosh who at age 16 in 1803 obtained a a certificate from David Jamison, a justice of the peace from Culpeper County, and produced it in the District of Columbia Court in Alexandria on 17 November 1803 declaring that she was born free. She then moved to Richmond County NC and married John McKennon. In 1810 they had my 2-Great Grandmother Margaret McKennon who married Malcolm McKinnon. They moved to Echols County Georgia, and in 1843 had my Great Grandmother Mary Frances McKinnon who married William Jeremiah Absolom Ham and gave birth in 1875 to my Grandfather George Clinton Ham, father of my Mother Willie Julia (Billie) Ham.

The history of Britain's wars such as the Jacobite Rebellion and its use of Indentured Servitude to send war losers and poor people to America as servant labor substantially equivalent to slave labor is well known but

the history of the African Slave Trade is less well known:

Tim Hashaw in "The Birth of Black America" said:

"... Long before the birth of Jesus there had flourished in East Africa the magnificent city-state of Aksum. Ideally situated to control the long flow of trade passing from Asia and East Africa through the Red Sea to the Mediterranean, Aksum ... became [a] great cosmopolitan center... in the ancient world. By Roman times, the wealth and influence of Aksum was envied throughout the Mediterranean, and its people, the Ethiopians, were widely famed for piety, justice, hospitality, and a long, unbroken tradition of literature. In the fourth century A.D. ... Ethiopia under King Ezana ... established the world's first Christian state. ... The Christian rulers of Ethiopia had been tolerant of all religions, including Judaism and Buddhism. Because Christian Ethiopians had offered refuge to persecuted Muslims, the Prophet Muhammad, according to Islamic tradition, had instructed Muslim armies to leave Ethiopia in peace ...

on August 28, 1482 ... the Portuguese explorer Diogo Cao became the first European to reach the mouth of the great Congo (Zaire) River, six degrees south of the equator. Here he found unexpected evidence of an impressive advanced civilization; Africans unknown to the Mediterranean world yet refining gold, silver, copper, and iron and clothed in fine garments ...

This was ... [a] kingdom...[that] gave their kings the title of ngola (iron blacksmith), from which comes the name of the country, "Angola"

in the 1520s ... Somali Muslim warlord ... Ahmed Gran, son of an Ethiopian Christian priest and a Somali prostitute, invaded Ethiopia ... captured and burned Aksum ...

in 1616 ... at Jamestown ... the Virginia Company shifted its focus ... to social and economic ventures intended to create a permanent colony of consumers, producers, and manufacturers with whom company investors hoped to trade

•••

at the latter end of 1618, King James's chronicler William Camden had reported the sudden appearance in the sky of a comet ... on December 7, 1618, as the corsairs White Lion and the Treasurer were preparing to leave for the West Indies, Camden reported the comet visible at the latitude of Jamestown ... in 1619 ... the first Africans ... [were brought]... to English-speaking America from Angola

... The Spanish slave frigate San Juan Bautista left Africa with 350 slaves and crossed the Atlantic to be captured in the Gulf of Mexico in the summer of 1619 by two English pirate ships - the White Lion ... and the Treasurer the first Africans in English North America were ... delivered to Jamestown ... in 1619 ...

two dozen ... by the White Lion and ... half dozen [by]... the Treasurer

...

In less than two decades after arriving, many of this skilled and intelligent first generation of Jamestown Africans were free and had established their own farms and communities in Tidewater Virginia ... From 1619 to 1676, one generation has a brief opportunity to bestow freedom upon its descendants

...

Nearly sixty years [after 1619], Virginians saw another comet in the latitude of Jamestown ...

England in 1660 invited Charles II, grandson son of James I, to return to the throne and restore the Stuart dynasty. ... Charles II, among other things, that year gave the Royal African Company a charter to ship slaves directly from Africa. No longer would American plantations tions rely on freelance pirates raiding Spanish and Portuguese frigates for slaves. In 1660, slavery became a British industry, ... Britain sold Africans to the faraway colonies to do jobs that English peasants did not want to do. Between 1648 and 1681, the number of whites in Virginia increased by 5.2 percent, while the number of blacks in Virginia in the same time period increased by 10 percent, due in large part to imported Africans ... Thus began **Bacon's Rebellion** [of 1676]...

Nathaniel Bacon, a planter and the first American populist. Bacon raised an army by promising freedom to every enslaved African and indentured Englishman who would run away and join him. ...

Six months later, Bacon's campaign ceased being a war against natives and became a war of the colonial underclass against Jamestown's ruling royalist elite. Free black and white farmers, plus runaway Angolan fugitives, marched to Jamestown to protest government abuses and cast Berkeley and his favorites out of power. Governor Berkeley fled and, at the high point of the attack, Bacon's army, by then largely African, seized the colonial capital and burned it to the ground.

In the ashes of Jamestown, Governor Berkeley appealed to the Stuart king of England, who gave him a fleet to put down the ... rebels. Bacon died of natural causes at this time and the rebellion, though as powerful as ever, had no capable leader. ...

The royalist elite returned and rebuilt Jamestown. They of course did not ignore the great number of Africans in the rebellion and took steps to prevent a future reoccurrence.

•••

After 1660, as the number of imported Africans dramatically increased, issues involving the status of Africans passed from the local courts to the colonial legislature, particularly as a result of Bacon's Rebellion ... in 1691, the Virginia legislature ... outlawed mixed marriages and required that mixed children born out of wedlock to European women be bound as servants for thirty years ... European women and their offspring could not be enslaved ... in 1723, the Virginia Assembly took the last step and banned outright the freeing of slaves, unless they had performed some notable public service, such as reporting a planned slave rebellion ...".

According to britannica.com "... Nathaniel Bacon, (born January 2, 1647, Suffolk ... died October 1676, Virginia ... leader of Bacon's Rebellion (1676),

the first popular revolt in England's North American colonies.

A kinsman of the famous Sir Francis Bacon ...[their closest common ancestor was Robert Bacon b 1480 d 1548 Grandfather of Francis Bacon b 1561 d 1626 an English philosopher, statesman, scientist, jurist, orator, and author known as the father of empiricism Adm Fell-Com Trinity 1573 Matric 1573 Adm at Gray's Inn 1576 MA 1594 and 3-Great Grandfather of Nathaniel Bacon b 1647 d 1676]...

Nathaniel Bacon graduated from the University of Cambridge ...[Adm Fell-Com at St Catherine's 1661 adm at Gray's Inn 1664 MB 1667]...".

Maternal Line at Garden of Eden

Overview: my Mother's side Maternal ancestors U5 migrated out of Africa about 150,000 years ago to Finland



(years ago = BP = Before Present)

150,000 BP - Mitochondrial Eve - Haplogroup L1

75,000 BP - Haplogroups L2 and L3 - went out of Africa across the Red Sea

50,000 BP - Haplogroup N branched off of L3 to Incubation Period in Garden of Eden



Cousins of my Maternal DNA Line:

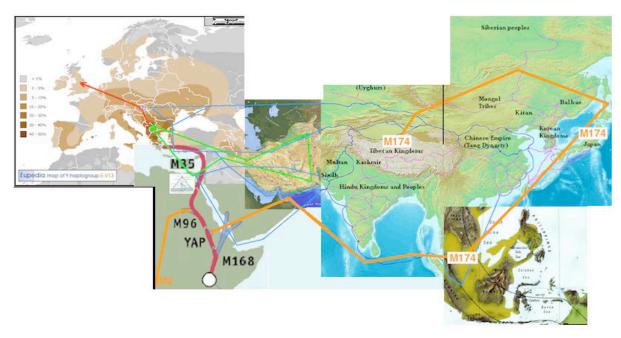
Part of Haplogroup N were ancestors of Noah who went with the Persian Gulf Flood to the Yemini Coast to Ethiopia, home of Abraham and Moses who went up the Nile to GizaPaternal Line at Nile River



According to Y-DNA, Enoch = Boskop descendants moved up the Nile to Giza and across the Indian Ocean to Sunda, Japan, and Tibet. The corresponding M-DNA migration to Sunda was by Haplogroup M branching off of L3

Paternal Line Cousins at Angkor Wat

Overview: my Father's side Paternal ancestors E3b1= E-V13 migrated out of Africa about 50,000 years ago to Britain with Roman Legions



50,000 BP - Africa Haplogroup M168



50,000 - 40,000 BP - Africa Haplogroup YAP



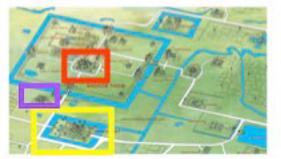
Cousins of my Paternal Y-DNA Line: 50,000 BP - M174 leaves YAP from Africa to Sunda, Japan, Tibet



Tibet - I Ching 64 = E8 triality

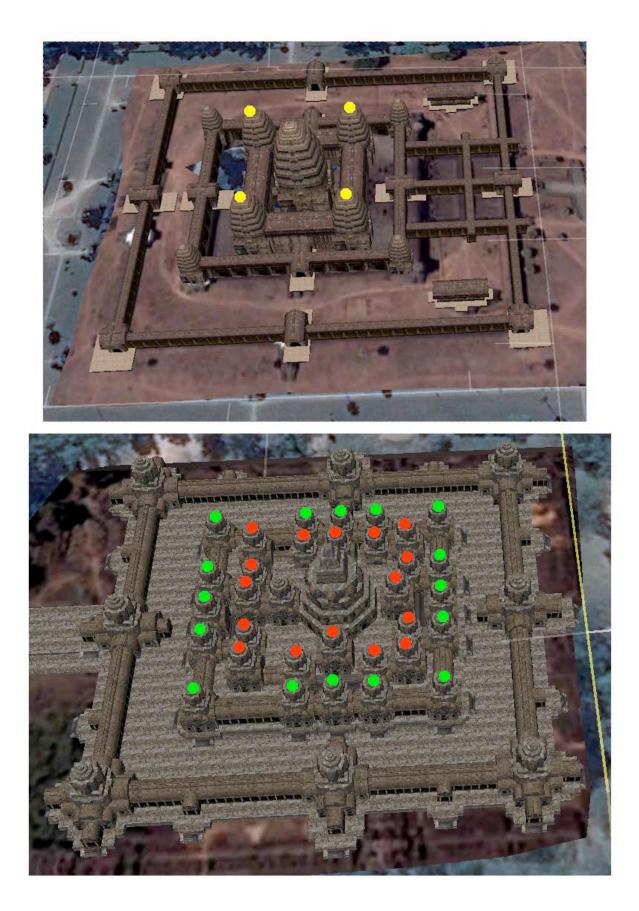
Japan - Shinto Futomani 128 = E8-Cl(16) half-spinor

Sunda - Origin of India-China Asia population (HUGO, Science 326 (2009) 1541- 1545) Rg Veda - 240 E8RV Hindu - Sanskrit - Mt Meru 256 = Cl(8) = Cl(16) spinor Angkor Wat (yellow) - Angkor Thom (red) - Phnom Bakheng (purple)



(tourismcambodia.com map)

Angkor Wat has 4 pillars around its center - IFA Tetragram = 4 bars out of 8 = 4e + 4oAngkor Thom has two arrays of 16 pillars each around its center - 16x16 = 256 IFA Odu Both are enclosed in 8-pillar squares - 8 IFA Opele Chain Elements - $2^8 = 256$ IFA Odu Both centers have 8 layers - $2^8 = 256$ IFA Odu = dim Cl(1,7) = Cl(8)



According to Wikipedia: "...Phnom Bakheng is a symbolic representation of Mount Meru ... a status emphasized by the temple's location atop a steep hill 65 m above the surrounding plain. The temple is built in a pyramid form of seven levels ... At the top level [are] five sandstone sanctuaries - [as in] Angkor Wat seen from Phnom Bakheng ...

... Originally, 108 small towers were arrayed around the temple at ground level and on various of its tiers; most of them have collapsed ...".



(google earth images)

Phnom Bakheng has 3-mile square moat with area $3^2 = 9$



Angkor Thom



Angkor Wat

has 2-mile square moat $2^2 = 4$

has rectangular moat with 1-mile base

Paternal Line at Nile River to Great Pyramid

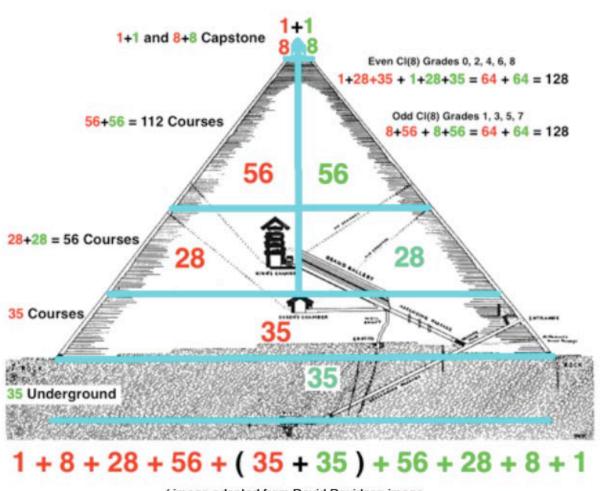
40,000 BP - M96 leaves YAP and goes up Nile Cousins of my Paternal Y-DNA Line: M2 branch going back south to Boskop



36,000 BP - M96 continues up Nile to build the Great Pyramid and during its construction to invent the efficient Hebrew Alphabet and the time of Late Wisconsin Glaciation and the time that the shock wave of the Geminga Supernova hit the Earth and beginning of Manetho's Rule of Gods on Earth (36,000 to 22,000 BP)



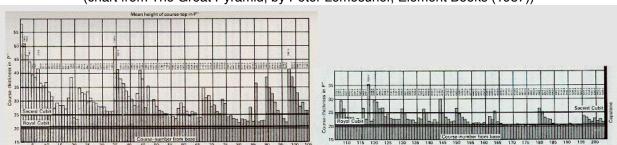
The Builders of the Great Pyramid who had migrated throughout the length of the Nile along which substantially contiguous settlements enabled them to maintain enough contact to maintain the details of the oral traditions of IFA so that when they built the earliest of the pyramids, the Great Pyramid, they did not deface it with any writing but instead encoded the IFA Clifford Algebra in the structure of the Pyramid itself: The Great Pyramid is built of 203 layers (courses) plus a now-missing capstone represented by 1+1 + 8+8 = 18 for a total of 221 courses above ground level. The Subterranean Pit is as deep below ground level as Queen's Chamber is above it so the Subterranean Pit depth equivalent to 35 courses is dual to the Queen's Chamber height of 35 courses just as the 70 mid-grade grade 4 elements of the Cl(8) Clifford Algebra are (35+35) 35 elements plus 35 elements, dual to each other. When the Subterranean 35 courses are included, the total number Courses of the Great Pyramid is 221 + 35 = 256 = number of IFA Odu and dimension of IFA Clifford Algebra Cl(8)



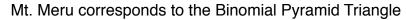
CI(8) = 1 + 8 + 28 + 56 + (35 + 35) + 56 + 28 + 8 + 1

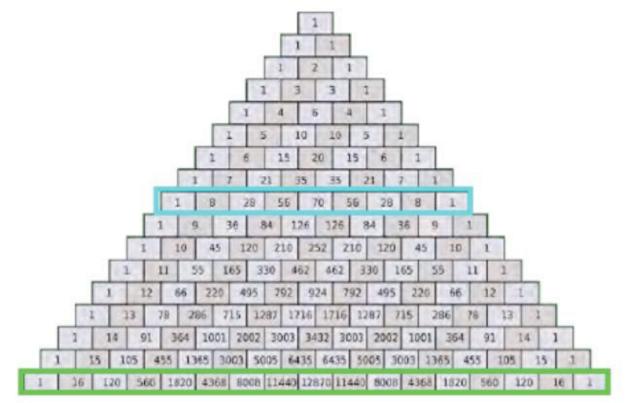
(image adapted from David Davidson image for a larger version of this image go to tony5m17h.net/GreatPyrCl8.png
 or valdostamuseum.com/hamsmith/GreatPyrCl8.png)
(for more details about the Great Pyramid Geometry correspondences see viXra 1305.0060)

1 and 4 and 9 are the top three components of the Square Pyramidal Number of order 8 1+4+9+16+25+36+49+64 = 204 = 203 courses of Great Pyramid + Capstone



(chart from The Great Pyramid, by Peter Lemesurier, Element Books (1987))





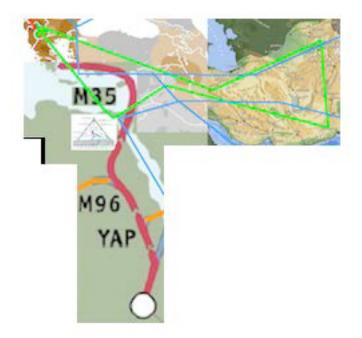
Square Pyramidal Number of order 16 = 1496 = 8 x 11 x 17

Paternal Line and Cousins with Alexander the Great

22,000 BP - M35 leaves M96 and Africa to cross Mediterranean from the Nile Delta into the Middle East and Kosovo / Macedonia Manetho's Rule by Demigods and Spirits of the Dead (22,000 to 11,000 BP) ended after Ice Age when sea levels rose requiring agri-tech for survival Manetho's Rule of Mortal Humans began 11,000 BP which was about 25-26,000 years after the Geminga shock wave 11,000 BP also had a supernova (Vela X) and the Sphinx was built.

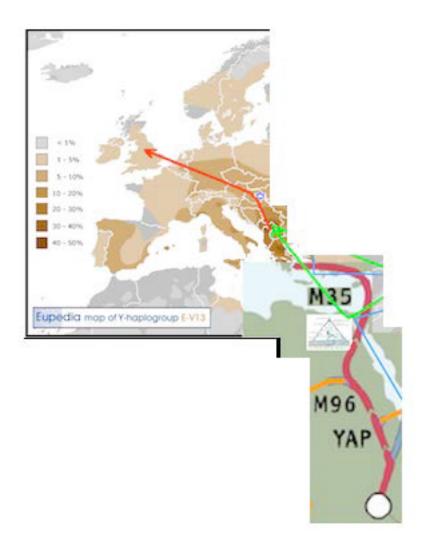


8,000 BP - During Manetho's Rule of Mortal Humans (11,000 BP through now) 330 BC - Cousins of my Paternal Y-DNA Line - Alexander the Great army goes East to India and South to Great Pyramid / Alexandria and then returns to Kosovo / Macedonia.



Paternal Line Roman Legions, Radhanite Cousins, and End of Line

100 BC - Gaius Marius formed Roman Legions using Kosovars / Macedonians. 130 AD - Roman Legions controlled Danube / Rhine / Britain (up to Hadrian's Wall).

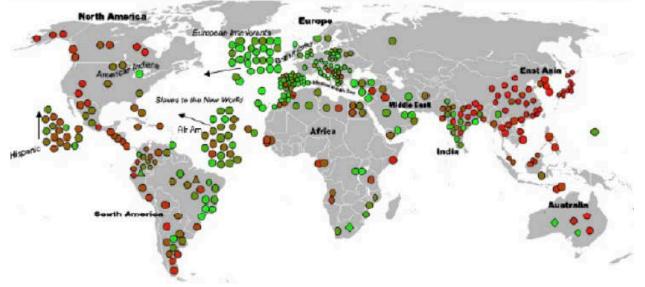


Cousins of my Paternal Y-DNA Line E-V13 that had evolved from M35: 300 AD - Hungarian Ashkenazim founded 500 AD - Ashkenazim in Hungary set up Radhanite Europe / Tang China trade



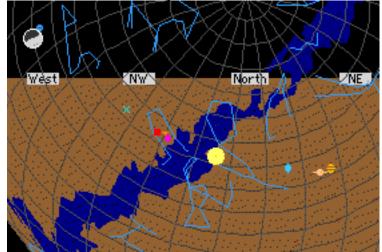
1000 AD - Tang Dynasty ended and Venice, Genoa, etc. succeeded Radhanites

1000-2000 AD - my European and African Ancestors came to America

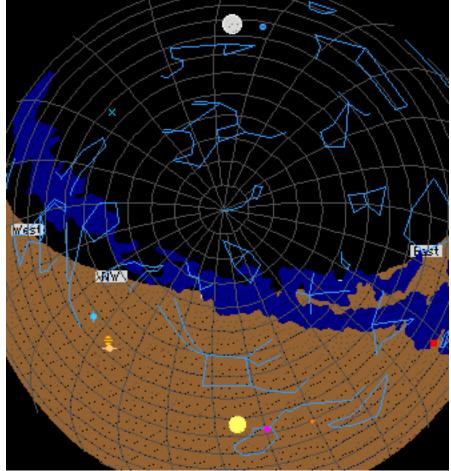


(my MIchigan Native American Ancestors were already in America)

2017 AD - I Frank Dodd (Tony) Smith, Jr., am 76 years old, having been conceived on Shavuot, 6-7 Sivan, 5700 (12-13 June 1940) (year of Metal and Dragon) in the Braban Hotel in Cartersville, Georgia, USA,



and born on Purim, 14 Adar, 5701 (13 March 1941) (year of Metal and Snake) in Cartersville, Georgia, USA, at about 1 AM Eastern Standard Time



Since I have no issue,

my Paternal Y-DNA Line (and all my other Lines) ends with me Frank Dodd (Tony) Smith, Jr. - AB Princeton 1963



Silver + Palladium

Ag = currency Pd = Cold Fusion of D+D+D+D -> He + He + 48 MeV Tiger Eye = Quartz SiO2 intergrown with Goethite Fe2O3.H2O = needle iron ore with Ferric Fe3+ Iron(III) hydrated with nH2O = Limonite Iron = Steel Industry

Limonite = H20 neutron absorption + Iron charged-particle absorption = Mike Shield



Operation Ivy H-bomb Mike 82 tons 1 November 1952



ADVANCED CALCULUS by H. K. NICKERSON, D. C. SPENCER AND N. E. STEENROD the honors course in Advanced Calculus ... Princeton University TABLE OF CONTENTS

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II. LINEAR TRANSFORMATIONS OF VECTOR SPACES - leads to Lie Groups and

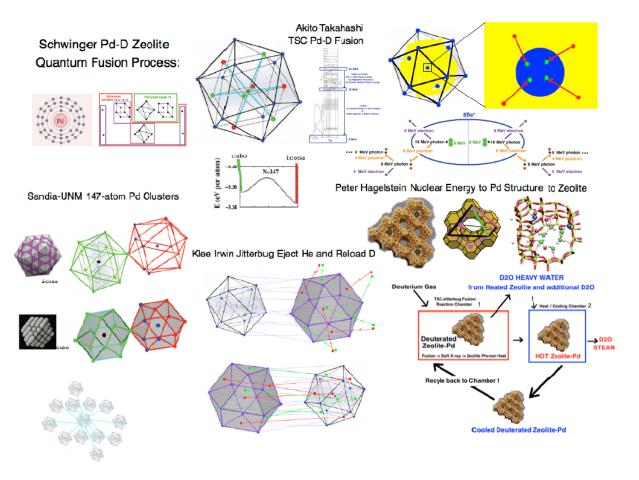
Symmetric Spaces

III . THE SCALAR PRODUCT IV. VECTOR PRODUCTS IN R3 - leads to Vector Products in R7 V. ENDOMORPHISMS VI. VECTOR-VALUED FUNCTIONS OF A SCALAR VII. SCALAR-VALUED FUNCTIONS OF A VECTOR VIII. VECTOR-VALUED FUNCTIONS OF A VECTOR IX. TENSOR PRODUCTS AND THE STANDARD ALGEBRAS - leads to Clifford Algebras and Spinors X. TOPOLOGY AND ANALYSIS XI. DIEFEBENTIAL CALCULUIS OF FORMS

XI. DIFFERENTIAL CALCULUS OF FORMS XII. INTEGRAL CALCULUS OF FORMS XIII. COMPLEX STRUCTURE - leads to Potential Theory, Green's Functions, Bergman Kernels, Bounded Domains, and Schwinger Sources

This text has the basic background for my E8 Cl(16) Physics - viXra 1602.0319

Cold Fusion - Deuterium in 147-atom Pd nanoclusters embedded in Zeolite Cages



Frank Dodd (Tony) Smith, Jr. - 2016 - viXra 1603.0098

Abstract:

147-atom Palladium clusters embedded in Zeolite cavities enable Cold Fusion when exposed to Deuterium gas by Klein Paradox Tunnelling of D+D+D+D producing He + He + 47.6 MeV. Cold Fusion Energy goes to Optical Mode Phonons in the Pd clusters and then to the Zeolite where it is stored as Heat that is released by D2O Heavy Water to produce useful energy. Ejection of He + He and reloading of D+D+D+D is done by Jitterbug transformation between Icosahedral Ground State and Cuboctahedral Metastable State of 147-atom Pd clusters. Synthesis of 147-atom Pd clusters has been done by Burton, Boyle, and Datye at Sandia / U. New Mexico, USA. Zeolite synthesis has been discussed by Sharma, Jeong, Han and Cho at Chungnam Nat. Un., Korea. Based on prior experimental results of Arata and Zhang (replicated by McKubre at SRI) and of Parchamazad the expected energy production is on the order of kilowatts per milligram of Palladium.

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How does Pd-D Cold Fusion Work ?

Julian Schwinger in 1990 lecture at Universite de Bourgogne said:

"... in the very low energy cold fusion, one deals essentially with a single state, described by a single wave function, all parts of which are coherent ...".

Akito Takahashi proposed a process Tetrahedral Symmetric Condensation (TSC) that for 4 Deuterons (D) in an icosahedral cluster of Palladium (Pd) atoms produces a Schwinger coherent quantum state

that effectively distributes the electron population among deuterons so that the Coulomb barrier is eliminated and the four Deuterium (D) nuclei can simultaneously interact and fuse, forming two 4He nuclei plus 47.6 MeV energy. Peter Hagelstein used phonon models for Relativistic Coupling Between Lattice Vibrations and Nuclear Excitation, enabled by break-down of Foldy-Wouthuysen transformation due to 8-15 THz Lattice Vibration Modes, to show direct transfer of the 47.6 MeV energy of Cold Fusion to the Pd lattice as excited optical phonon modes.

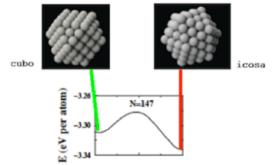
The only Cold Fusion experiments producing heat consistently and reproducibly are the detections of heat using Pd Clusters and Deuterium gas

by Arata and Zhang (replicated by McKubre at SRI) and by Iraj Parchamazad. Arata and Zhang (and SRI) used Palladium black with initial cluster sizes distributed around 5 nm so that a substantial number of Pd clusters had diameter 1.5 nm. However, clumping increased the cluster size to around 40 nm at which size Takahashi et al said, based on their similar work, the "heat-power level drop[ped]... drastically".

(see Current Science 108 (25 Feb 2015) LENR Special Section Preface) Iraj Parchamazad and Melvin Miles avoided the clumping problem by growing the Pd clusters within Zeolite cavities. Using Sodium Zeolite Y whose cavity size is around 1.2 nm (but capable of expansion by about a factor of 2), they produced Pd clusters of 1.5 nm size size which were dispersed within the Zeolite cavities thus preventing clumping. Upon exposure of his Pd clusters in Zeolite to Deuterium gas, he produced heat in 10 out of 10 experiments with **Cold Fusion Energy on the scale of kiloWatts per milligram of Palladium**.

(see coldfusionnow.org/iraj-parchamazad-lenr-with-zeolites/)

1.5 nm diameter Pd clusters have 147 atoms and can be in two states: an Cuboctahedral Metastable State and an Icosahedral Ground State

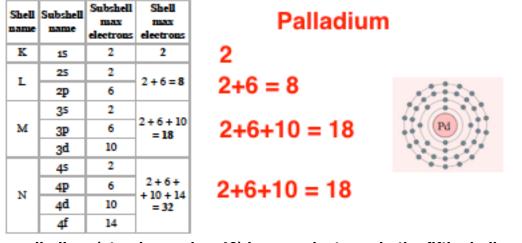


that can transform into each other by a Fuller Jitterbug Transformation.

Why is Palladium uniquely useful for Deuterium Cold Fusion ?

10 11 12 13 14 15 16 17 1 2 . ٠ 12 ≤ 1 3 ۲ * * * * * * * * * * ۲ ٢ -4 * * * * * * * 5 ÷ 6 7 Lanthanides Actinides

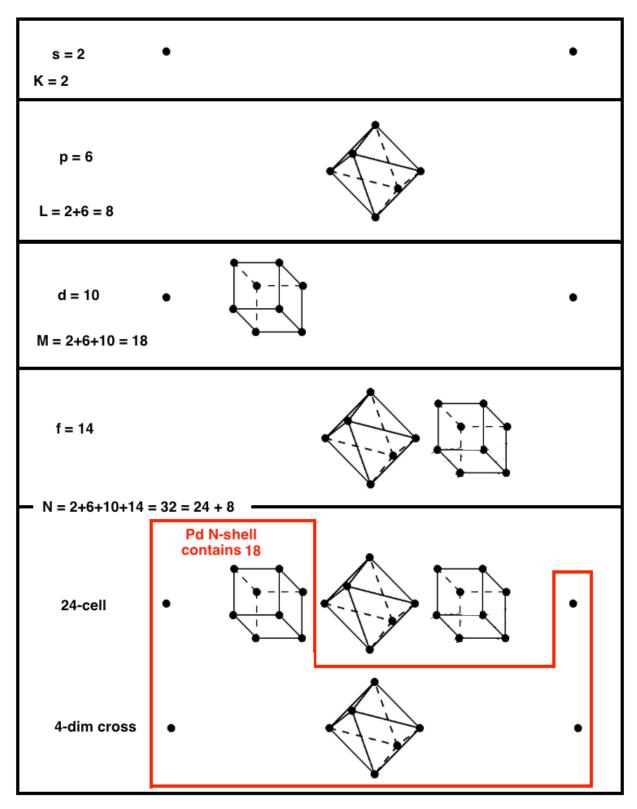
... Each s subshell holds at most 2 electrons Each p subshell holds at most 6 electrons Each d subshell holds at most 10 electrons Each f subshell holds at most 14 electrons Each g subshell holds at most 18 electrons ...



palladium (atomic number 46) has no electrons in the fifth shell, unlike other atoms ...[in its periodic table neighborhood]...".

Pd has uniquely closed electron shell structure. Wikipedia says (I added red material specifically about Pd): "...

. . .



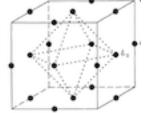
(24-cell image from John Baez review of "On Quaternions and Octonions" by Conway and Smith)

Geometrically:

2 of the First Shell corrrespond to the Root Vectors of B1 = Spin(3)

8 of the Second Shell correspond to the Root Vectors of B2 = Spin(5)

18 of the Third Shell correspond to the Root Vectors of B3 = Spin(7)



(image from Representation Theory by Fulton and Harris)

The B3 Root Vectors live in 3-dim space, which is where Element Electron Shells live.

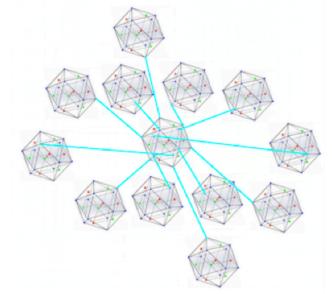
32 of the Fourth Shell correspond to the Root Vectors of B4 = Spin(9)

Palladium is the only element whose outer shell has more electrons than the 8 electrons of noble gases beyond Helium.

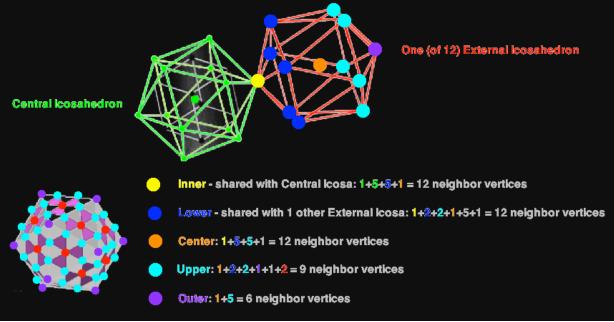
The 18 electrons in the outer shell of Palladium replicate the full state of the Third Shell (M shell).

What is the structure of the icosahedral 147-atom Pd cluster ?

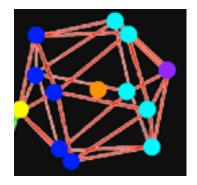
The icosahedral 147-atom ground state has 12 exterior icosahedra and a central icosahedron with 12 interior vertices which are the innermost vertices of 12 exterior TSC Fusion site icosahedra:



The 12 exterior icosahedra each have outer faces on the outer boundary of the 147-atom cluster.



147 = 1+12+30+12+72+20:1 atom is at the cluster center 12 atoms surround the cluster center 5 x 12 / 2 = 30 atoms are in the next layer out 12 atoms are at centers of exterior icosahedra 12 x 6 = 72 atoms are on outer surface of exterior icosahedra 20 atoms are on outer surface between exterior icosahedra The 20 Exterior-Face-Center Pd atoms each have 3+6 = 9 neighbors. Each of the 12 exterior icosahedra of the 147-atom cluster has 13 Pd atoms:

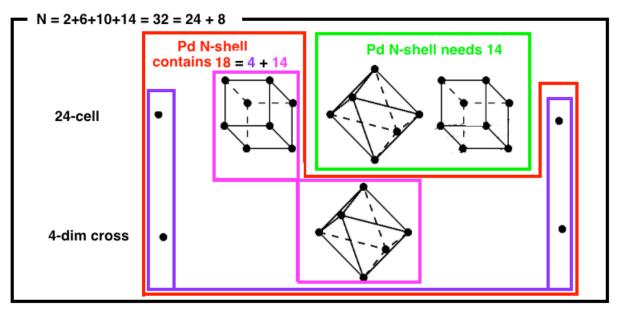


How do the Palladium atoms in a cluster interact with each other ?

The interaction is primarily through the outer shell of electrons (N-shell for Palladium).

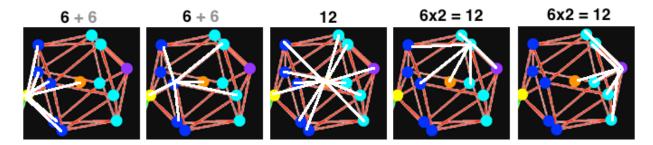
A full N-shell has s + p + d + f = 2 + 6 + 10 + 14 = 32 electrons.

Palladium N-shell has 2 + 6 + 10 = 18 electrons and "holes" to receive 14 electrons:



Each Palladium atom has 18-14 = 4 N-shell electrons that can interact with 4 electrons of 4 Deuterium atoms absorbed into a Pd cluster, helping them to participate in a Schwinger coherent quantum state for TSC Fusion.

Further, each Palladium atom has 14 N-shell electrons 12 to fill needs of other Pd atoms and 2 for a Dirac Fermion Band for Klein Paradox Tunnelling.



6x2 = 12: For the 1 exterior vertex Pd with 6 neighbors,

all 6 of which are in the icosahedron,

12 electrons go 2 to each icosahedron neighbor

and 14-12 = 2 electrons go to a Dirac Fermion Band for Klein Paradox Tunnelling. It receives 12 electrons, 2 from each of its 1+5 = 6 icosahedron neighbors leaving 2 holes related to Dirac Fermion Band for Klein Paradox Tunnelling.

6x2 = 12: For each of the 5 exterior surface Pd with 9 neighbors,

2+1+2+1 = 6 of which are in the icosahedron,

12 electrons go 2 to each icosahedron neighbor

and 14-12 = 2 electrons go to a Dirac Fermion Band for Klein Paradox Tunnelling. It receives 12 electrons, 2 from each of its 2+1+2+1 = 6 icosahedron neighbors leaving 2 holes related to Dirac Fermion Band for Klein Paradox Tunnelling.

12: For the 1 central Pd with 12 neighbors,

all 12 of which are in the icosahedron,

12 electrons go 1 to each icosahedron neighbor

and 14-12 = 2 electrons go to a Dirac Fermion Band for Klein Paradox Tunnelling. It receives 12 electrons, one from each of its 1+5+5+1 = 12 icosahedron neighbors leaving 2 holes related to Dirac Fermion Band for Klein Paradox Tunnelling.

6 + **6**: For each of the 5 interior Pd shared with 1 other icosahedron and with 12 neighbors, 1+2+1+2 = 6 of which are in the icosahedron,

6 electrons go 1 to each icosahedron neighbor

and 14-6 = 8 electrons go 2 to a Dirac Fermion Band for Klein Paradox Tunnelling and 6 to the other icosahedron.

It receives 6+6 = 12 electrons, 1 from each of its 1+5 = 6 icosahedron neighbors and 6 from the other icosahedron,

leaving 2 holes related to Dirac Fermion Band for Klein Paradox Tunnelling.

6 + 6: For the 1 interior Pd shared with the central icosahedron and with 12 neighbors, 5+1 = 6 of which are in the icosahedron,

6 electrons go 1 to each icosahedron neighbor

and 14-6 = 8 electrons go 2 to a Dirac Fermion Band for Klein Paradox Tunnelling and 6 to the central icosahedron.

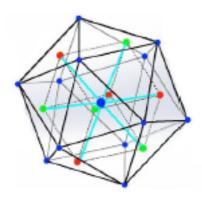
It receives 6+6 = 12 electrons, 1 from each of its 5+1 = 6 icosahedron neighbors and 6 from the central icosahedron,

leaving 2 holes related to Dirac Fermion Band for Klein Paradox Tunnelling.

All 13 Pd atoms in the icosahedron have 18-14 = 4 electrons for TSC condensation guidance.

In TSC Icosahedra of a Pd cluster 4 D (D+D+D+D) form a Schwinger Coherent Quantum State

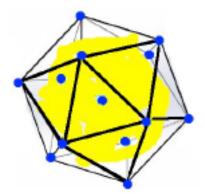
From a classical approximation point of view there are 12+1 = 13 Pd nuclei (blue) within which there is a 2-tetrahedral configuration of 4 D nuclei (red) and 4 D electrons green)



In the Schwinger coherent quantum state (yellow) the 4 D nucei and 4 D electrons are smeared out all over the interior of the icosahedral TSC cell

and

the 4 D electrons screen out the positive charge of the 4 D nuclei making the Schwinger coherent quantum cloud effectively neutral with no Coulomb repulsion or attraction.

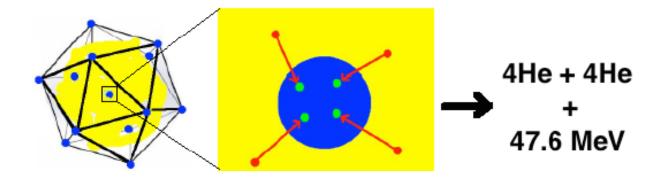


The process of forming the Schwinger State which collapses to the central Pd atom where Deuterium nuclei undergo Cold Fusion is called by Akito Takahashi Tetrahedral Symmetric Condensation (TSC).

The D Schwinger State nuclei go to the central Pd atom and by Klein Paradox Tunnelling 4 D nuclei undergo TSC Cold Fusion producing 4He + 4He + 47.6 MeV

Now look at the central Pd atom in the TSC cell. Its outer electron shell of 18 electrons has 4 free electrons (14 of them being bound to the outer 12 Pd atoms plus 2 forming a Dirac Fermion Band)

which 4 free electrons pull the 4 D nuclei out of the Schwinger quantum cloud into the Central Pd Atom



When the 4 D nuclei get into the small volume of the Central Pd Atom they "see" each other as repulsive like electrical charges resulting in a very high Coulomb barrier between them

but

that is when the Dirac Fermion Band takes effect and gets them to rapidly penetrate the barrier by Klein Paradox Tunnelling (see Appendix for deescription of Klein Paradox Tunnelling)

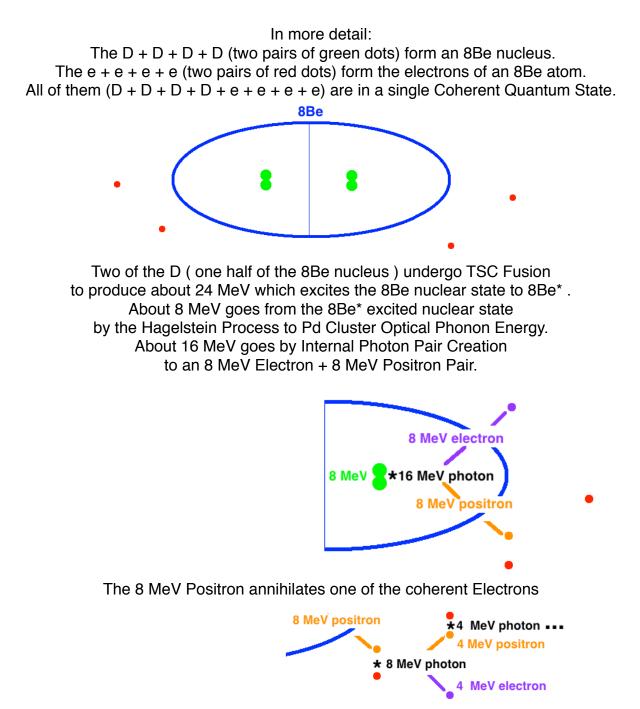
and

then all 4 Deuterium nuclei undergo TSC Fusion to produce energy + 2 Helium nuclei which then pick up the left-over 4 Deuterium electrons to form 2 Helium atoms.

Takahashi said, about his TSC process 4D -> 8Be* -> 4He + 4He + 47.6 Mev: "... Immediately at ... 8Be* formation ...

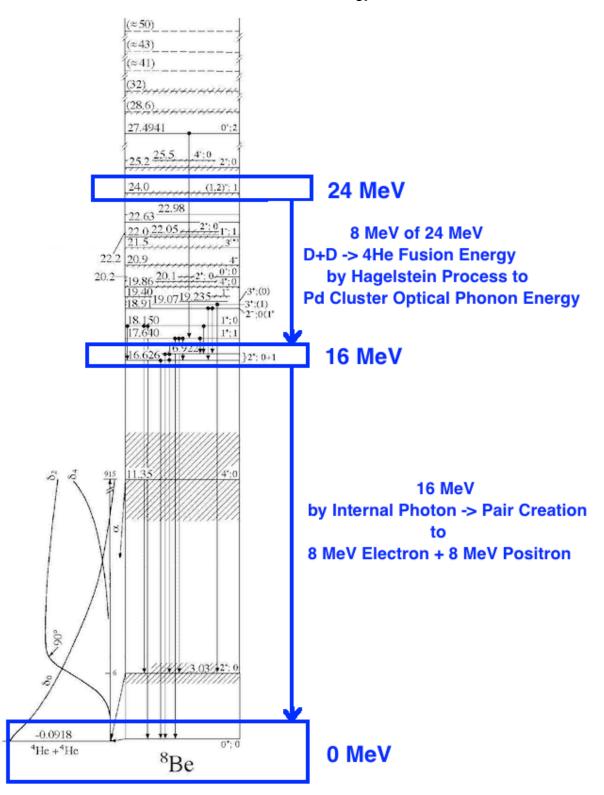
4d-cluster shrinks to much smaller size (about 2.4 fm radius) of 8Be* nucleus, and four electrons should go outside due to the Pauli's repulsion for fermions. Shortly in about few fs or less (note; Lifetime of 8Be at ground state is 0.67 fs), 8Be* will break up into two 4He particles"

plus energy release of 47.6 MeV.



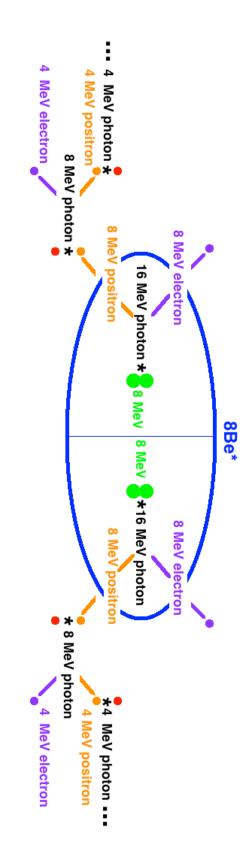
producing an 8 MeV photon which creates a 4 MeV Electron + 4 MeV Positron Pair with the 4 MeV Positron annihilating the other of the two relevant coherent Electrons. Effectively the two zero kinetic energy coherent Electrons (red dots) are replaced by an 8 MeV Electron + a 4 MeV Electron (purple dots) whose 12 MeV kinetic energy becomes vibrational energy of the Pd Cluster. The 16-12 = 4 MeV photon may continue the annihilation to vibrational energy process.

The other half of the 8Be structure will undergo the TSC Fusion energy process in the same way at a slightly different time.



Here is a more detailed 8Be energy level chart:

(image from "Energy Levels of Light Nuclei A = 8" by Tilley, Kelley, Godwin, Millener, Purcell, Sheu, and Weller 2012) The overall process looks like this:



47.6 MeV TSC Cold Fusion energy goes to Pd cluster Optical Phonons

Hagelstein and Chaudhary in ICCF 18 (Misssouri 2013) Poster:

Relativistic Coupling Between Lattice Vibrations and Nuclear Excitation said: "... for relativistic dynamics ... the fundamental theory includes a very strong coupling between the center of mass momentum operator, and internal nuclear transitions. This coupling is connected to changes in the internal structure of a composite when it moves (as a result of the Lorentz transform), compared to the rest frame wavefunction.

Under normal conditions a generalized Foldy-Wouthuysen transformation eliminates this strong coupling, which results in a model in the rotated frame with no residual firstorder interaction. As a result, one would expect generally not expect any significant coupling to survive.

The conditions under which any residual coupling would be expected are the same conditions where the generalized Foldy-Wouthuysen rotation "breaks down" ... in that it becomes very difficult to deal with the loss operator in the rotated picture. Under conditions where the Foldy-Wouthuysen transformation "breaks down" in this sense due to the presence of a strong Brillouin-Wigner loss operator, there exists no useful general nonrelativistic limit. In this case,

the strong coupling between the center of mass momentum and internal nuclear states remains, and can be used for coherent dynamical processes.".

Wikipedia says: "... **Optical phonons** are out-of-phase movements of the atoms in the lattice, one atom moving to the left, and its neighbour to the right. This occurs if the lattice basis consists of two or more atoms. They are called *optical* because in ionic crystals, like sodium chloride, they are excited by infrared radiation. The electric field of the light will move every positive sodium ion in the direction of the field, and every negative chloride ion in the other direction, sending the crystal vibrating. Optical phonons have a non-zero frequency at the Brillouin zone center and show no dispersion near that long wavelength limit. This is because they correspond to a mode of vibration where positive and negative ions at adjacent lattice sites swing against each other, creating a time-varying electrical dipole moment. Optical phonons that interact in this way with light are called *infrared active*. Optical phonons that are *Raman active* can also interact indirectly with light, through Raman scattering. Optical phonons are often abbreviated as LO and TO phonons, for the longitudinal and transverse modes respectively; the splitting between LO and TO frequencies is often described accurately by the Lyddane-Sachs-Teller relation.

When measuring optical phonon energy by experiment, optical phonon frequencies are sometimes given in spectroscopic wavenumber notation, where the symbol ω represents ordinary frequency (not angular frequency), and is expressed in units of cm⁻¹. The value is obtained by dividing the frequency by the speed of light in vacuum. In other words, the frequency in cm⁻¹ units corresponds to the inverse of the wavelength of a photon in vacuum, that has the same frequency as the measured phonon. The cm⁻¹ is a unit of energy used frequently in the dispersion relations of both acoustic and optical phonons ...".

Hagelstein and Chaudhary in Current Science 108 (25 Feb 2015): Low Energy Nuclear Reactions : Phonon Models for Anomalies in Condensed Matter Nuclear Science said:

"... a... new physics model which addresses the fractionation of a large quantum; and a new fundamental Hamiltonian which describes the coupling between vibrations and internal nuclear degrees of freedom ...

the nuclear energy quantum is fractionated into much smaller quanta, which can go into vibrational modes.

For this to work in the model, the vibrational modes first need to be highly excited ...

deuterons are responsible in fractionating the nuclear quanta in operation with excited optical phonon modes, and the deuterons can accomplish this cleanly. However, THz acoustic mode excitation would also be expected to produce fractionation with participation of the host Pd nuclei, which do not fractionate cleanly (leading to disintegration of the Pd nuclei) ...

there is a strong coupling between the vibrational degree of freedom and internal nuclear degrees of freedom implicit in a relativistic model,

but this coupling is normally eliminated by a generalized Foldy–Wouthuysen transformation ...

The fundamental relativistic Hamiltonian under discussion is

$$\hat{H} = \sum_{j} (\mathbf{M}c^{2} + \mathbf{a} \cdot c\hat{\mathbf{P}})_{j} + \sum_{k} \frac{|\hat{\mathbf{p}}_{k}|^{2}}{2m} + \sum_{j < j'} \frac{Z_{j}Z_{j'}e^{2}}{4\pi\varepsilon_{0}|\mathbf{R}_{j'} - \mathbf{R}_{j}|} + \sum_{k < k'} \frac{e^{2}}{4\pi\varepsilon_{0}|\mathbf{r}_{k'} - \mathbf{r}_{k}|} - \sum_{j,k} \frac{Z_{j}e^{2}}{4\pi\varepsilon_{0}|\mathbf{R}_{j} - \mathbf{r}_{k}|}.$$
(5)

If we use a Born-Oppenheimer approximation, then the lattice nuclear problem that remains is

$$\hat{H} = \sum_{j} (\mathbf{M}c^{2} + \mathbf{a} \cdot c\hat{\mathbf{P}})_{j} + \sum_{j < k} \mathcal{V}(|\mathbf{R}_{j} - \mathbf{R}_{k}|) - \frac{i\hbar\hat{\Gamma}(E)}{\hbar},$$
 (6)

where we have augmented the normal Born-Oppenheimer model with a loss term due to coupling with the electrons.

... we have in this a starting place to analyse coherent energy exchange between nuclei and vibrations under conditions of fractionation ...

phonon - nuclear coupling matrix element... in the case of the D2 / 4He transition ... is consistent in magnitude with what is needed to account for the rate at which excess heat is observed in experiments

• • •

Fractionation is easier when fewer oscillator quanta are involved, so we would expect the highest frequency vibrational modes to be involved (THz frequency vibrations). There is only a weak coupling between vibrations and the D2 / 4He transition ...

the D2 / 4He transition occurs with a single phonon exchange with the large nuclear energy quantum transferred to other more strongly coupled transitions and subdivided (many nuclear excitations for a single D2 / 4He de-excitation),

and subsequently fractionated to optical phonons ... excess heat is basically 'silent' (in that there is nothing energetic emitted in the primary reaction) ...

The rate of fractionation without subdivision then has to match the energy release rate. For example, if the system produces excess heat at the 1 W level,

then there are 2.6 x 10^11 reactions/sec and it must take 3.8 x 10^(-12) sec for each of

the large 24 MeV quanta to be fractionated. If the optical phonon mode has an energy of 36 MeV, then the average time associated for the net transfer of a single phonon in connection with fractionation must be 5.7×10^{-21} sec. These numbers are consistent with the models we have studied over the years

If the nuclear system is treated relativistically, there is a very strong coupling present between the vibrational and internal nuclear degrees of freedom ...

there exists a unitary transformation that eliminates this very strong first-order coupling. Under conditions where this unitary transformation is useful, the vibrational and nuclear degrees of freedom are nearly independent ...

when the ... destructive interference ...[of]... the unitary transformation which eliminates the strong first-order coupling ... is spoiled ... there will be a[n]... enhanced rate for coherent energy exchange under conditions of fractionation ...

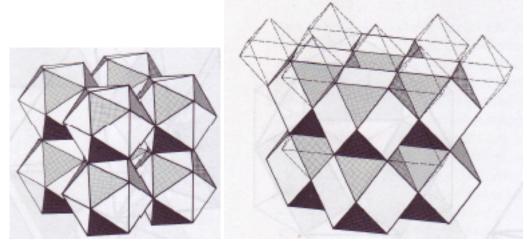
a highly excited vibrational mode ... remove[s]... the destructive interference ...".

Letts in Current Science 108 (25 Feb 2015): Low Energy Nuclear Reactions : Dual Laser Stimulation says: "... PdD lattice vibrations might occur around 8 and 15 THz ...".

 8 - 15 THz Pd-D Fusion Frequency is interestingly coincident with: Critical Temperature of BSCCO superconducting crystals Beck - Mackey Dark Energy Josephson Junction Frequency Energy of Neutrino Masses

Reloading D with Pd cluster Jitterbug from Icosahedron to Cuboctahedron

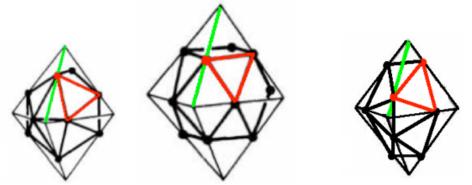
Icosahedra and Cuboctahedra both have 12 vertices so that it is possible to transform them into each other. Buckminster Fuller called that transformation the Jitterbug



(images from Synergetics by Buckminster Fuller (Macmillan 1975, 1982))

To make Cuboctahedra (unit edge length) from Icosahedra (unit edge length) choose 6 pairs of Icosahedra triangle faces (white in the above images) and lengthen the common edge of each pair by a factor of sqrt(2). That expansion flattens each of the triangle pairs to produce 6 square faces of the Cuboctahedron. The other Icosahedral 20 - 2x6 = 8 (shaded) triangle faces are rotated and become the other 14 - 6 = 8 triangle faces of the Cuboctahedron. thus decreasing the number of faces from 20 = 8+(6+6) to 8+6 = 14 while keeping the number of vertices constant at 12.

The triangle faces of the Icosahedron/Cuboctahedron are rotated by a Golden Ratio



(images adapted from Geometrical Frustration by Sadoc and Mosseri (Cambridge 2006)) angle defined by sliding Icosahedron vertices on the edges of a circumscribing Octahedron from points dividing edges into Golden Ratio segments to points dividing edges into two equal segments so that the Octahedron then circumscribes a Cuboctahedron. If the edge lengths of the Icosahedron/Cuboctahedron are kept the same then the Octahedron surrounding the Cuboctahedron will be an expansion of the Octahedron surrounding the Icosahedron.

Just as in the choice of a Cuboctahedron square diagonal to be compressed, there are two ways in which the edge could be divided into Golden Ratio segments, corresponding to the two possible orientations of an Icosahedron. Choice of Golden Ratio segments for one edge forces (by requiring consistency) the choices for all other edges.

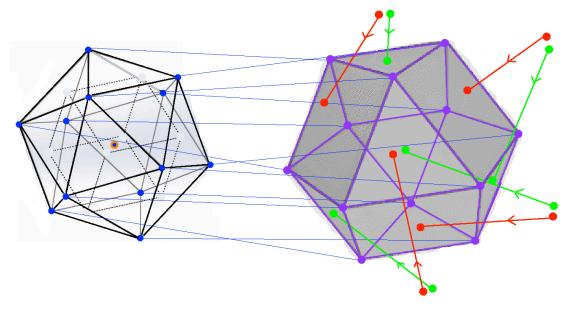
The time scale of such a Jitterbug Transformation of a Pd cluster may be on the order of a picosecond (compare Euro. Phys. J. D. 19 (2002) 333-337 by Pundt et al).

The volume expansion of the Jitterbug Transformation from Icosahedron (unit edge) to Cuboctahedron (unit edge) is:

lcosahedron volume = (5/12) (3 + sqrt(5)) = 2.18169499Cuboctahedron volume = (5/3) sqrt(2) = 2.3570226

Icosahedron/Cuboctahedron volume ratio = 0.9256147947 Cuboctahedron/Icosahedron volume ratio = 1.0803630254

The cuboctahedral configuration resulting from Fusion Energy Jitterbug is not only larger than the Icosahedral configuration, it has 6 large square openings allowing easier entry into the Pd cluster of the Deuterium Nuclei (red dots) and Electrons (green dots) as well as easy exit of the Fused Deuterium 4He + 4He nuclei from the Pd cluster.



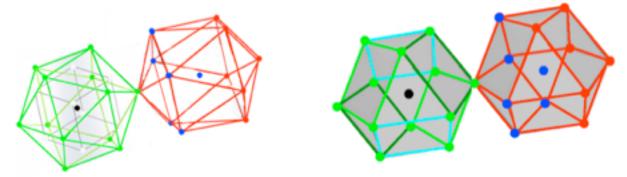
Also, the cuboctahedral configuration has 8 small triangle faces to which the 4 Nuclei and 4 Electrons of the Deuterium are attracted to form the Tetrahedral Symmetric Coherent Quantum State. The size required for Jitterbug / TSC Fusion is a Palladium atomic cluster whose ground state is icosahedral and can easily Jitterbug Transform into a cuboctahedral state and whose size is large enough to contain several TSC Fusion Cluster sites, each of which is an icosahedron that can Jitterbug transform into a cuboctahedron.

The 13-atom Pd/Ni cluster (0.70 nm) is an icosahedron, for 1 TSC Fusion Cluster site.

The 2-shell 55-atom Pd/Ni cluster (1.13 nm) has two icosahedra that share a central vertex, for only TSC Fusion Cluster sites.

Clusters of between 56 and 147 atoms contain from 2 to 13 TSC Fusion Cluster sites by partially filing the 3rd shell of atoms.

The 3-shell 147-atom Pd/Ni cluster (1.56 nm) has 12 exterior TSC Fusion Cluster sites plus 1 central TSC Fusion Cluster sites, so it contains 13 TSC Fusion Cluster sites.



(see viXra 1502.0069)

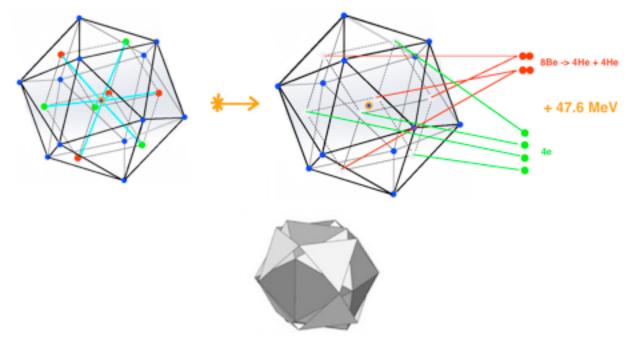
Clusters of between147 and 309 atoms contain at least 13 TSC Fusion Cluster sites The 4-shell 309-atom Pd/Ni cluster is 2.00 nm in size, so it is disfavored with respect to the 3-shell 147-atom cluster for use with Sodium Zeolite Y whose pore size is 0.74 nm expandable to 1.5 nm.

Most of the TSC Fusion Energy is carried to the Pd Cluster Structure by the 4He+4He and the 4e electrons of the TSC coherent quantum state according to the Hagelstein Coupling between Nuclear Excitation and Atomic Structure.

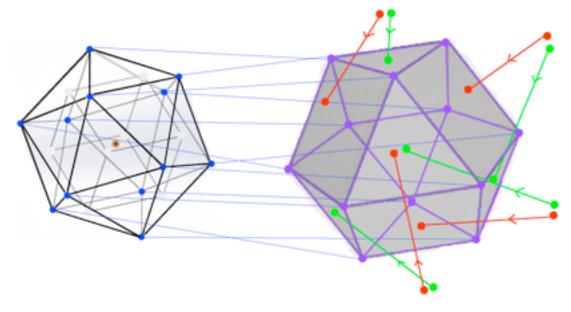
The Pd Structure Energy of Excited Optical Phonon Modes is carried by the Zeolite Cage Electrostatic Field (on the order of 3 V/nm) to be stored in the Zeolite as heat which Heat can be accessed by Zeolite-Water reaction.

Each of the 13 TSC fusion icosahedra is capable of TSC fusion

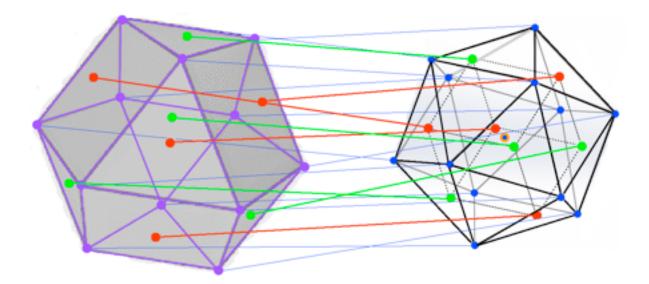
Some of the TSC Fusion Energy goes to a Jitterbug transformation



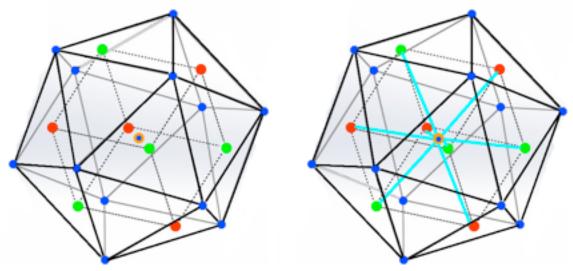
of the icosahedral Palladium, depleted of Deuterium fusion fuel, to a cuboctahedral configuration



which has 6 large square openings through which the 4He TSC Fusion Product Ash can leave the Pd cluster and ambient Deuterium Fuel can enter to reload the Palladium cluster. Replacement is easier for the 12 outer TSC configurations than for the 1 central TSC configuration which is not directly exposed to ambient D gas After entering the Palladium cluster the 4 Deuterium nuclei (red dots) and 4 electrons (green dots) form a Tetrahedral Symmetric Coherent Quantum State centered on the 8 triangular faces of the cuboctahedral configuration. Then, since the icosahedral configuration is the Palladium cluster ground state, another Jitterbug transformation



takes the Palladium cluster to an icosahedral configuration with the replenished Deuterium nuclei and electrons ready for another round of TSC fusion



How much energy does TSC Cold Fusion produce ?

According to Hagelstein's model for fusion energy going to excited optical phonons in the Pd cluster, instead of the "... four electrons ... go[ing] outside ...", the four electrons should remain part of Schwinger's "coherent ... single state" until after fusion when the four electrons and the two 4He nuclei would produce two 4He atoms, with most of the 47.6 MeV going to excited optical phonons in the Pd cluster.

If the Pd Clusters were embedded in Zeolite Cages, heat from the Pd Cluster would be transferred to the Zeolite, from which it could be extracted by the Zeolite-Water process.

A 3-shell 147-atom icosahedral Palladium atomic nanocluster contains 13 TSC Fusion Site Icosahedra and each TSC Fusion event produces 47.6 MeV 47.6 MeV x 13 TSC Sites / 147-atom Pd Cluster x 4.45 x 10^(-17) Watt-Hours / MeV = = 2.754 x 10^(-14) Watt-Hours / 147-atom Pd Cluster for each Jitterbug Cycle

Mass of 147-atom Pd Cluster 147 x 106 x 1.66 x 10⁽⁻²¹⁾ = 2.587 x 10⁽⁻¹⁷⁾ milligrams

SO

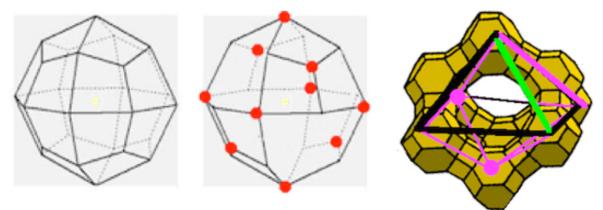
a milligram of 147-atom Pd Clusters gives about 1 KiloWatt-Hour each Cycle.

If 36 seconds = 1/100 hour is taken as the Cycle time then

a TSC-Jitterbug Fusion device with 1 milligram of Palladium in the form of 147-atom Pd clusters with full D-Loading should produce 100 KiloWatt-Hours in an hour.

Zeolite Structure

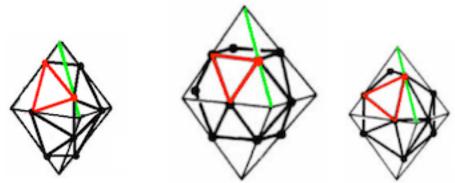
The Zeolite Y Cavity has geometric symmetry related to an isometric trapezohedron = tetragonal trisoctahedron with the 4 holes corresponding to deleting 4 octahedral-type 3-face groups



In the center image, the 10 red dots correspond to the 10 sodalite cages.

In the right image, magenta is used for hidden lines and for the 2 hidden sodalite cages and

the green octahedron edge corresponds to the green edge in these Jitterbug process images

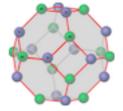


(images adapted from Geometrical Frustration by Sadoc and Mosseri (Cambridge 2006))

The green edge midpoint cuboctahdral vertex is at the widest point of the cavity mouth as expected for the larger cuboctahedron volume and

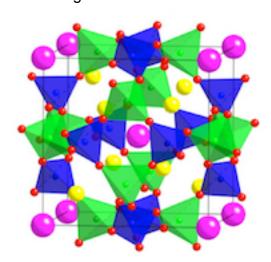
the green edge Golden Ratio point icosahedral vertices are at narrower points of the cavity mouthas expected for the smaller icosahedral volume.

Each sodalite cage is a 24-vertex truncated octahedron as in this image from Wikipedia



A more detailed view of a sodalite cage from

http://som.web.cmu.edu/structures/S099-sodalite.html has red dots for Oxygen and pink spheres for OH and yellow spheres for Sodium and blue tetrahedra for Silicon and green tetrahedra for Aluminum



It shows that of the 24 vertices of the sodalite cage, 12 are Aluminum and 12 are Silicon so each Zeolite Cavity has $10 \times 12 = 120$ Aluminum atoms.

Zeolite Cavities have Electrostatic Fields on the order of 3 V / nm.

R. A. van Santen and D. L. Vogel, in Lattice Dynamics of Zeolites (Advanes in Solid-State Chemistry, Vol. 1 (1989) 151-224), said: "... The vibrational spectrum of a zeolite may be visualized as the sum of three contributions,

the first of which which is given by the zeolite framework, the network formed by SiO4 and AIO4 tetrahedra sharing corners.

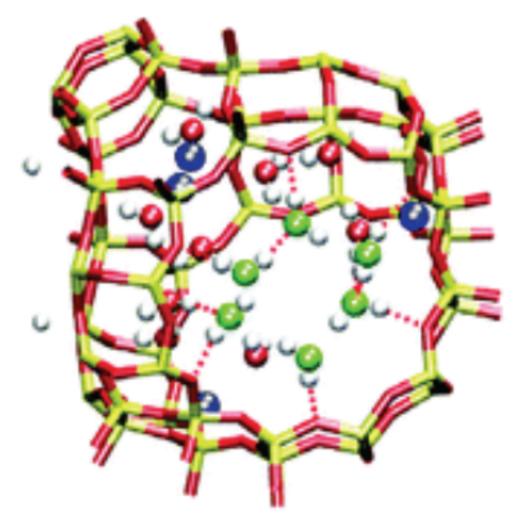
The second contribution originates from the ...[material]... located in the cages and channels formed by the framework ... The [material] vibrate[s] against the framework ...

The third contribution is given by the presence of hydroxyl groups and water molecules. Hydroxyl groups are either located in lattice vacancies, or present as isolated groups bound to the external zeolite surfaces, or internally bridging two tetrahedra. ... Due to the very high oscillator strength of the hydroxyl group, water and hydroxyl groups give rise to strong absorption bands between 3200 cm-1 and 3750 cm-1 (symmetric and antisymmetric stretching modes). ...".

Angela Di Lella, Nicolas Desbiens, Anne Boutin, Isabelle Demachy, Philippe Ungerer, Jean-Pierre Bellat, and Alain H. Fuchs, Phys. Chem. Chem. Phys. 8 (2006) 5396-5406) studied water in Zeolites, saying: "... We report ... Monte Carlo simulations of water



adsorption in [Zeolite] NaY ... faujasite ... The existence of cyclic water hexamers ... located in the 12-ring windows recently disclosed by neutron diffraction ...



... experiments ... were ... observed in the case of NaY ...".

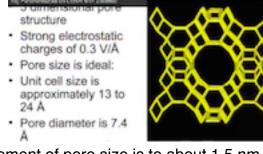
Dmitry Kopelevich and Chia-Yi Chen, in Phonon interactions in zeolites mediated by anharmonicity and adsorbed molecules (Molecular Simulation 2008), said: "... thermal conductivity of nanoporous materials can be significantly affected by adsorption of guest molecules. These molecules serve as moving defects and provide additional scattering centers for heat-carying phonons. ...

we perform molecular dynamics simulations of a model system, namely sodalite zeolite with small molecules ... encapsulated in its cages. We measure effects of sorbates ... such as correlations between different phonon modes and the phonon frequency and lifetime. ... The phonon lifetime often increases upon encapsulation of a sorbate into the zeolite which suggests that the sorbate-phonon interactions are qualitatively different from phonon scattering by point defects fixed in the lattice. ...".

Iraj Parchamazad used Sodium Zeolite Y also known as faujasite. The Wikipedia page for faujasite says:

 "... The faujasite framework consists of sodalite cages which are connected through hexagonal prisms.
 The pores are arranged perpendicular to each other.
 The pore, which is formed by a 12-membered ring, has a relatively large diameter of 7.4 Å [0.74 nm]
 The inner cavity has a diameter of 12 Å [1.2 nm] and is surrounded by 10 sodalite cages. ...".

Ruby Carat and Melvin Miles interviewed Iraj Parchamazad of University of La Verne in 2012. In that video interview Iraj Parchamazad said that the Zeolite cavity size can oscillate and vary, enlarging up to about 2.4 nm.



A corresponding enlargement of pore size is to about 1.5 nm which would permit a 3-shell 147-atom Palladium cluster to enter the Zeolite Cavity.

Iraj Parchamazad did not use Sandia's 1.5 nm Palladium clusters in his Zeolite but

used an organometallic solution containing Palladium atoms.

After putting that into the Zeolite he heated the Zeolite

to burn off Carbon, Hydrogen, and Oxide

leaving a Zeolite and some Palladium.

Then he exposed the Zeolite/Palladium to Deuterium,

and got excess heat 10 out of 10 times, indicating fusion.

I would like to see experiments with Zeolite directly using Sandia 1.5 nm Palladium NanoClusters.

If there is difficulty with getting the Sandia Clusters to fit into the Sodium Zeolite Y then I would like to see experiments with Zeolite ITQ-37

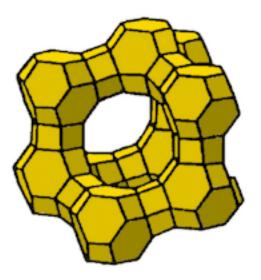
which has pore size about 2 nanometers. (Royal Society of Chemistry, 29 April 2009 and Sun et al, Nature 2009)

Transfer of Energy from Pd Cluster Structure to Zeolite Structure

After TSC Fusion, by Hagelstein's process, the energy is stored in the Pd cluster as excited Optical Phonon modes.

The Pd Structure Energy of Excited Optical Phonon Modes is carried to the Zeolite in which the Pd cluster is caged to be stored as Zeolite heat.

Each Zeolite Y Cavity is surrounded by 10 sodalite cages which are arranged in a 3-dimensional Diamond network as shown in this image from http://www.vurup.sk/sites/vurup.sk/archivedsite/www.vurup.sk/english/products/molek/slovsit1/ english.html



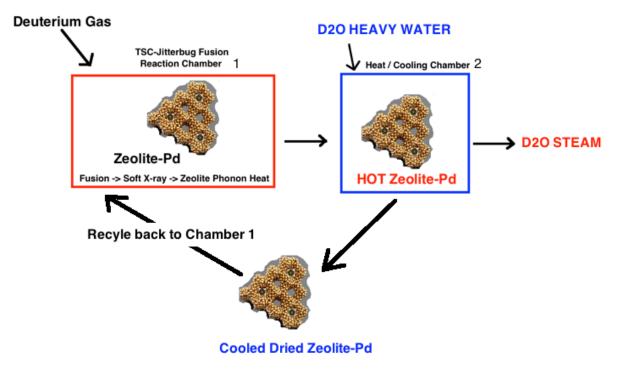
The Pd Structure Energy of Excited Optical Phonon Modes is carried by the Zeolite Cage Electrostatic Field (on the order of 3 V/nm) to be stored in the Zeolite as heat which Heat can be accessed by Zeolite-Water reaction.

Extraction of Cold Fusion Energy from Zeolite Structure

According to a 7 June 2012 techthefuture.com web article by Tessel Renzenbrink: "... Zeolite is a mineral that can store up to four times more heat than water ... zeolite retains a hundred percent of the heat for an unlimited amount of time ... When water comes into contact with zeolite it is bound to its surface by means of a chemical reaction which generates heat. Reversely, when heat is applied the water is removed from the surface, generating large amounts of steam. The transference of heat to the material does not cause its temperature to rise. Instead, the energy is stored as a potential to adsorb water. The ...[German Fraunhofer

Institute]... scientists used these particular properties to turn zeolite into a thermal storage system. They created a storage device and filled it with zeolite pellets. To charge the pellets, they exposed them to heat.

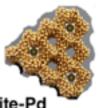
To retrieve the energy they simply added water. ...".



Here is my design for a TSC-Jitterbug Zeolite Pd-D fusion heat engine:

(Zeolite-Pd images adapted from Calvo amd Carre in Nanotechnology 17 (2006) 1292-1299 and from http://gwenbeads.blogspot.com/2014/04/infinite-skew-polyhedron-faujasite-4446.html)

D2O Heavy Water is used to take heat from the Zeolite to make steam so that Hydrogen from H2O does not poison the TSC-Jitterbug process by replacing Deuterium in the Palladium nanoclusters, a possible problem pointed out by Melvin Miles. D20 heavy water from Fisher Scientific costs about \$1,000 per liter for 99.8 atom % D.



Preparation of Zeolite-Pd

Sodium Zeolite Y has unit cell size about 2.5 nanometers which corresponds to the edge-length per cavity of its overall octahedral structure.

According to http://www.google.com/patents/US20040047803

"... Synthesis and stabilization of nanoscale zeolite particles ...

Zeolite Y is of great interest ... Zeolite crystals prepared under conventional synthesis conditions frequently have a mean particle size of between 1 and 5 μ m. ... it would ... be useful if the zeolite particles were sufficiently small to form a colloidal suspension ... Mono- or di-saccharides can be used to keep the crystal size of faujasite (zeolite X and Y) small

... Sucrose, dextrose or other saccharides are added to a conventional aluminium silicate reaction mixture obtained by mixing aqueous alkali metal silicate and alkali metal aluminate solutions at low temperatures, followed by ageing and hydrothermal synthesis. Crystal sizes of between about 30 and 40 nm are claimed ...".

According to Journal of the Taiwan Institute of Chemical Engineers 50 (2015) 259–265 by PankajSharma, Su-JungJeong, Moon-HeeHan, and Churl-HeeCho

"... nanosized NaY zeolite crystals from clear solution using ... (TMAS) ... tetramethylammoniumsilicate ... yields particle of size around 50 nm but in aggregated form ...".

According to a Journal of Catalysis article by Patrick D. Burton, Timothy J. Boyle, and Abhaya K. Datye, "Facile, surfactant-free synthesis of Pd nanoparticles for heterogeneous catalysts"

"... room temperature reduction of Pd(OAc)2 in MeOH is slow enough to produce a suspension of ... metal-phase ... Pd NPs. ...

A Pd-NP/C catalyst was prepared by mixing the carbon support into the suspension of Pd NPs and evaporating the solvent. Aggregate formation was a concern, as there were no capping agents to prevent particle growth. Therefore, the nanoparticles were collected quickly before substantial aggregation could occur. ... this technique is general and can be extended to other powder supports. ...".

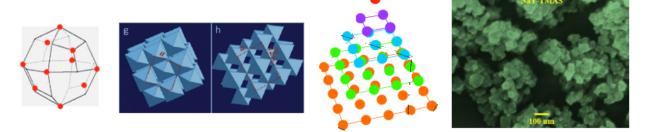
An "other powder support" that would be useful for TSC-Jitterbug fusion energy would be 30-40 nanometer Zeolite Y Crystals in colloidal suspension.

As the Pd nanoclusters "... grow for 20 ... min ..." up to size 1.56 nm for the 147 atom size that is optimal for TSC-Jitterbug fusion,

they are small enough to fit into the Exterior Cavities of the Zeolite Y Crystals (which are have average pore opening 0.74 nm and cavity size 1.2 nm but which sizes can oscillate to be up to about twice those sizes) Due to the open structure of the Zeolite Y Crystals, growth up to the 147 atom size can continue inside the Exterior Cavities of the Zeolite Y Crystals. As soon as the Pd nanoclusters have grown to the 147 atom size the solvent can be evaporated and the powder of 30-40 nm Zeolite Y Crystals loaded with Palladium can be collected and placed in the TSC-Jitterbug Fusion Reaction Chamber for exposure to Deuterium gas and heating the Zeolite Y Crystals by fusion energy.

The Zeolite Y Crystal has octahedral structure

(images from news.chess.cornell.edu/articles/2011/OctahedralNanoparticles.html mathworld.wolfram.com/SquarePyramidalNumber.html Journal of the Taiwan Institute of Chemical Engineers 50 (2015) 259–265)



and each unit cell with 1 Cavity is 2.5 nanometers in diameter so an octahedral Zeolite Y Crystal with diameter 35 nanometers would have an edge length 35 / sqrt(2) = 25 nm = 10 cellsand the octahedron would have 19 square layers:

> layer 1 = 1 external + 0 internal = 1 for total of 1 of which 1 is external layer 2 = 4 external + 0 internal = 4 for total of 5 of which 5 are external layer 3 = 8 external + 1 internal = 9 for total of 14 of which 13 are external layer 4 = 12 external + 4 internal = 16 for total of 30 of which 25 are external layer 5 = 16 external + 9 internal = 25 for total of 55 of which 41 are external layer 6 = 20 external + 16 internal = 36 for total of 91 of which 61 are external layer 7 = 24 external + 25 internal = 49 for total of 140 of which 85 are external layer 8 = 28 external + 36 internal = 64 for total of 204 of which 113 are external layer 9 = 32 external + 49 internal = 81 for total of 285 of which 145 are external layer 10 = 36 external + 64 internal = 100

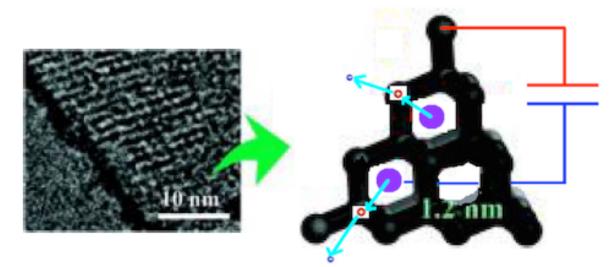
layers 11 through 19 are mirrors of 1 through 9, for a total of 285 with 145 external so an octahedral Zeolite Y Crystal with diameter 35 nm would have 285 + 100 + 285 = 670 cavities with 145 + 64 + 145 = 354 (52.8 %) external and therefore relatively easily accessible to the Pd nanoclusters in the colloidal suspension.

Zeolite Y unit cell atomic mass is (from nptel.ac.in Introduction to Catalysis Lecture 36 Zeolites) (56x23 Na + 56x59 AlO2 + 136x60 SiO2 + 264x18 H2O) = 17,504for actual mass = $17504 \times 1.66 \times 10^{(-21)} = 2.906 \times 10^{(-17)}$ milligrams The atomic mass of a 147-atom Pd nanocluster is 147x106 = 15,582for actual mass = $15,582 \times 1.66 \times 10^{(-21)} = 2.587 \times 10^{(-17)}$ milligrams For 35 nm Zeolite Y Crystals only about 1/2 of their Cavities are External so it may be

optimal to use Zeolite Y Crystal mass = 2 x Palladium mass in the colloid.

Zeolite Heat and Capacitor Electricity

According to a 26 January 2011 PhysOrg.com article by Lisa Zyga: "... The unique 3D array of nanopores in zeolite-templated carbon ...



(image modified to show Zeolite-Templated Carbon framework as Black, Palladium NanoClusters as Purple, Ambient Fluid with Deuterium for TSC-Jitterbug Reloading as White, Excited Optical Phonons from TSC-Jitterbug Fusion as Cyan arrows ionize parts of the ZTC, ejecting electrons (Blue) into the Ambient Fluid and leaving positive ions (Red) in the Zeolite-Templated Carbon thus building up a Capacitance Voltage between the Zeolite-Templated Carbon and the Ambient Fluid)

... enables it to be used as an electrode for high-performance supercapacitors that have a high capacitance and quick charge time ... The zeolite-templated carbon consists of nanopores that are 1.2 nm in diameter ... and that have a very ordered structure ...".

Synthesis of Zeolite-Templated Carbon

is described in the 2013 Caltech Ph.D. Thesis of Nicholas Stadie:

"... Zeolite-templated carbon (ZTC) materials were prepared ... by ... established methods ...

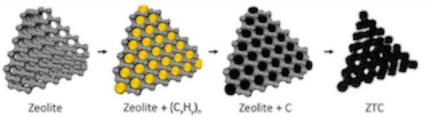


Figure 4.1. A schematic of template-carbonization in a porous zeolite framework, to produce zeolite-templated carbon (ZTC). The ZTC capacitor process converts TSC-Jitterbug fusion energy directly to electricity. Since it does not require the Zeolite-heat-water-steam chemical structure only the Zeolite Y Crystal geometric configuration is needed so all the Zeolite Y can be converted to ZTC carbon configurations attached to a single base carbon substrate that acts as a Capacitor Electrode. (It would be difficult to use separated Zeolite Y Crystals as an electrode.)

However,

the ZTC has fewer Exterior Cavities than the colloidal free-floating Zeolite Y Crystals because

each ZTC structure is attached to the carbon substrate by a base face,

thus eliminating the Exterior Cavities on that base face

so that

for 35 nm ZTC structures only about 1/3 of their Cavities are External (as opposed to about 1/2 for free-floating 35 nm Zeolite Y)

so it may be optimal

for the number of ZTC Cavities to be 3 x the number of Pd 147-atom nanoclusters.

Synthesis of 147-atom Pd clusters and Embedding into Zeolite

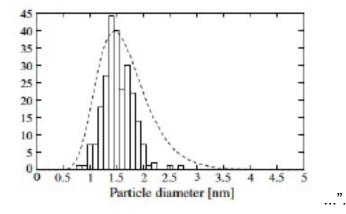
147-atom Pd clusters have diameter about 1.5 nanometers.1.5 nm Pd Clusters have been produced at Sandia National Laboratories

and University of New Mexico Center for Micro-Engineered Materials according to a Journal of Catalysis article

"Facile, surfactant-free synthesis of Pd nanoparticles for heterogeneous catalysts" at

http://www.flintbox.com/public/filedownload/2871/2011-038%20Science%20Direct %20Article

by Patrick D. Burton, Timothy J. Boyle, and Abhaya K. Datye showing



Tim Boyle said in email October 2014:

"

. . .

"... We easily remade the Pd NP just need to get TEM to see what size they are.

If they come out good, we can go ahead and make some for you.

Couple of things.

This is very easy and ya'll may want to do it yourselves

(esp after the next couple of comments).

Simply dissolve Pd-acetate in MeOH and stir for 5 min,

let grow for 20 more and should have your size.

The problem is these will continue to grow and plate out onto the sides of the container, unless you use a substrate.

Would you want these on a substrate, then that'll need to be supplied.

If we make it, we'd have to send it as a solution ...

could you handle this and could you use it?

It won't be a powder, which I think is what you want.

We can dry it down to a powder but not sure what size that will be

or how they'd cluster and how they'd redisperse or in what solvent.

we can try to deposit the materials on a number of surfaces and just let it dry.

Again, not sure how the clustering of these particles will occur.

A gram will take about 2.5 g of Pd(Oac)2 which we have but will need replaced. ...".

Sandia Pd Cluster Recipe

(updated June 2016 based on ideas of Arindom Saha of Quantum Gravity Research)

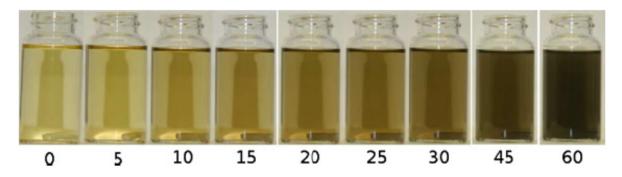
- 1 15 ml of methanol (MeOH) in a scintillation vial
- 2 Add 5 mg palladium acetate (Pd(OAc)2) whose color is red-orange
- 3 Reduce the Pd(OAc)2 by MeOH to Pd atoms

by stirring for 5 minutes with unobstructed exposure to room lighting.

4 - Add 10 mg of Zeolite substrate in colloidal suspension

5 - Place on elevated stir plate and allow to react undisturbed for 20 minutes.

During 20 minutes the Pd atoms form clusters that grow to size 1.5 nm (147 atoms) Initially the Pd atom clusters are very small (only a few atoms) and will migrate into Zeolite cages and continue to grow to size 1.5 nm (147 atoms) at 20 minutes Color of colloidal suspension changes from pale yellow to dark green over the 20 min



6 - At 20 minutes Pd-loaded substrate (and any remnant Pd still in colloidal suspension) are removed and the Pd-loaded substrate dried

7 - Pd-loaded substrate is placed in reaction chamber where it is exposed to Deuterium gas from tank

and

calorimeter measurements are taken to measure any heat that might be produced by TSC-Jitterbug fusion

(analagous to heat produced by Arata and Zhang (replicated by McKubre at SRI) with no external power input - only palladium powder + deuterium gas)

The substrate may be 30-40 nm Zeolite Crystals, such as Sodium Zeolite Y or ITQ-37. At 30-40 nm size each will have about 12 to 16 large Cavities per edge About half of the Cavities will be on the Exterior Surface of the Tetrahedral Crystal where they will be easily accessible by Pd atom clusters in the colloidal suspension

Global Energy and TSC-Jitterbug-Zeolite Fusion machines

Can TSC-Jitterbug-Zeolite Fusion produce Abundant Cheap Energy so that Expensive Competition for geologically concentrated Cheap Oil



will become unnecessary ?

Using total Earth Energy Reserves in Terawatt-years, according to M. Taube, in his book Evolution of Matter and Energy on a Cosmic and Planetary Scale (Springer-Verlag 1985), the number of years that 10^10 people could consume energy at the present USA per capita rate, a consumption rate of about 1,000 Terawatt-years/year, is:

	Reserves	Duration
	(Terawatt-years)	(years)
Oil	850	1
Gas	550	1
Methane	1,500	2
Coal	7,000	7
Uranium	1.9 X 10^9	2,000,000
	(1/1000 of	
	Earth supply)	
Thorium	7.9 x 10^9	8,000,000
	(1/1000 of	
	Earth supply)	
Deuterium	1.9 x 10^9	2,000,000
	(1/1000 of	
	ocean supply)	
Lithium	1.9 x 10^9	2,000,000
	(source of	
	tritium)	

As to solar energy, the total solar energy received by Earth is about 109,000 Terawattyears/year so that 10^10 people could consume energy at the present USA per capita rate by using about 1% (one percent) of the solar energy received by Earth. This could be done, for example, by building a lot of orbiting solar energy collection dishes and beaming the energy to Earth.

The total geothermal heat flux is about 66 Terawatt-years/year, and the total tidal energy is about 3 Terawatt-years/year, so that those sources would be inadequate to support 10^10 people consuming energy at the present USA per capita rate.

For Everybody on Earth to be Happy, the Abundant Cheap Energy must provide a high Standard of Living (current USA standard) for a lot of people (10 billion), and:

last for a long time (more than decades) - rules out Oil, Gas, Methane, and Coal;

have no serious radioactive waste - rules out Uranium, Thorium, and Tritium (Lithium);

have realistically scalable capital cost - rules out Solar which would require Satellite collectors with area 1% of pi x $6,000^2 = 1,000,000 \text{ km}^2 = (1,000 \text{ km})^2$ or cloud-free collectors on Earth surface with the same area. Less than 100% efficiency would require correspondingly larger area of collectors.

That leaves one possible source of Abundant Cheap Energy for 10 billion people:

	Reserves (Terawatt-years)	Duration years)
Deuterium	1.9 x 10^9 (1/1000 of ocean supply)	2,000,000

Since a gram of properly structured Palladium gives TSC-Jitterbug Pd-D Cold Fusion Energy on the scale of Megawatts:

1 milligram of Palladium gives a 1 kiloWatt Machine, useful for "electric motors, tools, machines and heaters" (Wikipedia) Such small energy machines could use the ZTC Electric Capacitor technology.

1 gram of Palladium gives a 1 MegaWatt = 1340 HorsePower Machine, useful for "large electric motors; large warships such as aircraft carriers, cruisers, and submarines; large server farms or data centers; and some scientific research equipment such as supercolliders, and the output pulses of very large lasers. A large residential or commercial building may use several megawatts in electric power and heat. ... railway... electric locomotives ... typically have a peak power output of 5 or 6 MW, although ... Eurostar ... uses more than 12 MW, while heavy diesel-electric locomotives typically produce/use 3 to 5 MW ..." (Wikipedia) C-130 aircraft have 4 engines each with 4300 HorsePower (globalsecurity.org) so would need a 4 x 4300 / 1340 = 13 grams of Pd Such mid-sized energy machines could use, depending on portability and site requirements, either Zeolite Steam or ZTC Electric Capacitor technology. 1 kg of Palladium gives a 1 GigaWatt Machine,

useful for "large power plants ... HVDC converters have been built with power ratings up to 2 GW" (Wikipedia)

Such machines could use either Zeolite Steam or ZTC Electric Capacitor technology, using HVDC converters up to 2 GW to convert the ZTC Electric Capacitor DC into AC.

1,000 kg = 1 ton of Palladium gives 1 TeraWatt. The total power used by Humans in 2006 was 16 TW. The average lightning strike peaks at 1 TW, but lasts only 30 microseconds. Powerful 20th century lasers produce TW, but only for nanoseconds. (Wikipedia)

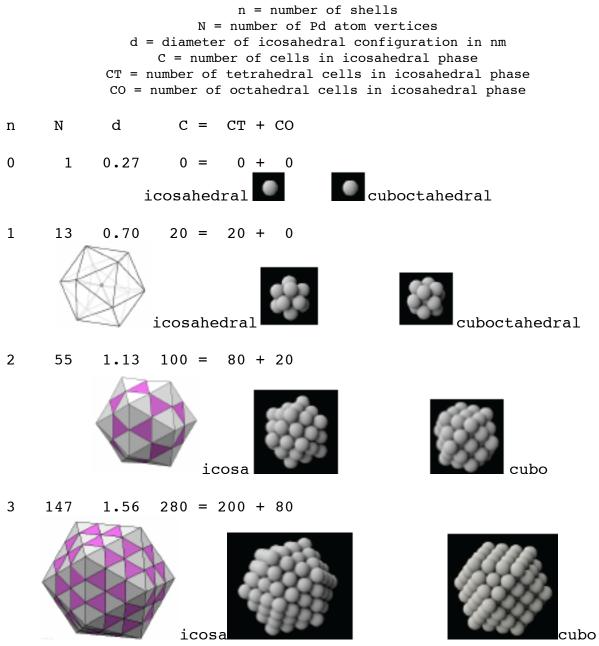
1,000 tons of Palladium gives 1 PetaWatt. The Lawrence Livermore Nova laser has power of 1.25 PW in a 5x10⁽⁻¹³⁾ sec pulse. The total power of sunlight hitting the Earth is about 174 PW. (Wikipedia)

222 tons of Palladium were mined world-wide (based on 2006 and 2007 data, Wikipedia):

Russia produced 98 tons South Africa produced 89 tons Canada produced 13 tons USA produced 11 tons the rest of the world produced 11 tons

Appendix A: Details of Structure of 147-atom Pd clusters

There are two basic structures that are Jitterbug Transforms of each other: **Icosahedral and Cuboctahedral**



(Images from: Polyhedral Clusters by Lord et al; Frank and Kasper in Acta Cryst. 11 (1958) 184-190; Mackay in Acta Cryst. 15 (1962) 1916-1918; vimeo.com/27662398 by Yan Liang (L2XY2) August 2011. Data for n, N, and d from Shtaya-Suleiman dissertation Gottingen 2003.)

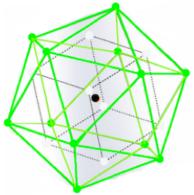
147-atom Icosahedral Geometry

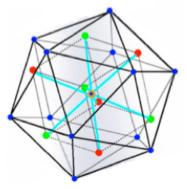
The 147-atom cluster is a central Palladium atom surrounded by 3 layers of Pd atoms:

Layer 1 = central 1 (black) + 12 icosahedral (green) = 13 vertices and 20 tetrahedral cells

It is a single icosahedron configuration that allows TSC fusion

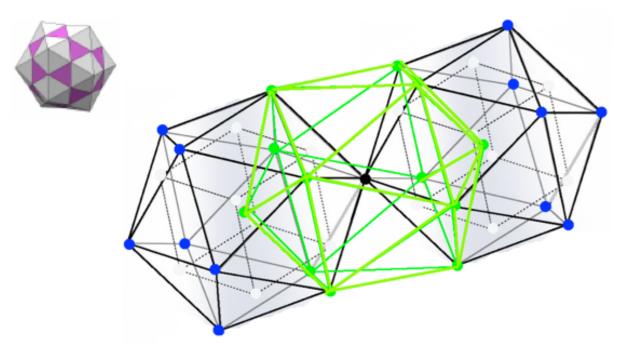
of 4 Deuterium nuclei (red dots) screened by their 4 electrons (green dots) condensing along symmetrical paths (cyan lines) to fusion at the center





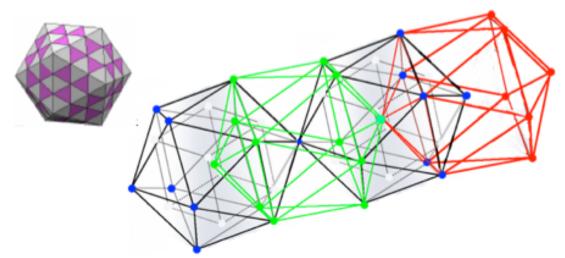
Layer 2 adds 42 vertices (blue) for total of 55

and 60 tetrahedral + 20 cuboctahedral cells for total 80 tetra + 20 cubo = 100

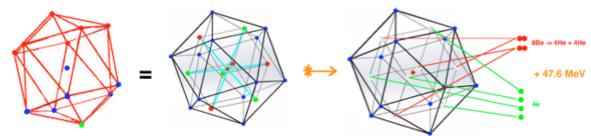


It is a configuration of 2 TSC fusion icosahedra sharing the central vertex with the remaining 55 - (26-1) = 30 vertices in 3 10-vertex bands

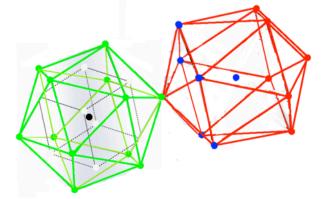
Layer 3 adds 92 vertices (red) for total of 147 and 120 tetrahedral + 60 cuboctahedral cells for total 200 tetra + 80 cubo = 280



It is a configuration of 12 TSC fusion icosahedra

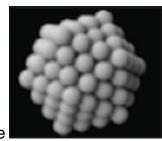


each of which shares a vertex with one of the 12 vertices of the Layer 1 icosahedron.



so that the entire 3-layer 147-atom configuration has 13 TSC fusion icosahedra: 12 outer icosahedra and 1 central icosahedron. The 13 TSC configurations have 13x13 = 169 vertices but 24 vertices are shared between an outer and the central TSC and 5x12 = 60 vertices are shared between two outer TSC so 169 - 24/2 - 60/2 = 127 of the 147 vertices are in the 13 TSC The remaining 147 - 127 = 20 vertices outside the 13 TSC are at the centers of the triangle faces of the entire 147-atom icosahedron.

147-atom Cuboctahedral Geometry

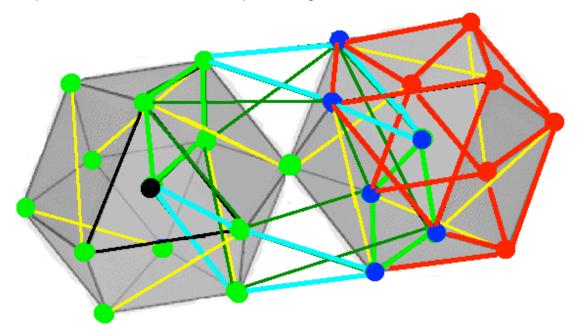




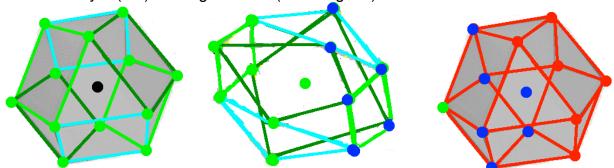
The 147-atom 3-layer icosa structure

goes to

a 3-layer cuboctahedral structure by Jitterbug transformation of all 147 atoms.



Like the icosa case, in the cubo case there is a central (black) vertex surrounded by 12 (green) cubo-configured vertices and a second layer (blue) forming an intermediate (distorted) cuboctahedron and a third layer (red) forming an outer (more regular) cuboctahedron.



In the cubo case, there are also 12 outer TSC Jitterbug cuboctahedra plus a single central TSC Jitterbug cuboctahedron, so Jitterbug transformation of the entire 147-atom Pd cluster works consistently with individual JItterbug transformations of the 13 TSC icosahedra and TSC Jitterbug cuboctahedra.

How do the Icosahedral Clusters grow to 147 atoms ?

Eric A. Lord, Alan L. Mackay, and S. Ranganathan say in

"New Geometries for New Materials" (Cambridge 2006):

"... The Mackay icosahedron is obtained by packing tetrahedra and octahedra around an icosahedron [12 vertices +1 center = 13 vertices]...

if an octahedron is placed on every face of an icosahedron, the angular gap between neighboring octahedra can be closed by a very small deformation, to bring them into face contact $[12 + 20 \times (6-3)/2 = 42 \text{ vertices}]$...



... The concave regions of the resulting polyhedron can be filled by five-rings of tetrahedra [42 + 12 + 1 center = 55 vertices]...



... The [55]-atom Mackay cluster ... [triangles: dark = octahedra; light = tetrahedra]... The process can be continued ... [with octahedra on each of the 12x5 = 60 outer cell faces of 5-rings thus adding $60 \times (2/2 + 1/3) = 80$ vertices and creating 2 TSC Fusion structures sharing a central vertex.

This also creates concave places for 30 pairs of tetrahedra adding no vertices plus 12 tetra-5-rings adding 12 vertices for a total of 54+80+12 + 1 center = 147.



147-atom cluster

has 12+1 = 13 TSC Fusion sites]...".

Lord et al use 12, 54, and 146 atoms for Mackay clusters while Liang uses 13, 55, and 147 atoms. The difference is whether or not the center vertex is counted, that is, not so much a real physical difference but a difference in math convention.

How many D atoms can live in a 147-atom Pd cluster ?

F. Calvo and A. Carre say in Nanotechnology 17 (2006) 1292–1299 "Structural transitions and stabilization of palladium nanoparticles upon hydrogenation": "... Cuboctahedra ...[and]... icosahedra ... contain exactly the same number of atoms. ... In the case of ... the 147-atom Pd cluster ... the favoured structure in the pure metal is the three-layer icosahedron.

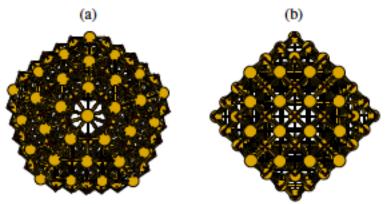


Figure 1. Palladium clusters fully loaded with hydrogen. (a) Pd₁₄₇H₂₀₀, I_h symmetry; (b) Pd₁₄₇H₁₆₄, O_h symmetry.

Since the minimum full load for Icosa or Cubocta Pd/Ni 147-atom clusters is 164 D/H atoms, no more than 3 cycles of full TSC fusion (each consuming 56 D/H nuclei) can occur without replenishment of D/H from the surroundings of the clusters (such as immersion of the clusters in D/H gas).

How long does it take Deuterium to load into Palladium ?

Wang, Hara, and Watanabe in Materials Transactions, Vol. 48, No. 3 (2007) pp. 560 to 565 say: "... Pure Pd, Pd-4 at%Pt and Pd-8 at%Pt ... powders smaller than 200 mesh (<74 mm) were prepared ... hydrogen absorption ...[by Pd-4 at%Pt]... was extremely fast and attained to equilibrium within tens of seconds. Hydrogen absorption by Pd and Pd-8 at%Pt was also very fast ...".

Tens of seconds is much longer than the times for TSC Fusion and for Jitterbug so it determines the time duration of one TSC-Jitterbug Fusion Cycle and

for the purpose of rough calculations it seems reasonable to take

36 seconds = 1/100 hour = time duration of one TSC-Jitterbug Fusion Cycle.

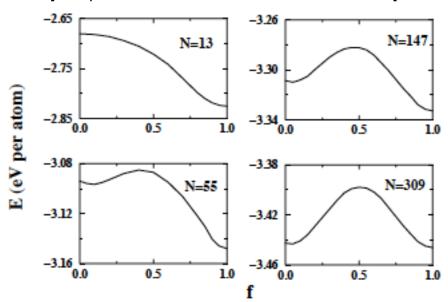
This time is much shorter than the usual loading time for old-type Cold Fusion experiments using Palladium rods, discs, much-larger-than 1.5 nm powder, etc because there are only 3 layers of Pd atoms in 1.5 nm 147-atom Pd clusters.

What about more than 147 atoms ?

As more layers are added, the deformations of tetrahedra and octahedra accumulate and eventually destabilize the structures necessary for Jitterbug and TSC Fusion. The next Mackay cluster beyond 147 atoms has 147+162 = 309 atoms.

Barretau, Desjonqueres, and Spanjaard in Eur. Phys. J. D. 11 (2000) 395-402 say: "... the icosahedron is the preferred structure at small sizes, and the critical size at which the relative stability becomes favorable to cuboctahedrons is N = 561 for PdN clusters ...[for which]... For N = 13 the cuboctahedron is ... unstable.

For N = 55, 147, and 309 atoms the cuboctahedron is metastable and slightly distorted. Its transformation to a perfect icosahedral structure needs an activation energy of 12 meV for N = 55, 28 meV for N = 147 and 45 meV for N = 309. The activation energies involved in the inverse transformation are 61 meV for N = 55, 51 meV for N = 147 and 48 meV for N = 309. ...[compare 47.6 MeV for each TSC Fusion event]...



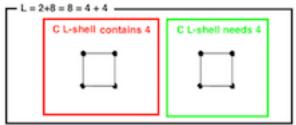
... The evolution of the potential energy profile of homogeneously relaxed ... PdN clusters during the Mackay [Jitterbug] transformation for increasing values of N. f is a fraction of the displacements ... f = 0 and 1 correspond to the ... cuboctahedron and icosahedron, respectively ...".

N = 309 is disfavored for TSC-Jitterbug Fusion with respect to N = 147 for two reasons: energy levels are too close for rapid Jitterbug cubocta to icosa transition N = 309 Pd Cluster is too large (2 nm) to fit through 1.5 nm expanded Sodium Zeolite Y pore so

147 atoms is optimal for Pd cluster Cold Fusion

Appendix B: Graphene and Klein Paradox Quantum Tunnelling

Consider the outer shell (L-shell) of Carbon:



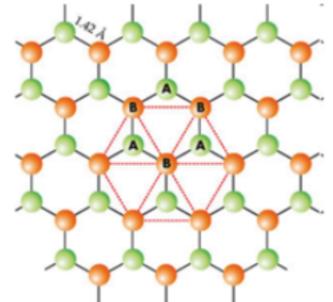
The useful chemistry of Carbon (graphite, diamond, buckyballs, graphene, organics) is due to the fact that

each Carbon atom has the 4 L-shell electrons that every other Carbon atom needs. If each Carbon atom is connected to 4 other Carbon atoms

then the result is a 3-dim Diamond Packing with Tetrahedron Vertex Figure.

However, Diamond is only a metastable state. Graphene is a stable state.

P. B. Allen and B. K. Nicolic, in University of Delaware PHYS 824: Introduction to Nanophysics - Electronic band structure of graphene, said: "... Band structure of graphene ... originates from orbital hosting the fourth valence electron. The bands which correspond to the dispersion of bonding and antibonding molecular orbital (constructed from orbitals on two carbon atoms) are called pi and pi* bands ...



The honeycomb lattice of graphene ... is not a Bravais lattice. Instead, it can be viewed as bipartite lattice composed of two interpenetrating triangular sublattices ...

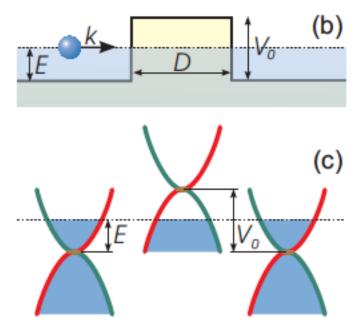
the single-particle electron states are ... two classes, called sigma and pi.

The even sigma states are derived from carbon s and px , py orbitals (i.e., their hybridized sp2 orbitals ...),

while **the odd pi states are derived from carbon pz orbitals** ... electron and hole states in graphene should be interconnected, exhibiting properties analogous to the

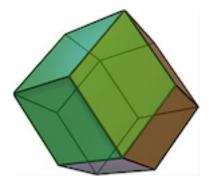
charge-conjugation symmetry in quantum electrodynamics ... because graphene lowenergy quasiparticles have to be described by two-component wave functions ... which are needed to define the relative contributions of the A and B sublattices in the quasiparticles make-up. The two-component description for graphene is very similar to the [Dirac Equation] spinor wave functions in QED...".

I. Katsnelson, K. S. Novoselov & A. K. Geim, in Chiral tunnelling and the Klein paradox in graphene (arXiv cond-mat/0604323), said: The ... Klein paradox - unimpeded penetration of relativistic particles through high and wide potential barriers - ... can be tested ... using electrostatic barriers in single- and bi-layer graphene. Due to the chiral nature of their quasiparticles, quantum tunnelling ... becomes ... qualitatively different from ... normal, non-relativistic electrons. ...



... Tunnelling through a potential barrier in graphene: ... (b) ... diagrams ... show the positions of the Fermi energy E across such a barrier. The Fermi level (dotted lines) lies in the conduction band outside the barrier and the valence band inside it. The blue filled areas indicate occupied states. The pseudospin ... is parallel (antiparallel) to the direction of motion of electrons (holes), which also ... keeps a fixed direction along the red and green branches of the electronic spectrum. (c) - Low-energy spectrum for quasiparticles in bilayer graphene. The spectrum is isotropic and, despite its parabolicity, also originates from the intersection of energy bands formed by equivalent sublattices, which ensures charge conjugation, similar to ... single-layer graphene. ... charge carriers in bilayer graphene ... are massive quasiparticles with a finite density of states at zero energy, similar to conventional nonrelativistic electrons. On the other hand, these quasiparticles are also chiral and described by spinor wavefunctions, similar to relativistic particles or quasiparticles in single-layer graphene ... the origin of the unusual energy spectrum can be traced to the crystal lattice of bilayer graphene with four equivalent sublattices. ... the relevant QED-like effects appear to be more pronounced in bilayer graphene ...".

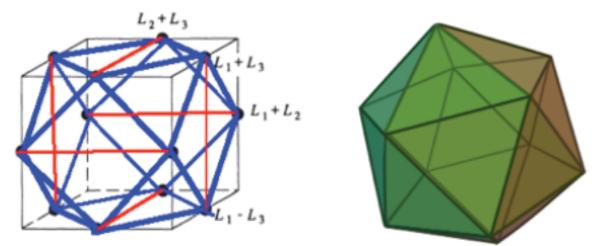
If each Palladium atom were to be connected to 14 other Palladium atoms then the result would be a 3-dim FCC Lattice with Rhombic Dodecahedron Vertex Figure



However, it may be that the Rhombic Dodecahedron FCC Lattice is only metastable

and

more stable state may be based on its dual, the Cuboctahedron



which can transform by Jitterbug Transformation into an Icosahedron.

Just as Graphene directly uses 3 of the 4 Carbon electrons

the Cuboctahedron / Icosahedron directly uses 12 of the 14 Palladium electrons.

Just as the 4th Carbon valence electron in Bilayer Graphene produces a Dirac Fermion band with Klein Paradox Tunneling through Potential Barriers the 14 - 12 = 2 Palladium valence electrons produce a Dirac Fermion band which, using Klein Paradox Tunneling through Potential Barriers, enable TSC Fusion of Deuterium in Palladium Cluster structures.

Frank Dodd Tony Smith Jr

[74] <u>viXra:1705.0271</u>

Should Consensus Suppress the Individual ?

[73] <u>viXra:1702.0058</u>

Physical Interpretation of the 30 8-Simplexes in the E8 240-Polytope

[72] <u>viXra:1701.0496</u>

From E8 Root Vector Geometry to the LHC

[71] <u>viXra:1701.0495</u>

<u>E8 Root Vector Geometry - AQFT - 26D String Theory - Schwinger Sources -</u> <u>Quantum Consciousness</u>

[70] <u>viXra:1611.0087</u>

Ramon Llull's Art and Structure of Nature

[69] <u>viXra:1610.0318</u>

LHC 2016 Sees 3 Higgs Mass States

[68] <u>viXra:1605.0084</u>

Dark Energy Warp Drive

[67] <u>viXra:1603.0119</u>

Dark Energy and 16 BSCCO Josephson Junction edges

[66] <u>viXra:1603.0098</u>

Cold Fusion - Deuterium in 147-atom Pd nanoclusters embedded in Zeolite cages

[65] <u>viXra:1602.0319</u>

E8 Root Vectors and Geometry of E8 Physics

[64] <u>viXra:1602.0056</u>

E8 AQFT and Sarfatti-Bohm Free Will

[63] <u>viXra:1601.0177</u>

DNA-RNA and Cl(16) Clifford Algebra of E8 Physics

[62] <u>viXra:1512.0300</u>

World-Line String Bohm Quantum Potential and Consciousness

[61] <u>viXra:1511.0098</u>

Connes NCG Physics and E8

[60] <u>viXra:1511.0041</u>

T-quark Widths for 3 Mass States

[59] <u>viXra:1510.0369</u>

Ifa Owari Adinkra Clifford (Giza) Llull Lukasa Origins of E8 Cl(16) Physics

[58] <u>viXra:1509.0199</u>

Klein Paradox Tunnelling and TSC Fusion of D in Pd Nano-Clusters

[57] <u>viXra:1508.0157</u>

LHC 2015-16 and E8 Physics

[56] <u>viXra:1508.0065</u>

E8 Root Vectors - Physical Interpretation

[55] <u>viXra:1507.0173</u>

Fock - Hua - Wolf - Schwinger - Wyler Quantum Theory

[54] <u>viXra:1507.0069</u>

E8 Cosets and 4+4 Kaluza-Klein Lagrangian

[53] <u>viXra:1505.0188</u>

Bell-Christian - S7 - Brown SL(8,R) - E8 - Bohm

[52] <u>viXra:1505.0008</u>

Icosahedral Islands in Pd Film for TSC Jitterbug Fusion

[51] <u>viXra:1504.0046</u>

Palladium in Methanol as Realization of Icosahedral Colloidal QuasiCrystal

[50] <u>viXra:1502.0248</u>

Schwinger Pd-D Zeolite Quantum Fusion Process

[49] <u>viXra:1502.0096</u>

TSC Pd-D Fusion and Zeolite-Heat-Water

[48] <u>viXra:1502.0069</u>

TSC Pd-D Fusion, Effective Electron Mass, Muon Fusion

[47] <u>viXra:1501.0234</u>

TSC Jitterbug Fusion of D in Pd NanoClusters

[46] <u>viXra:1501.0078</u>

Standard Model and Gravity from Tetrahedra

[45] <u>viXra:1405.0030</u>

Cl(16) - E8 Lagrangian - AQFT

[44] <u>viXra:1404.0057</u>

SuperNova Precession Period of Peace

[43] <u>viXra:1403.0300</u>

B-mode Octonionic Inflation of E8 Physics

[42] <u>viXra:1403.0178</u>

Cosmos 2014 Bruno Llull E8 Physics

[41] <u>viXra:1403.0035</u>

Deep State USA/UK

[40] <u>viXra:1402.0178</u>

Unimodular SL(n,R) Gravity and E8 Physics

[39] <u>viXra:1402.0150</u>

Minimal Math Structures Needed for E8 Physics

[38] <u>viXra:1401.0070</u>

Exotic R4 and E8 Physics

[37] <u>viXra:1312.0088</u>

Spinor Doubling and Evolution of Our Universe

[36] <u>viXra:1312.0036</u>

Outline of E8 Physics

[35] <u>viXra:1311.0094</u>

Tony Smith's Web Book 2013

[34] <u>viXra:1311.0088</u>

Schwinger - Hua - Wyler

[33] <u>viXra:1310.0182</u>

E8 Physics 2013

[32] <u>viXra:1309.0096</u>

Can LHC 2016 Data Answer the Question: is Our Universe Metastable ?

[31] <u>viXra:1308.0064</u>

26D Strings, Bohmions, and Quantum Consciousness

[30] <u>viXra:1307.0047</u>

Skunk Works Cusp Fusion Rocket

[29] <u>viXra:1305.0060</u>

<u>Vedic Meru and Nile Pyramid: African IFA to RigVeda-Pachisi to Tarot to Llull to</u> <u>Cartan-Dirac-Riesz-E8Physics</u>

[28] <u>viXra:1304.0071</u>

Introduction to Real Clifford Algebras: Cl(8) to E8 to Hyperfinite II1

[27] <u>viXra:1303.0166</u>

Beyond Higgs: Physics of the Massless Phase

[26] <u>viXra:1301.0150</u>

E8 Physics and 3D QuasiCrystals

[25] <u>viXra:1212.0083</u>

Has Fermi LAT seen the Higgs ?

[24] <u>viXra:1212.0046</u>

<u>3 Fermion Generations from E8 Physics Conformal Gravity/Higgs Sector</u></u>

[23] <u>viXra:1211.0137</u>

<u>Spinors to World-Line Strings to Kerr-Newman Fermions to Schwinger Sources to</u> <u>Wyler/Hua Geometry</u>

[22] <u>viXra:1210.0072</u>

E8 Physics Model and 26D String Theory with Monster Group Symmetry

[21] <u>viXra:1209.0109</u>

Tetrahedra, Dark Energy, and Cold Fusion

[20] <u>viXra:1209.0007</u>

Pd/Ni Clusters for D/H TSC Jitterbug Fusion

[19] <u>viXra:1208.0145</u>

F4 and E8: Wrong Assumption: E8 Cannot Unify Fermions and Bosons. Useful Truth: F4 and E8 Lie Algebras Have Both Commutator and Anticommutator Structure.

[18] <u>viXra:1207.0028</u>

<u>126 GeV Standard Model Higgs</u>

[17] <u>viXra:1204.0078</u>

E8QC - Quantum Contraction Building Block of Our Universe

[16] <u>viXra:1203.0027</u>

LHC 2012 Beyond Moriond: Hunt for Multi-Higgs

[15] <u>viXra:1202.0028</u>

The Third Grothendieck Universe: Clifford Algebra Cl(16) E8 AQFT

[14] <u>viXra:1112.0072</u>

Moriond 2012 Theory Proposal: 3-Mass-State SM Higgs Preserves Consistency up to Planck Scale

[13] <u>viXra:1112.0035</u>

LHC Higgs: 145 Gev or 126 Gev ?

[12] <u>viXra:1110.0015</u>

<u>Great Pumpkin and Golden Channel Higgs: 3 Higgs States Consistent with</u> <u>Electroweak Gfitter</u>

[11] <u>viXra:1109.0037</u>

Higgs as Primitive Idempotents

[10] <u>viXra:1108.0031</u>

Golden Channel Higgs from 2/fb at LHC: 3 Higgs States Consistent with Electroweak

<u>Gfitter</u>

[9] <u>viXra:1108.0027</u>

Introduction to E8 Physics

[8] <u>viXra:1107.0048</u>

Higgs 2011: Will LEE Hide the Higgs ?

[7] <u>viXra:1107.0044</u>

EPS HEP 2011 and E8 Physics

[6] <u>viXra:1106.0042</u>

<u>3-State Higgs-Tquark System</u>

[5] <u>viXra:0909.0062</u>

The True Lost Symbol of our Conscious Cl(8)^8 Universe

[4] <u>viXra:0909.0014</u>

Conformal Kepler Solar System, Pioneer and 55 Cancri

[3] <u>viXra:0907.0040</u>

From Ancient Africa

[2] <u>viXra:0907.0007</u>

The Math of Hua Luogeng - Another Game in Town

[1] <u>viXra:0907.0006</u>

Physics of E8 and Cl(16) = Cl(8)xCl(8)

My Favorite Princeton '63 Texbook: Nickerson, Spencer, Steenrod

Condensate Structure of Higgs and Spacetime

Frank Dodd (Tony) Smith, Jr. - 2017

"... The Nambu Jona-Lasinio model ...

is a theory of Dirac particles with a local 4-fermion interaction and, as such, it belongs to the same class of effective theories as the BCS theory of superconducting metals ... the Nambu Jona-Lasinio model has very recently been applied to the standard model. In this application the Higgs meson is a ttbar top quark mass excitation ...".

(from Nambu Jona-Lasinio Models Applied to Dense Hadronic Matter, by Georges Ripka, in a Workshop on Nuclear Physics, Iguazu Falls, 28 Aug - 1 Sep 1989)

As to the Higgs in the E8 physics model (viXra 1602.0319), consider a generalized Nambu Jona-Lasinio model in which the Higgs is a Fermion-AntiFermion condensate. As the most massive fermion, the Truth Quark - AntiQuark pairs would be so dominant that the Higgs could be effectively considered as a condensate of Truth Quark - Truth AntiQuark pairs but the detailed picture would be as a condensate of Fermion - Anti-Fermion pairs where there are 24 types of Fermions, each Quark coming in color R, G, or B:

> E-Neutrino and Electron Down Quark (R, G, B) and Up Quark (R, G, B) M-Neutrino and Muon Strange Quark (R, G, B) and Charm Quark (R, G, B) T-Neutrino and Tauon Beauty Quark (R, G, B) and Truth Quark (R, G, B)

so that there are $24 \times 24 = 576$ Fermion-AntiFermion pairs for each Higgs and each Higgs can be in Bohm Quantum Resonance with 24×24 Bohm Quantum String states: dilaton; antisymmetric Planck-cell group; and symmetric Bohm Quantum Potential.

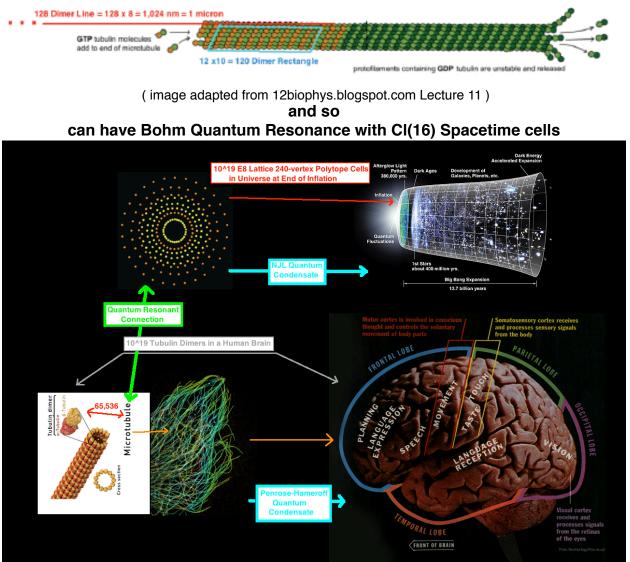
As to Spacetime in the E8 physics model (viXra 1602.0319), consider a generalized Nambu Jona-Lasinio model in which 8-dim Classical Lagrangian Spacetime is a condensate of Geoffrey Dixon's 64-dim Particle spinor T = RxCxHxO = Real x Complex x Quaternion x Octonion and its corresponding 64-dim AntiParticle spinor Tbar. The T - Tbar pairs of the condensate form the 128-dim part of E8 that lives in the Cl(16) Real Clifford Algebra as

248-dim E8 = 120-dim bivector D8 + 128-dim half-spinor D8

By Triality, the D8 / D4xD4 = 64-dim part of E8 representing Spacetime is equivalent to T and Tbar, with T representing Fermions and Tbar representing AntiFermions.

Each cell of E8 Classical Lagrangian Spacetime corresponds to 65,536-dim Cl(16) which contains 248-dim E8 = 120-dim D8 bivectors +128-dim D8 half-spinors

Human Brain Microtubules 40 microns long have 65,536 Tubulin Dimers



(image from Wikipedia and Time)

so that at any and all Times the State of Consciousness of a Human is in exact resonant correspondence with a subset of the cells of E8 Classical Lagrangian Spacetime

Therefore

E8 Classical Lagrangian Spacetime NJL Condensate is effectively the **Spirit World** in which the **Human States of Consciousness = Souls exist.**

After the death of the Human Physical Body the Spirit World interactions with its Soul are no longer constrained by Physical World interactions with its Body so that the Spirit World can harmonize the individual Soul with the collective Universal Soul by the process of Gehinnom whereby the Soul is prepared for Gan Eden.

Humans (NJL Higgs Mass) have Resonant Interaction with Spirits (NJL E8 Spacetime) through Bohmions of Bohm Quantum Potential

E8-Cl(16) Physics (viXra 1602.0319) gives a realistic model of the workings of psychic / spritual / shamanistic phenomena based on resonant connections between

1 - the Planck scale unit cell of E8-Cl(16) Quantum Spacetime has 65,536 elements - each is a binary Creation / Annihilation state of the 2^16-dim Cl(16) Clifford Algebra - the 248-dim E8 part has Creation / Annihilation generalized Heisenberg Algebra = H92 + A7 with graded structure 28 + 64 + (63+1) + 64 + 28

2 - the number of tubulin dimers in a human maximal 40-micron microtubule is 65,536 - each dimer is a binary Superposition Separation state

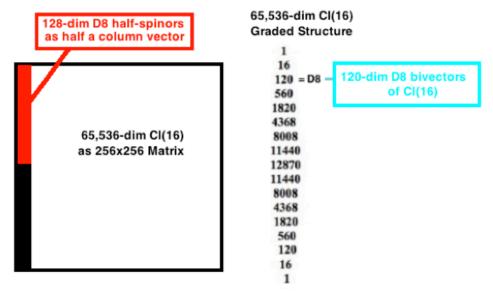


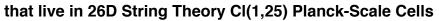
(images adapted from nonlocal.com/hbar/microtubules.html by Rhett Savage) Conformation Electrons Similarly Aligned (left image) - State 0 Conformation Electrons Maximally Separated (right image) - State 1

3 - 2^65,536 (also calculated by Ray) is the VERY LARGE number in the Clifford Algebra sequence: Start with nothing = Empty Set and form its Clifford Algebra: Cl(Empty Set) = 0-dim Then form the Clifford Algebra of that and continue: Cl(0) = 1-dim Cl(1) = 2-dim Cl(2) = 4-dim Cl(4) = 16-dim Cl(4) = 16-dim Cl(16) = 65,536-dim = MUCH larger than the number of particles in Universe.

How do the CI(16) Creation/Annihilation states Resonate with the Dimer Superposition Separation States ?

Resonance between CI(16) Creation/Annihilation states





and

Dimer Superposition Separation States



that live in Human Cells such as Brain Neurons

is based on Quanta of the Bohm Quantum Potential Bohm Quantum Potential is based on World-Lines = Strings and 26-dim String Theory Green, Schwartz, and Witten say in their book "Superstring Theory" vol. 1 (Cambridge 1986) "... For the ... closed ... bosonic string [26D String Theory that is NOT supersymmetric] The first excited level ... consists of ... the ground state ... tachyon ... and ... a scalar ... 'dilaton' ... and ... SO(24) ... little group of a ...[26-dim]... massless particle ... and ... a ... massless ... spin two state ...".

Closed string tachyons localized at orbifolds of fermions produce virtual clouds of particles / antiparticles that dress fermions.

Dilatons are Goldstone bosons of spontaneously broken scale invariance that (analagous to Higgs) go from mediating a long-range scalar gravity-type force to the nonlocality of the Bohm-Sarfatti Quantum Potential.

The SO(24) little group is related to the Monster automorphism group that is the symmetry of each cell of Planck-scale local lattice structure.

The massless spin 2 state = Bohmion = Carrier of the Bohm Force of the Bohm Quantum Potential.

Dimer Superposition Separation States

Consider the Superposition of States State 0 and State 1 involving one Tubulin Dimer

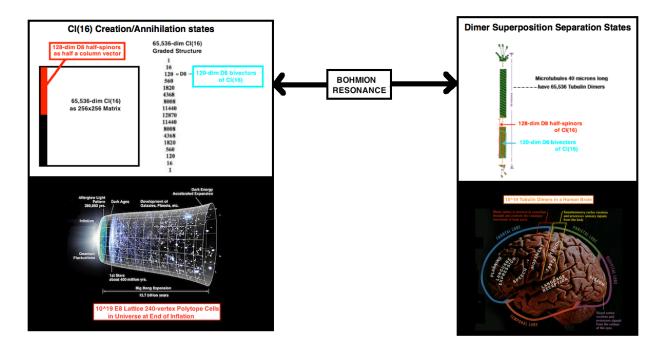


with Conformation Electron mass m and State1 / State 0 position separation a . The Superposition Separation Energy Difference (SSEDIFF) is the internal energy E ssediff = $G m^2 / a$

The Bohmion carrier of the Bohm Quantum Potential being massless spin 2 it acts with respect to the SSEDIFF as a spin 2 graviton would act, seeing its energy as Bohm Quantum Potential internal energy.

CI(16) Creation/Annihilation states

The Bohmion carrier of the Bohm Quantum Potential acts on the Cl(16) Creation-Annihilation Operators of E8 Physics as Bohm Quantum Operators. The Cl(16) Bohm Quantum Creation / Annihilation Operators are represented by the E8 Maximal Contraction generalized Heisenberg Algebra h92 x A7 = 28 + 64 + ((SL(8,R)+1) + 64 + 28) Bohmions mediate Resonance between Planck-scale CI(1,25) cells of E8-CI(16) Quantum Spacetime and Microbule Quantum Consciousness Patterns in the human brain



Dennis, de Gosson, and Hiley (arXiv 1412.5133) say "... Bohm's Quantum Potential can be viewed as an internal energy of a quantum system ..."

Peter R. Holland says in "The Quantum Theory of Motion" (Cambridge 1993): "... the total force ... from the quantum potential ... does not ... fall off with distance ... because ... the quantum potential ... depends on the form of ...[the quantum state]... rather than ... its ... magnitude ...".

Therefore:

Resonant Connections can exist among Spatially Distant Elements.

How does an Element find a Spatially Distant Resonant Connection Element ?

Feynman's Path Integral formulation of Quantum Theory shows that the amplitude for any Real Quantum Path from state A to state B is the sum the amplitudes of All Virtual Possible Paths from A to B. Therefore,

Virtual Bohmions must connect the Initial Element A

to each and every Intermediate Element on each and every Virtual Path from A to B and

the Initial Element must Virtually see every other Element in Our Universe and be able to evaluate (effectively instantaneously) whether or not it is Resonant.

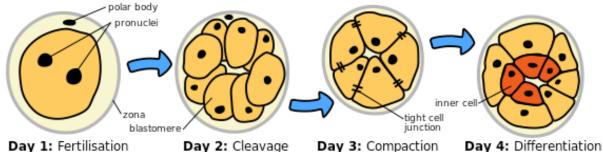
If ANY other Element (no matter how distant) is Resonant with the Initial Element, a Resonant Connection is established, effectively instantaneously.

Some properties of Resonance are discussed (from the point of view of

electromagnetic interactions) by Carver Mead in his book Collective Electrodynamics (MIT 2000): "... Any energy leaving one resonator is tranferred to some other resonator, somewhere in the universe. ... With the two resonators coupled, the energy shifts back and forth between the two resonators in such a way that the total energy is constant ... The conservation of energy holds despite an arbitrary separation between the resonators; it is a direct result of the symmetry of the advanced and retarded potentials. There is no energy "in transit" between them. ... the universe contains a truly enormous number of resonators ...".

Is there a Resonant Copy of You in the Planck-scale Cells of Spacetime ?

When You were conceived You were a Single Cell whose Microtubules could resonate



Day 1: Fertilisation

(image from Wikipedia on Human_embryogenesis)

with a corresponding Resonant Set of Planck-scale Cells of Spacetime. Then Your Single Cell divide by mitosis into 2 cells and your Resonant Cell also divides. After 2 more divisions You and your Resonant Set have cleaved into 8 similar Cells. When the cells divide into 16, cleavage continues as cellular differentiation.

8 cells represent the Cl(8) level of information, 2⁸ = 256 only on the order of 248-dim E8, so all cells are similar. 16 cells represent the Cl(16) level of information, 2¹⁶ = 65,536 much more that the 248 of E8, so there is enough information for differentiation.

Your growth is mirrored in a corresponding Resonant Set of Planck-scale Spacetime Cells.

```
<--- Bohmion Connection --->
Microtubule You
                                                     Planck-scale Resonant You
     ٨
                                                               ٨
      L
                                                               I
      I
                                                               I
Standard Model
                                                       Global E8 Spacetime
 NJL Higgs
                                                          NJL E8 Lattice
 Connection
                                                           Connection
                                                               L
      L
      L
                                                               I
     V
                                                               V
Your Near Neighbors
                                                     Other Planck-scale Sets
 in Physical M4
                                                 Resonating with Resonant You
```

The Higgs NJL Condensate mediating the Connection between You and Your Neighbors is Short-Range as it does not extend much beyond the scale of the Standard Model Fermions and Bosons to which the Higgs mechanism gives mass. Therefore, You may get a lot of detailed information from Your Near Neighbors, but You will not get much information from Neighbors that are Distant in Space or Time.

The E8 Spacetime NJL Condensate mediating between Your Resonant Set and Other E8 Resonant Sets is Long-Range as it extends throughout E8 Spacetime of Our Universe. D8 brane Spacetime has Planck-scale Lattice Structure superposition of 8 E8 Lattices:



As aimath.org/E8/e8graphinfo.html states: "... Crystal Graph for E8 ...



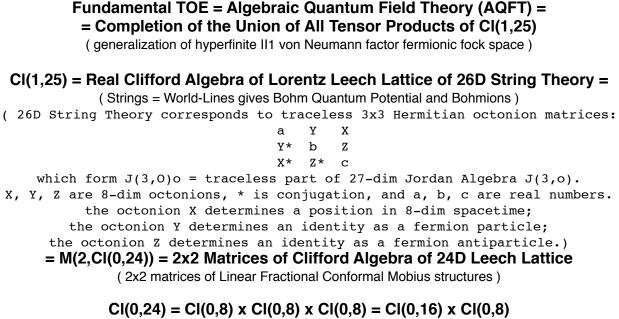
... This is a picture of the 248-dimensional Lie algebra of E_8 There are 248 nodes in the picture, one for each basis element of the Lie algebra. ... The Lie algebra of E_8 is generated by 8 pairs of elements (X,Y), one pair for each of the colored nodes in the Dynkin diagram. ...".

Since the E8 Spacetime lattices extend throughout Our Universe, Your Resonant Set is a part of an NJL Condensate that is connected by E8 lattices to ALL Resonant Sets in Our Universe, and can be in Resonant Connection with ANY of them.

For example, if Beethoven's Opus 131 14th String Quartet is in Your Consciousness, then Your Spirit Resonant Set can make Resonant E8 lattice Connection with the Spirit Resonant Set of Beethoven, and then by Bohmion Connection,

Beethoven's Spirit can have Resonant Connection with You.

Here is an overview of the Fundamental Structure of my E8 Physics model:

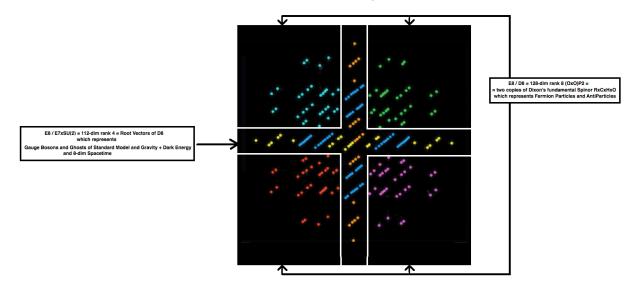


(8-Periodicity tensor product of Cl(0,8)) (Leech Lattice as 3 copies of E8 Lattice - shown by Dixon)

CI(0,16) contains E8 as 120-dim D8 BiVectors + 128-dim D8 half-spinors E8 contains recipe for Local Lagrangian of Standard Model and Gravity + Dark Energy

240 Root Vectors of E8 are represented by two Symmetric Spaces:

E8 / D8 = 128-dim rank 8 (OxO)P2 = = two copies of Dixon's fundamental Spinor RxCxHxO which represents Fermion Particles and AntiParticles



E8 / E7xSU(2) = 112-dim rank 4 = Root Vectors of D8 which represents 8-dim Spacetime and Gauge Bosons and Ghosts of Standard Model and Gravity + Dark Energy